

NANOMAGNETISM (I)

WHAT IS IT????

SO WHAT????

Robert D. Shull

**Leader: Magnetic Materials Group,
National Institute of Standards and Technology**

**Member: OSTP Nanoscale Science, Engineering
and Technology Subcommittee, NSET**

V. President: The Minerals, Metals, & Materials Society (TMS)



Magnetic Materials Group



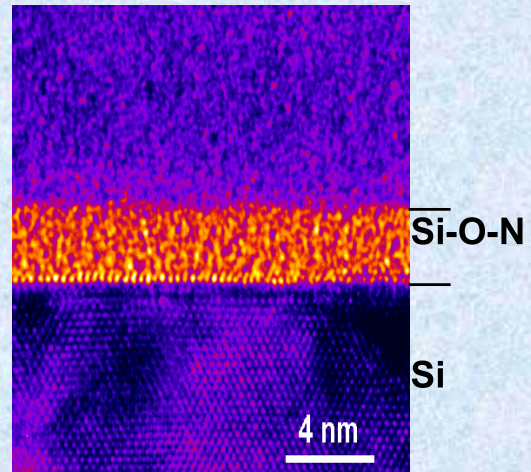
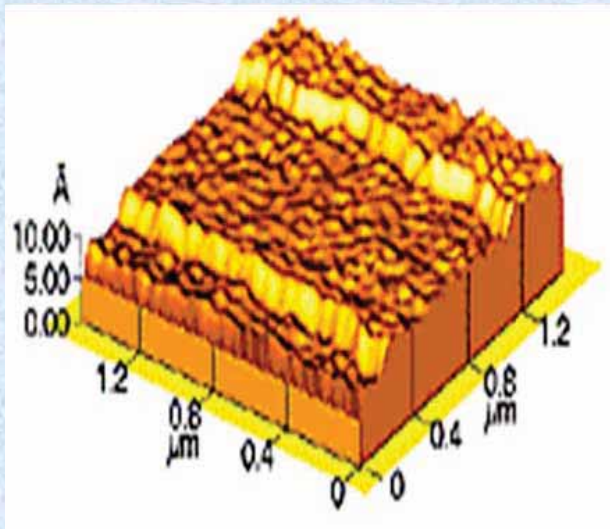
OUTLINE

- (I). **What is Nanotechnology??**
- (II). **Why is it Different???**
- (III). **Nanomagnetism Changes**
 - New Magnetic States
 - Time Dependence
 - Soft Magnetic Behavior
- (IV). **Summary**

NIST

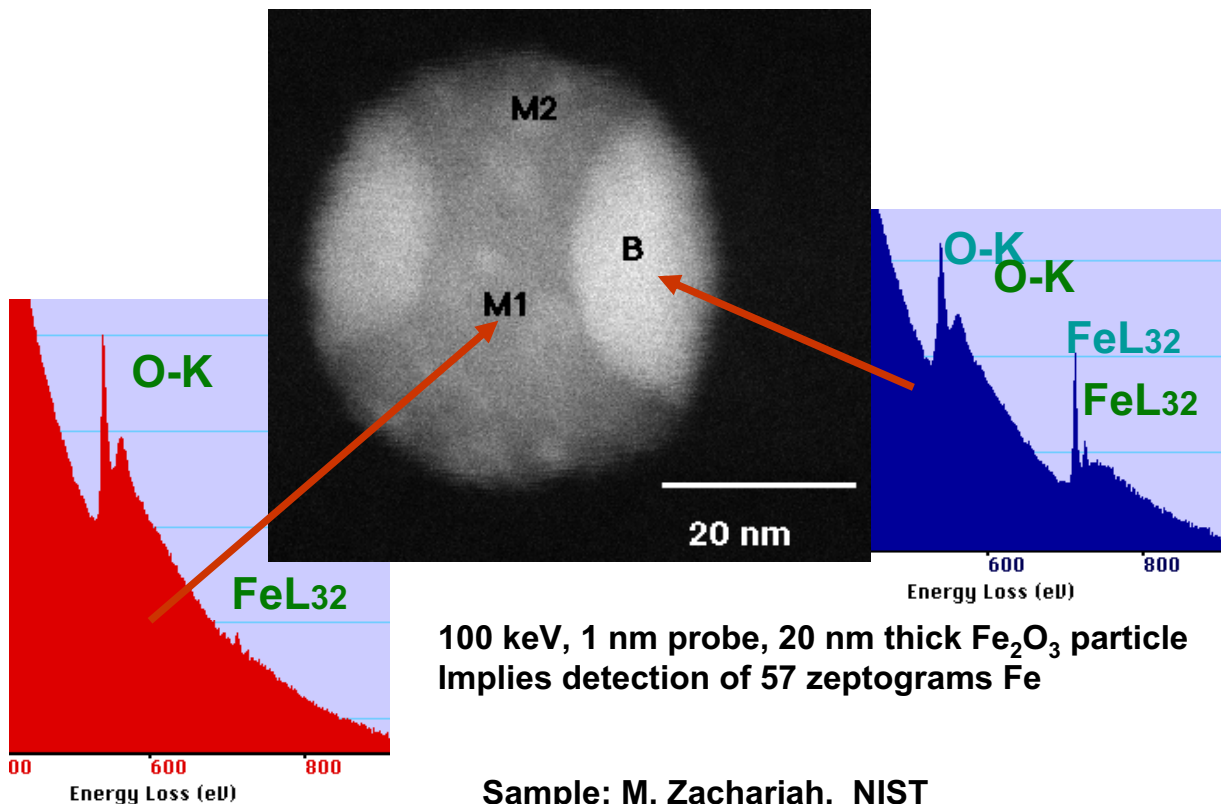
National Institute of Standards and Technology

NANOTECHNOLOGY IS THE ABILITY TO CONSTRUCT STRUCTURES WITH ATOMIC LEVEL CONTROL



Silicon Oxynitride
On Silicon
(J.H. Scott, NIST)

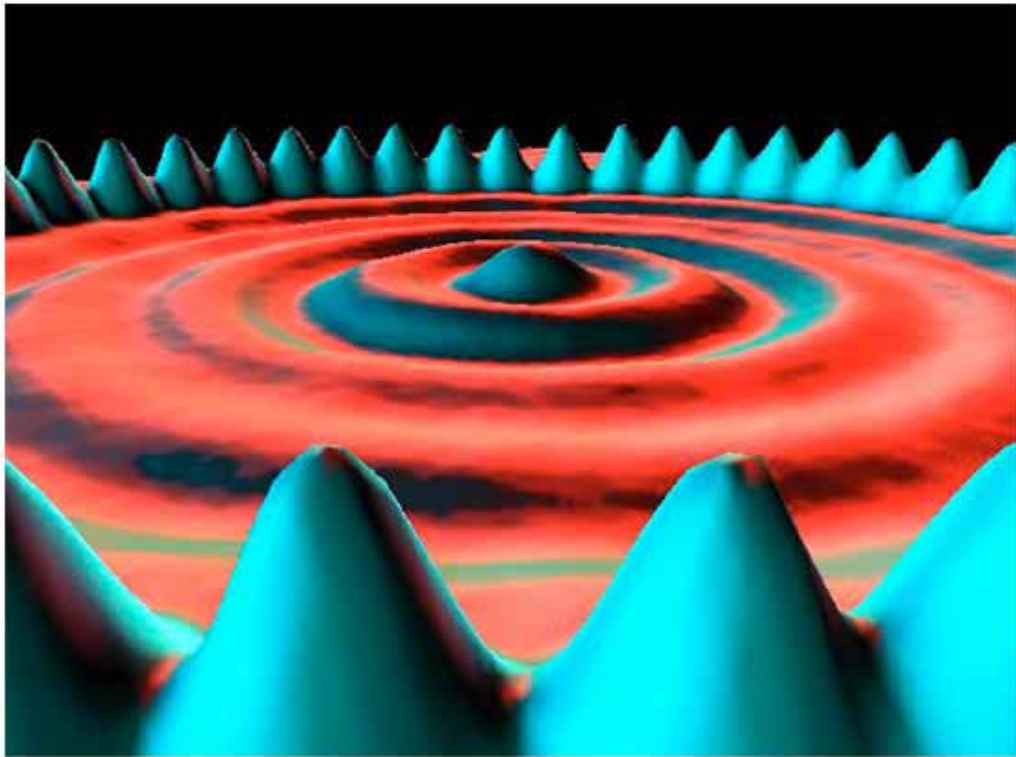
Flame Synthesized $\text{SiO}_2\text{-Fe}_2\text{O}_3$



100 keV, 1 nm probe, 20 nm thick Fe_2O_3 particle
Implies detection of 57 zeptograms Fe

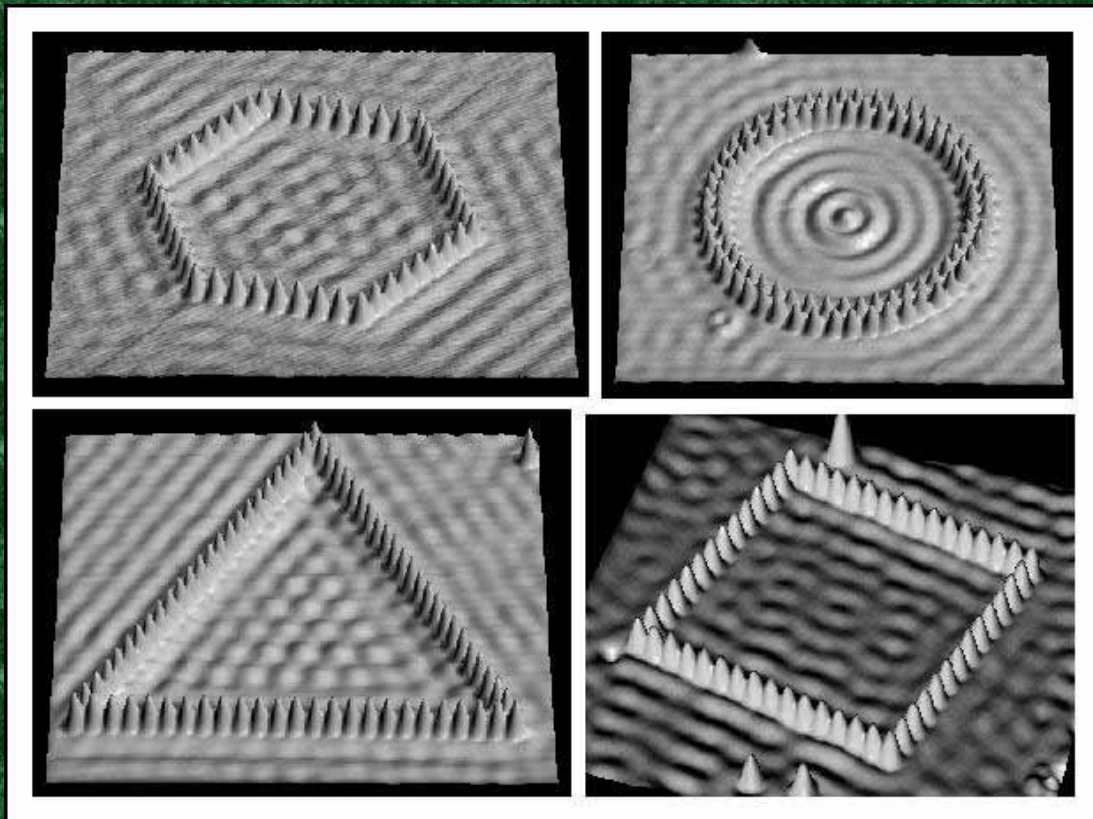
Sample: M. Zachariah, NIST
Analysis: D. Newbury, NIST

QUANTUM CORRAL (Fe atoms on Cu)



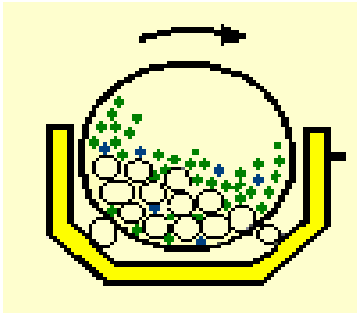
(Don Eigler, IBM-Almaden)

QUANTUM CORRALS (Fe on Cu)



(Don Eigler, IBM Almaden)

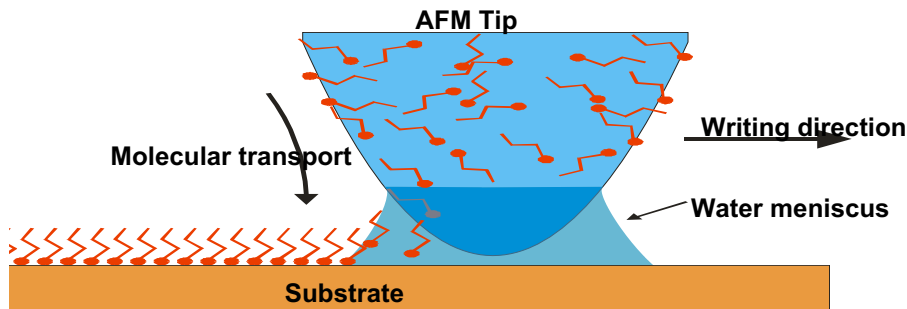
PRODUCTION METHODS



Mechanical Alloying



Plasma or Vapor Deposition

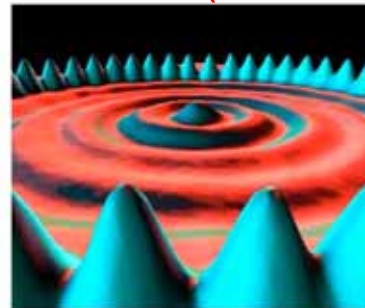


Dip Pen Lithography: Chad Mirkin (Northwestern Univ.)

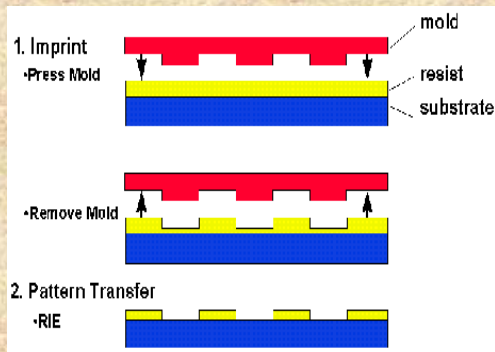
PRODUCTION METHODS

- Sputtering**
- Inert Gas Condensation (IGC)**
- Plasma Vapor Deposition (PVD)**
- Condensed Vapor Deposition (CVD)**
- Pulsed Laser Deposition (PLD)**
- Chemical Precipitation from Solution**
- Ion Replacement & Reduction**
- Sol Gel Chemistry**
- Solid Solution Precipitation**
- Rapid Solidification (RSP)**
- Mechanical Alloying (MA)**
- Electrodeposition**
- Filling of Nanopores**
- Dip Pen Lithography**
- Nanoimprint Lithography (NIL)**
- Atomic Force Microscope**
- Self Assembled Monolayers (SAMs)**
- ⋮

QUANTUM CORRAL (Fe atoms on Cu)



AFM - D. Eigler (IBM)

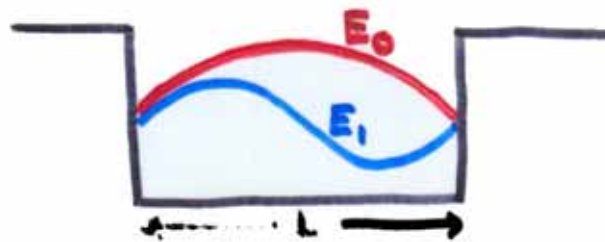


NIL - S. Chou (Princeton)

THREE REASONS
WHY PROPERTIES ARE DIFFERENT
WHEN MATERIALS POSSESS
SOME NANOSCALE DIMENSION

(1)

Quantization
of Energy States

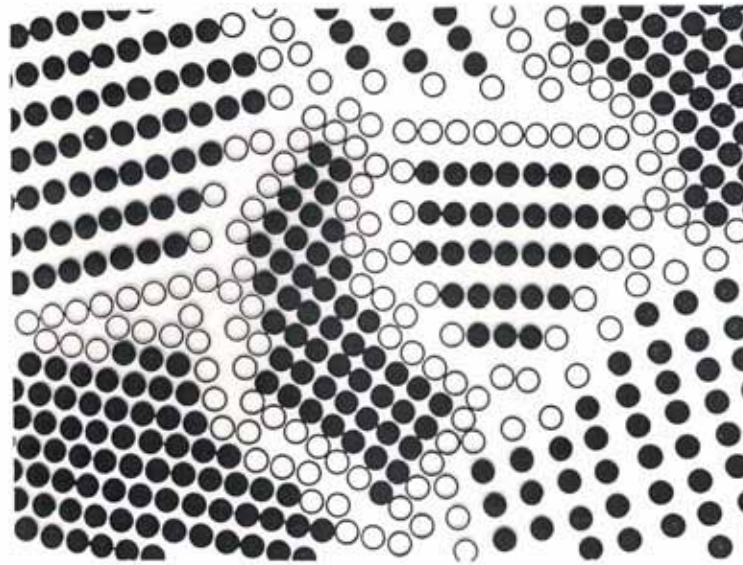


$$E_n = \frac{n^2 \epsilon}{L^2}$$

"Confinement" Effects

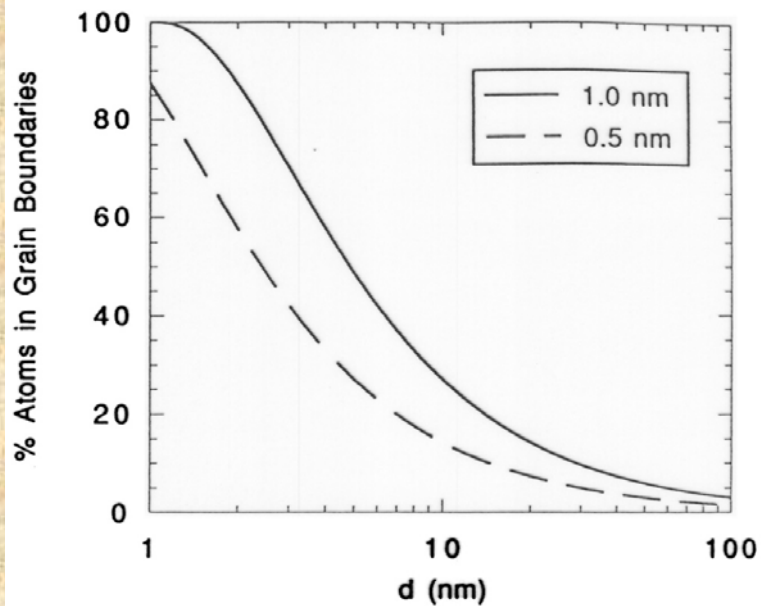
(2)

STRUCTURE SCHEMATIC: -NANOPHASE MATERIAL-



Schematic of an equiaxed nanocrystalline metal showing atoms associated with individual grains (filled circles) and those constituting the grain boundaries (open circles). [H. Gleiter, Prog. Mater. Sci. 89, 223 (1989)]

HIGH INTERFACE VOLUME -NANOPHASE MATERIALS-



Percentage of atoms in grain boundaries of a nanophase material as a function of grain diameter, with grain boundary thickness of 0.5 and 1.0 nm (i.e., 2 or 4 atomic planes). [R.W. Siegel, Annu. Rev. Mater. Sci. 21, 559 (1991)]

(3)

CRITICAL LENGTH SCALES

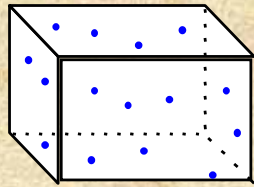
Resistivity – mean free path
Thermal Conductivity – mean free path
Strength – dislocation Burgers vector
Transmission & Reflection - wavelength
Diffraction & Scattering - wavelength
Absorption – penetration depth
Atomic Transport – diffusion length
Superconductivity – coherence length
Elasticity – bond & chain lengths
Reaction Rate – diffusion length
Boundary Motion – radius of curvature
Fluid Flow – boundary layer thickness
Magnetism – exchange length, domain wall width

MAGNETIC LENGTH SCALES (IN NANOMETERS)

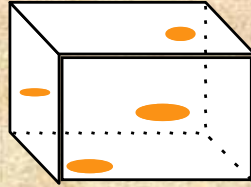
<u>LENGTH</u>	<u>SYMBOL</u>	<u>DEFINITION</u>	<u>Fe</u>	<u>Nd₂Fe₁₄B</u>
Exchange Length	l_{ex}	$\sqrt{(\mu_0 A/J_s^2)}$	1.5	1.9
Coherence Radius	R_{coh}	$(\sqrt{24})l_{ex}$	7	9
Domain Wall Width	δ_w	$\pi l_{ex}/\kappa$	40	3.9
Single-Domain Size	R_{SD}	$36\kappa l_{ex}$	6	107
Superparamagnetic Blocking Radius (at 300 K)	R_B	$(6k_B T/K_1)^{1/3}$	8	1.7

(Calculated by Michael Coey, Univ. of Dublin)

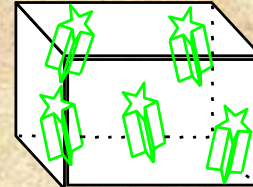
NANOCOMPOSITE MORPHOLOGIES



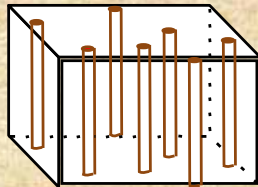
Spherical Particle



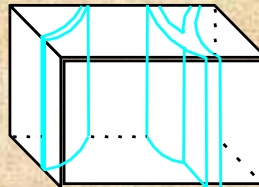
Disc-Shaped Particle



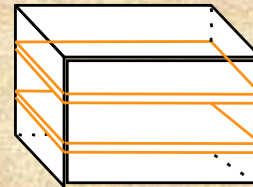
Rod-Shaped Particle



Fiber



Intergranular Film



Layered

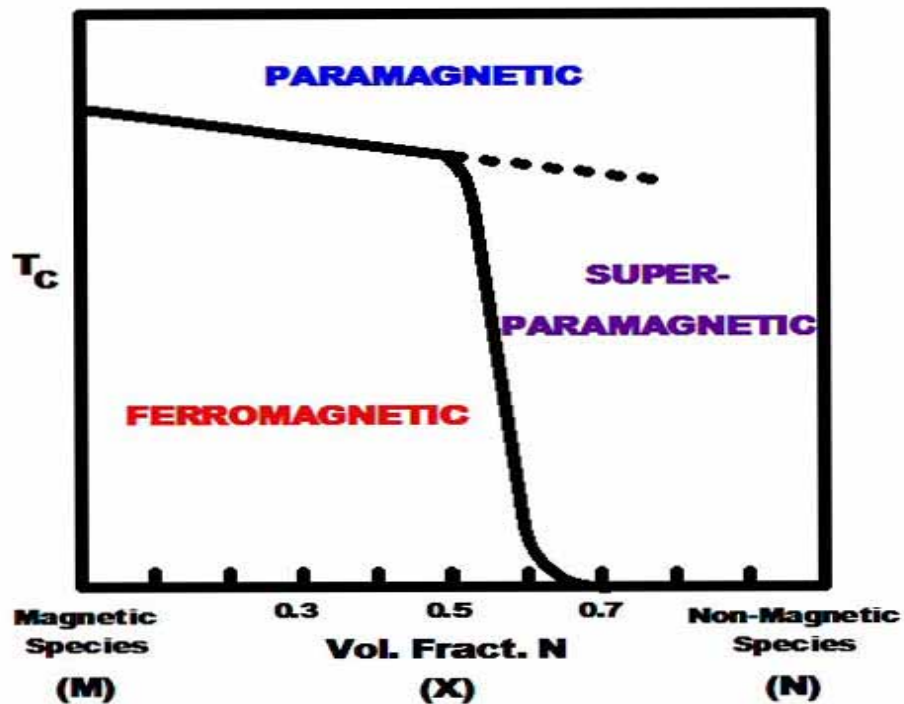
Critical Dimensions:

Particle Diameter, Separation Distance, Aspect Ratio,
Fiber Diameter, Layer Thickness, Grain Diameter, ...

NANOCOMPOSITE

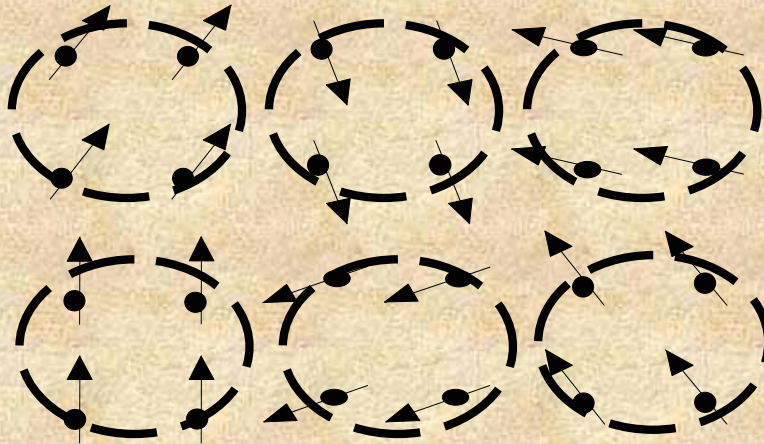


MAGNETIC PHASE DIAGRAM





SMALL PARTICLE BEHAVIOR

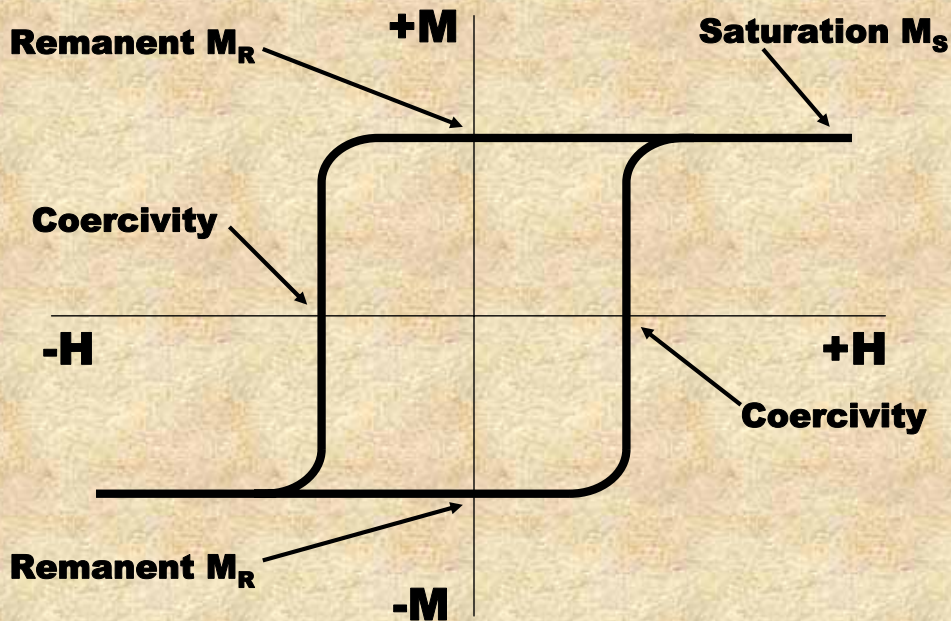


Assembly of magnetic clusters (each comprised of many ferromagnetically-aligned elemental moments of magnitude μ) acting independently.

= Superparamagnetic Material:

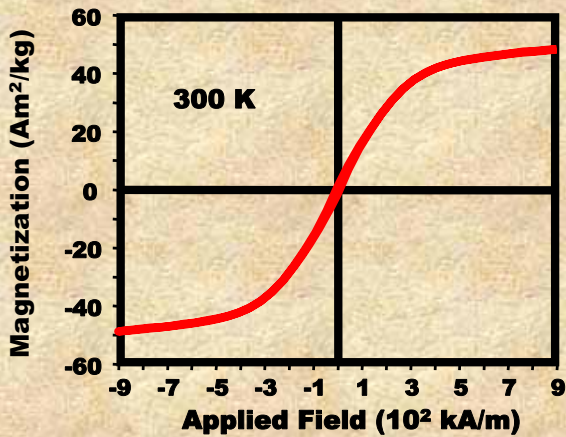


HYSTERESIS LOOP OF A FERROMAGNET





SUPERPARAMAGNETISM

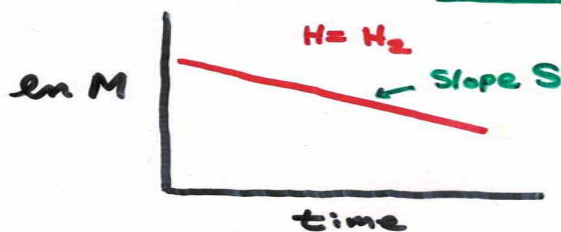
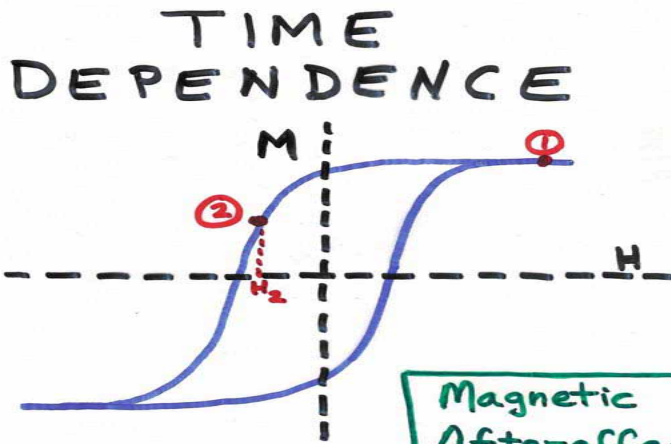


Applications:

- Magnetic Inks**
- Magnetic Separation**
- Vacuum Sealing**
- Magnetic Marking**
- Magnetic Refrigeration**
- Magnetic Resonance Imaging**

No Remaining Magnetism Upon Field Removal!!!

(Occurs when Particles are Very Small and Decoupled)

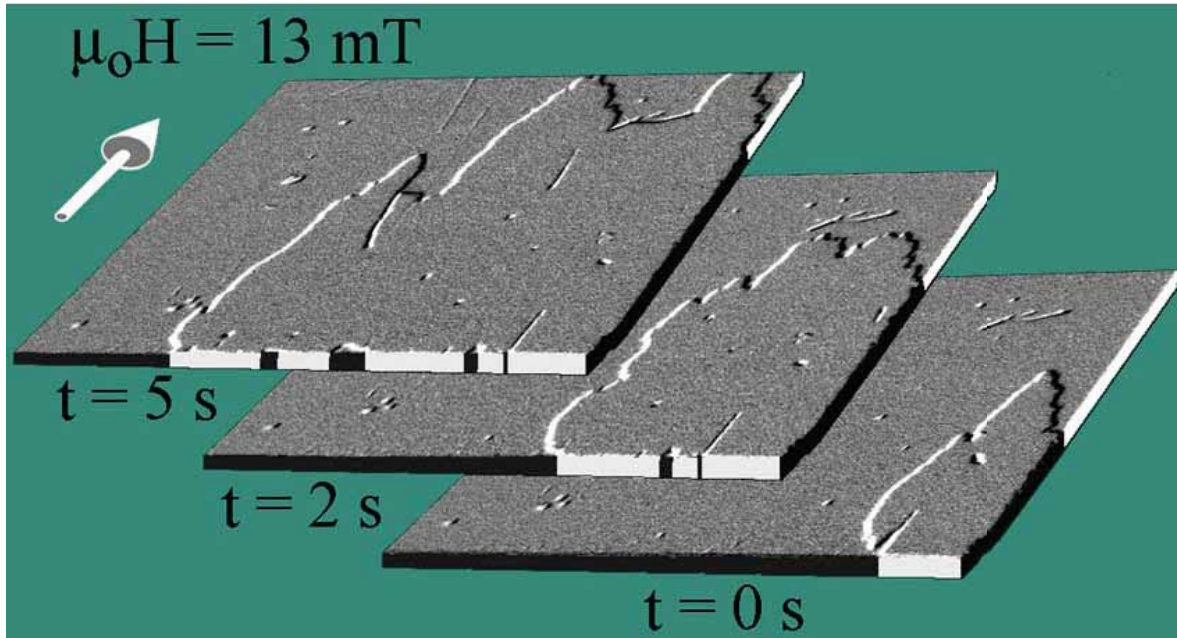


A New Concern for Nano-Magnetic Materials

For conventional Ferromagnets, there is no time dependence, so this is a new constraint on the application of Nanomagnets.



Time Dependent Domain Activity



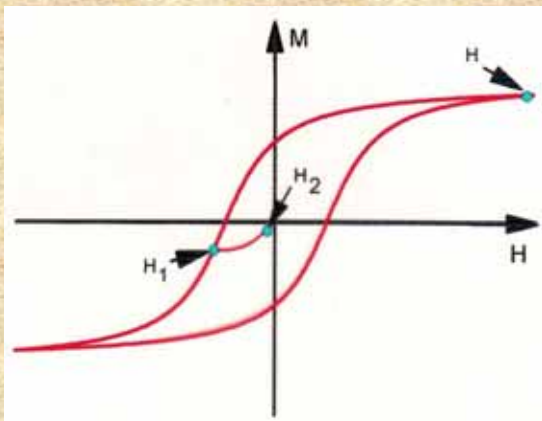
**Co(2.5 nm)/Ru(0.5 nm)/Co(2.1 nm) Synthetic AF Media
 - The New Type of High Density Recording Media**



Magnetic Materials Group



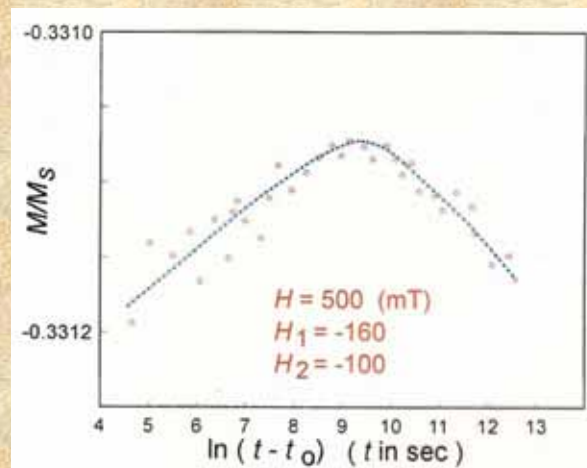
TIME DEPENDENCE



**Two-Step Field-
Change Method**

**Which Method
is Best???**

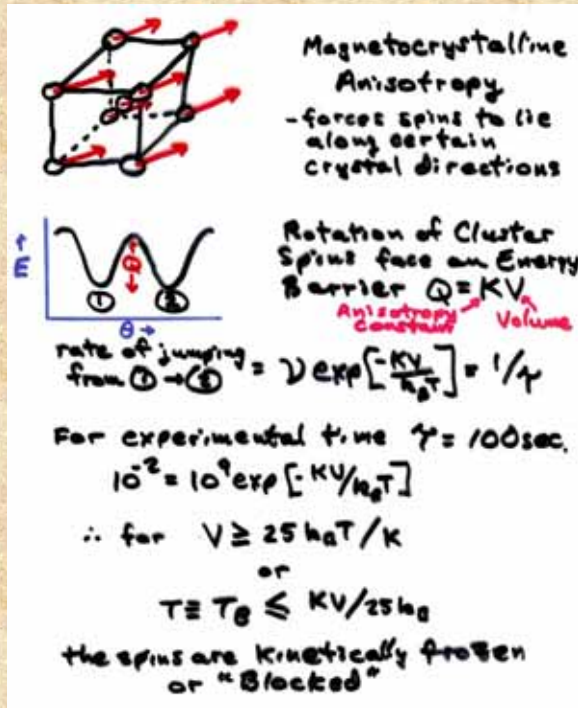
**Results in
2 Time Constants!**



NIST

National Institute of Standards and Technology

Kinetically Frozen Nanoparticle Moments



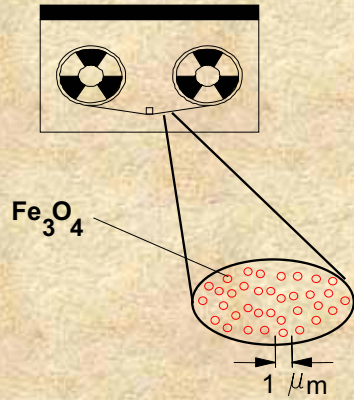
In nanoparticles, the Magnetic moments can be kinetically frozen if the temperature is low enough. That temperature is called the "blocking" temperature: T_B . That temperature depends slightly upon how it is measured. It also depends on the Volume of the material and the magnetic anisotropy of that material.

**HIGHER DENSITY
MAGNETIC RECORDING MEDIA
CHANGES WITH SIZE REDUCTION
(BOTH THICKNESS & LATERAL SIZE)**



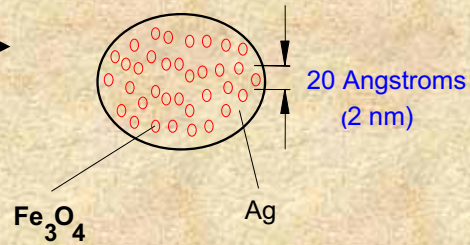
IMPROVED MAGNETIC RECORDING MEDIA

Conventional Media



High Density Media

NANOCOMPOSITES



Higher Density Achieved by Reduction of "Bit" Size so there are More Bits/Unit Area



NOVEL Metal-C60 Nanocrystalline Magnetic Thin Films

Co-C60

Fe-C60

Fe

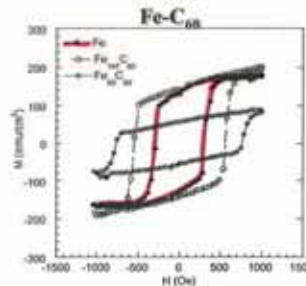
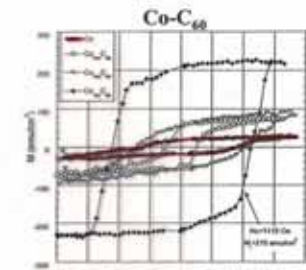
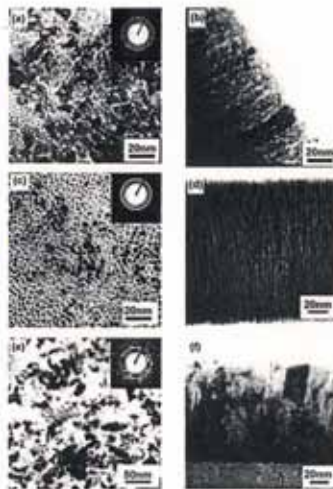


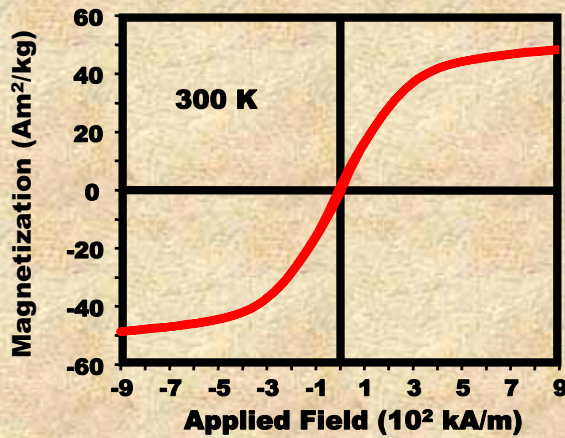
FIG. 3. TEM phase view with diffraction pattern and cross-section images revealing grain structures that have evolved by integrating C₆₀ molecules into the Fe and Co magnetic films; (a) and (b) are from the Co₁₀₀C₆₀ film; (c) and (d) are from the Fe₁₀₀C₆₀ film; (e) and (f) are from the pure Fe film.

L.A. Zheng, B.M. Lairson, E.V. Barrera, R.D. Shull, APL 77, 3242 (2000)



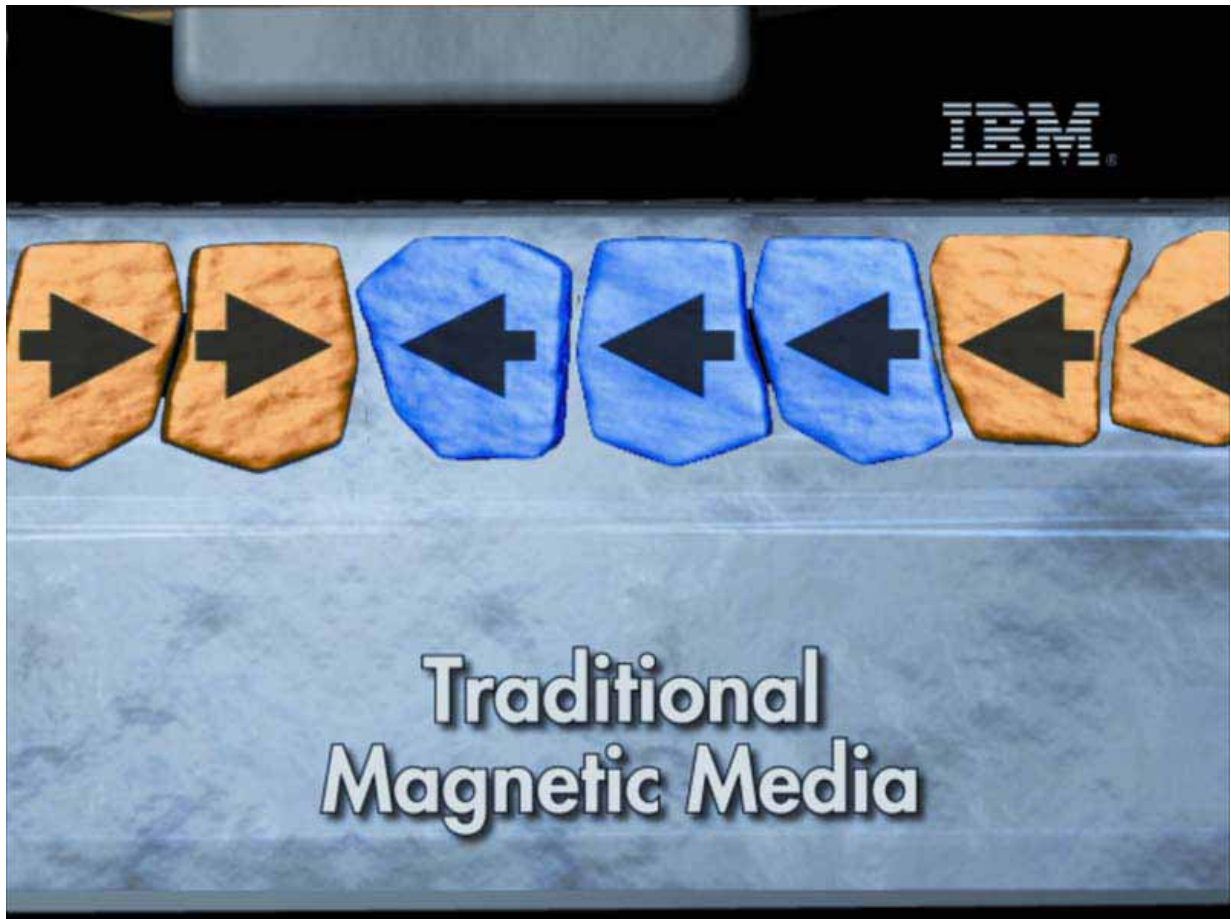


SUPERPARAMAGNETISM SETS A LIMIT TO PARTICLE (“BIT”) SIZE REDUCTION!!!



- Applications:**
- Magnetic Inks
 - Magnetic Separation
 - Vacuum Sealing
 - Magnetic Marking
 - Magnetic Refrigeration
 - Magnetic Resonance Imaging

**No Remaining Magnetism Upon Field Removal!!!
(Occurs when Particles are Very Small and Decoupled)**



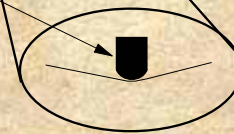
**NEED FOR
HIGHER
SENSITIVITY
MAGNETIC
FIELD
SENSORS
WITH
PARTICLE
SIZE
REDUCTION**

(Also true for Biological Applications of Small Magnetic Particles)

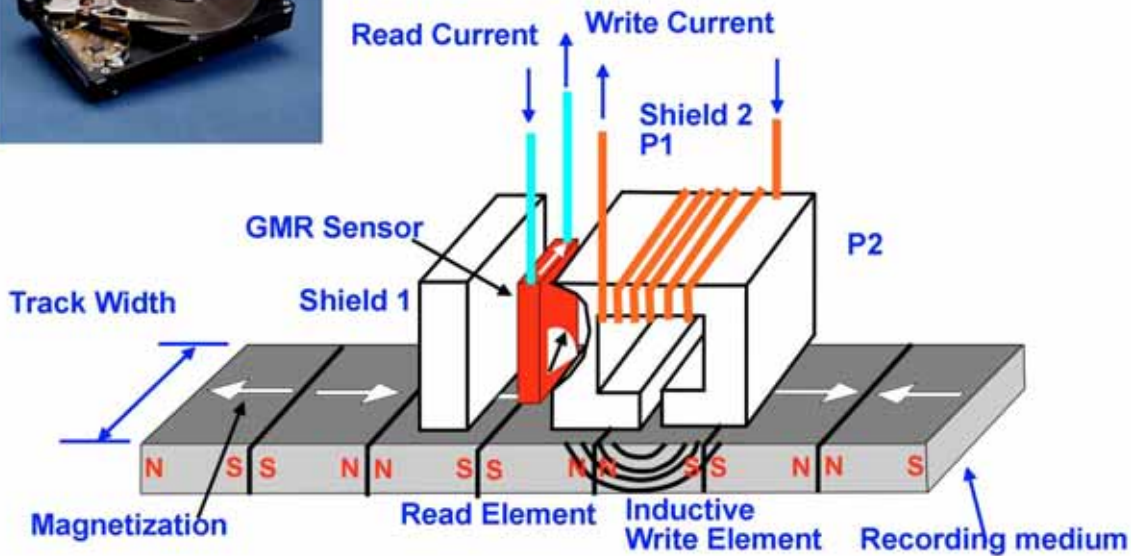
**MAGNETORESISTANCE
Recorder Heads**



Magneto-resistive
Read Head
(e.g., permalloy)
($\Delta\rho/\rho = 2.5\%$)

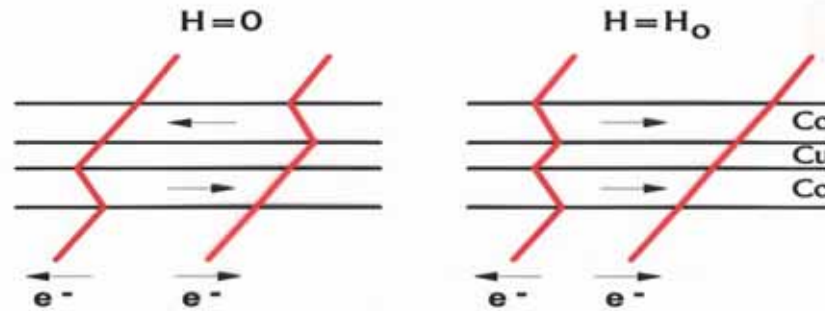


**Giant Magnetoresistance
(GMR) Heads**
($\Delta\rho/\rho > 50\%$)

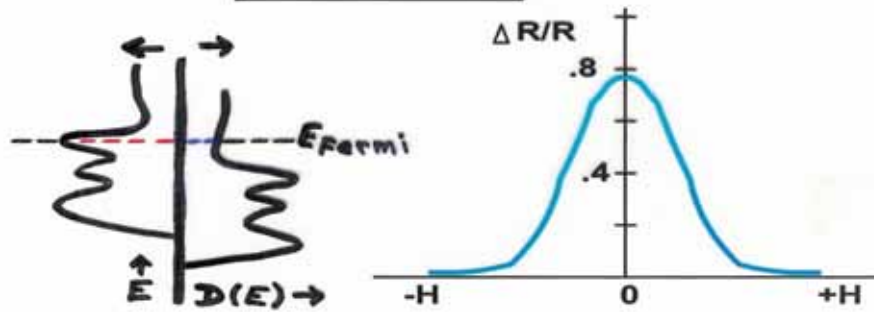


Magnetic recording process.

GIANT MAGNETORESISTANCE FIELD SENSORS

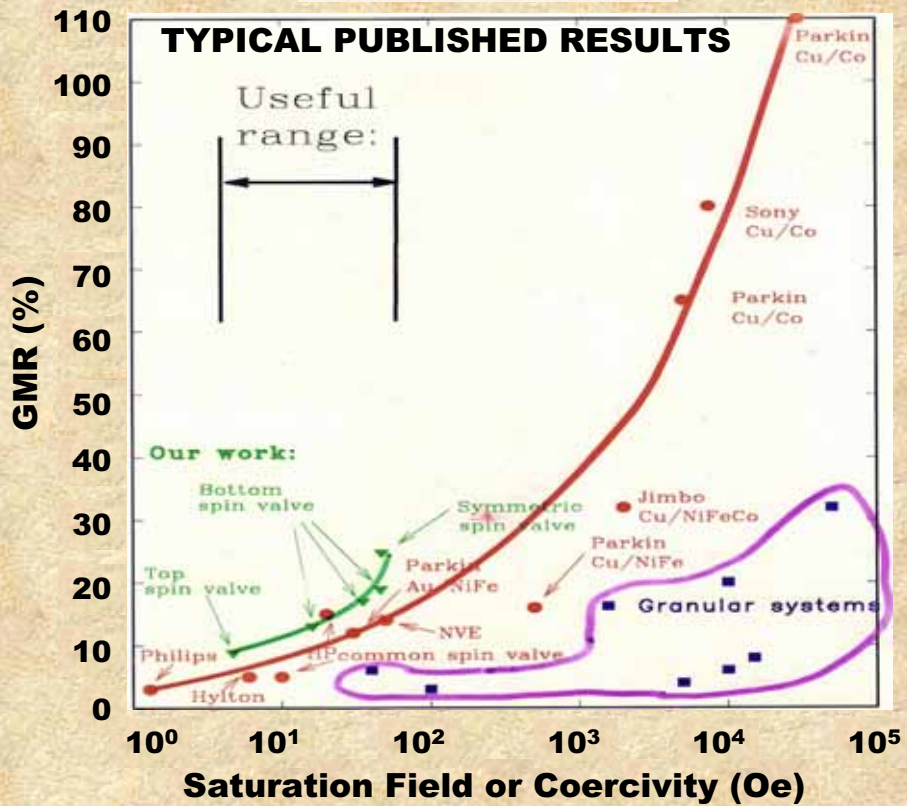


$$\frac{1}{R} = \frac{1}{\bar{R}} + \frac{1}{\bar{R}}$$



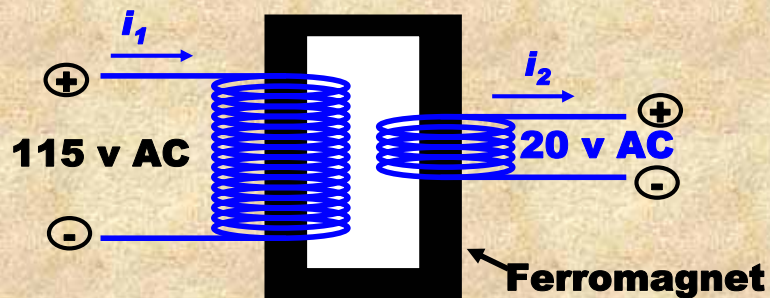
[Baibich, et. al., Phys. Rev. Lett. **61**, 2472 (1988).]

Magnetic Materials Group

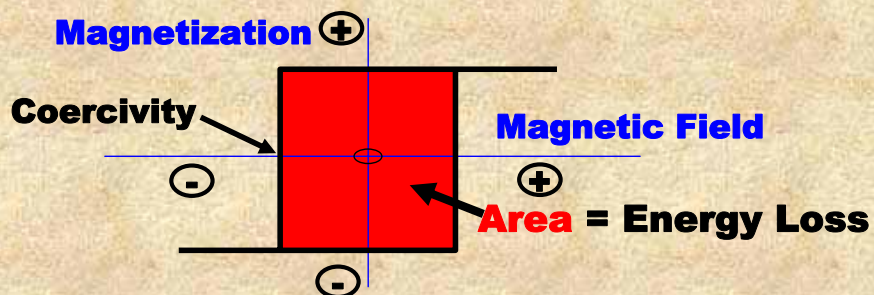


**SOFT MAGNETIC
PROPERTIES ARE DIFFERENT
WHEN MATERIALS POSSESS
SOME NANOSCALE DIMENSION**

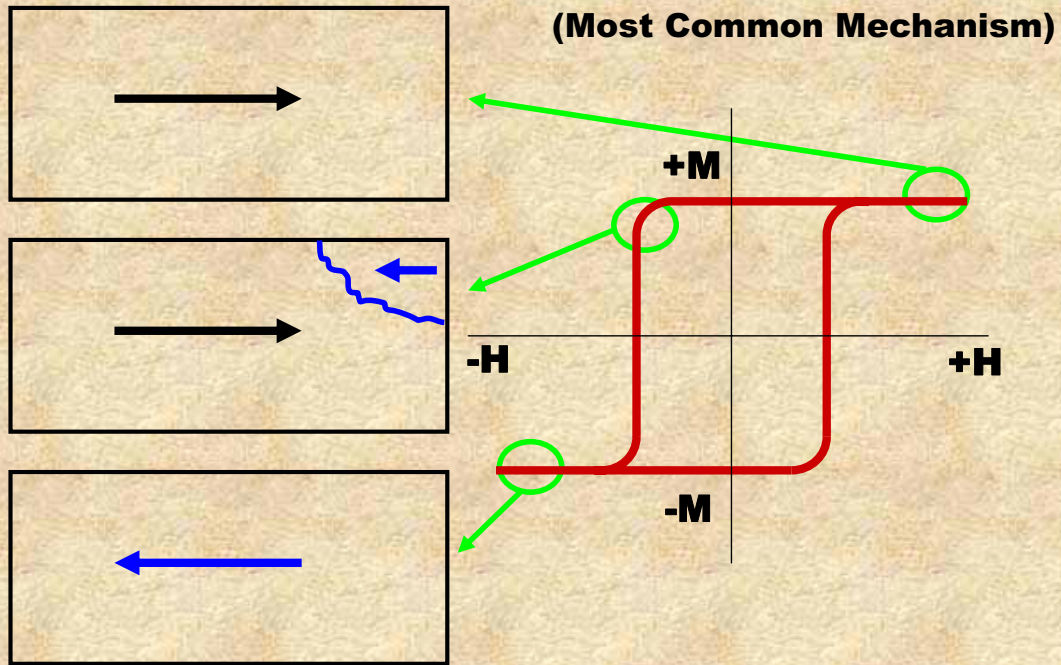
TRANSFORMER



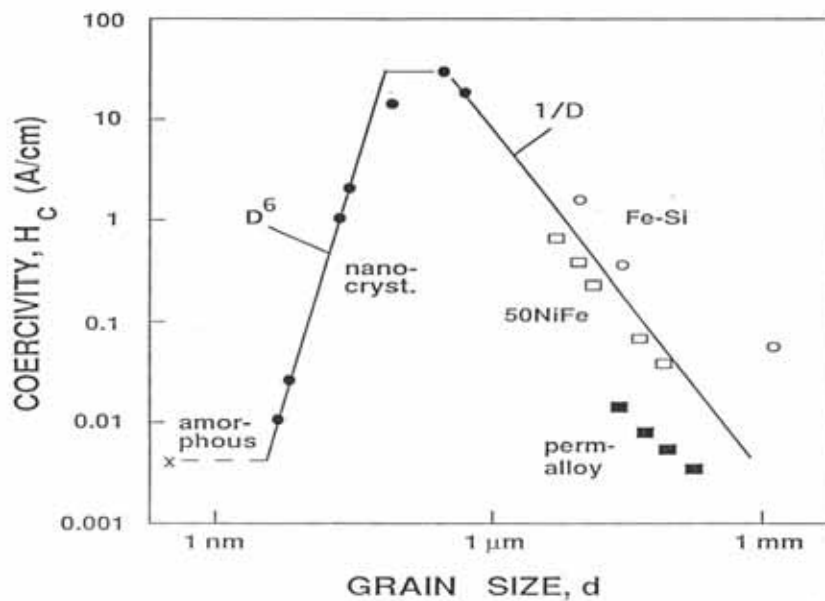
"Hysteresis Loop" of Ferromagnet



Magnetization Reversal by Domain Nucleation & Growth



ENHANCED (AND REDUCED) MAGNETIC COERCIVITY



Magnetic coercivity vs. grain size for several soft ferromagnetic materials. [G. Herzer, IEEE Trans. MAG26, 1397 (1990)]

- **Normally, coercivity increases with decreasing grain size.**
- **But, when the grain size becomes comparable to the domain wall width, magnetic coercivity begins dropping with the grain size and magnetic hysteresis decreases!!!**



Magnetic Materials Group



Summary

- **Increased surface/volume ratio of nanomagnets makes them more susceptible to interaction effects with neighboring magnetic materials.**
- **“Nanostructuring” a material can result in the creation of new magnetic states, like superparamagnetism.**
- **“Nanostructuring” a material can also result in a Time dependence in the magnetization.**
- **Improved magnetic field sensors (using the GMR effect and resonance techniques) are now enabling e more applications, including biomedical.**
- **“Nanostructuring” can also affect Domain motion, making it surprisingly easier & resulting in the best transformers**

NIST

National Institute of Standards and Technology

NANOMAGNETISM (II)

DOMAINS IN NANO-FERROMAGNETS???

Robert D. Shull

**Leader: Magnetic Materials Group,
National Institute of Standards and Technology**

**Member: OSTP Nanoscale Science, Engineering
and Technology Subcommittee, NSET**

V. President: The Minerals, Metals, & Materials Society (TMS)



Magnetic Materials Group



OUTLINE

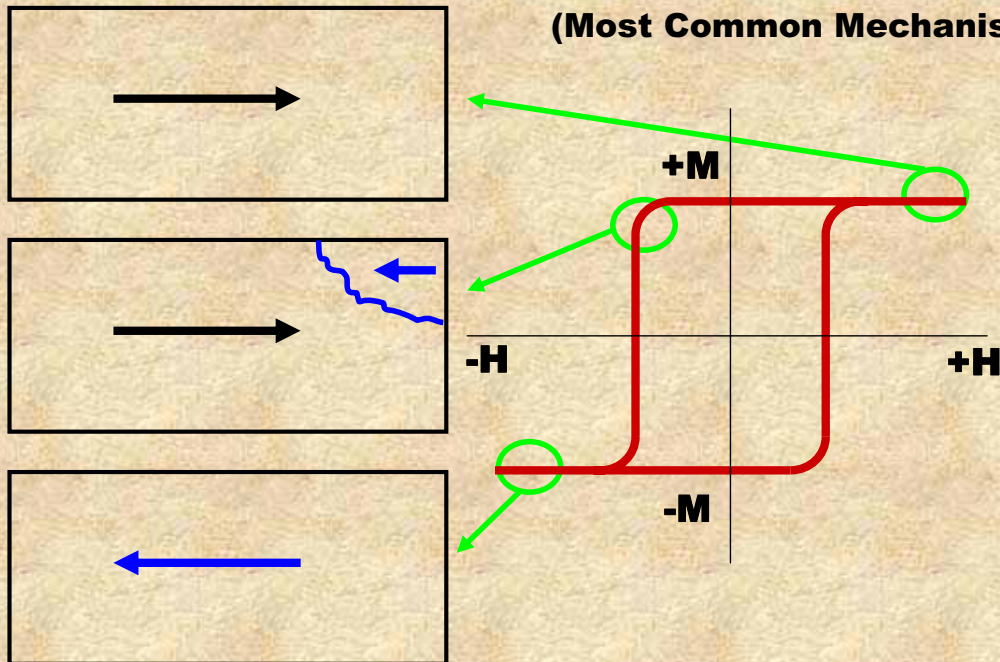
- (I). **Domains in Nanomaterials?**
- (II). **Size Dependence**
- (III). **Domains in Thin Film Nanocomposites**
 - AF/FM Bilayers
 - AF/FM Bilayers (AC-Demagnetized)
 - Hard/Soft FM Bilayers
- (IV). **Summary**

NIST

National Institute of Standards and Technology

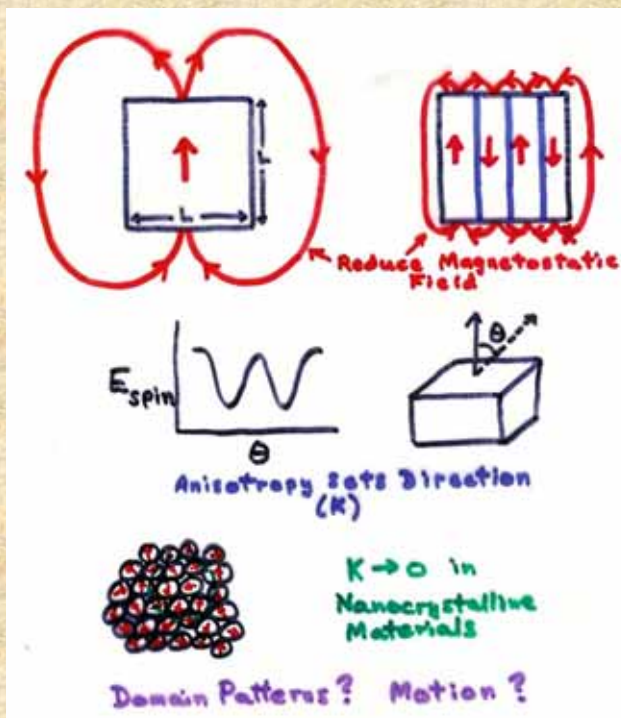
Magnetization Reversal by Domain Nucleation & Growth

(Most Common Mechanism)



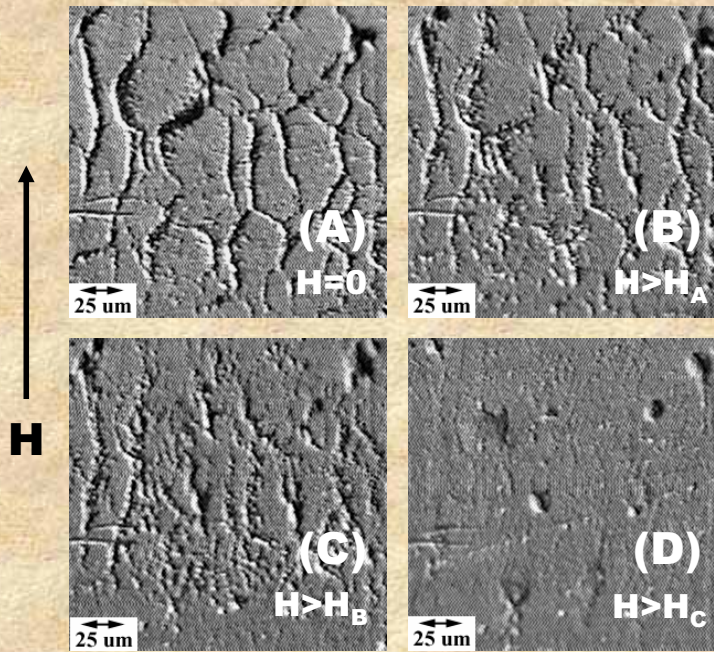
DO DOMAINS EXIST IN NANOCRYSTALLINE FERROMAGNETS???

Domains require an anisotropy to exist. Since the magnetocrystalline anisotropy is thought to go to zero in nanocrystalline materials, do magnetic domains actually exist in these materials???





Domain Patterns in Nanocrystalline ($d=18$ nm) Ni (Imaged by Magnetic Fluid Method)

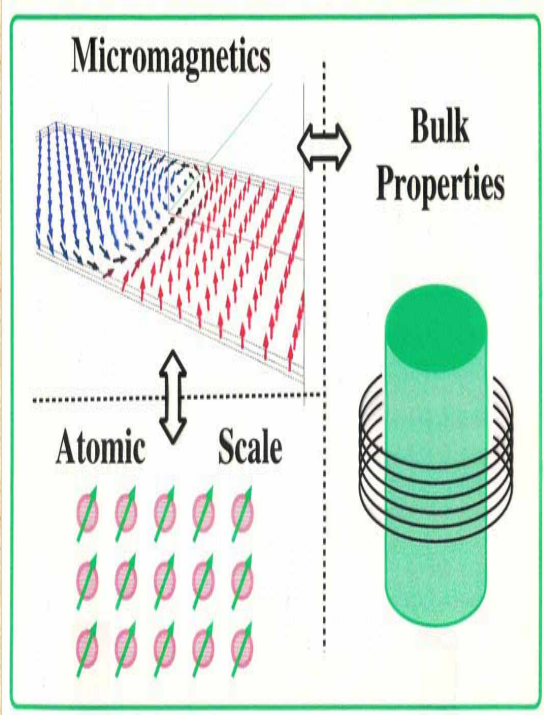


Field dependent patterns in a magnetic fluid on top of Nano-Ni shows domains exist and grow with the field.

The patterns also show the domains are much larger than the grains at $H=0$.

**DOMAIN WALLS
ARE ALSO A FUNCTION OF
SIZE**

Computational Standards



Micromagnetic Equations

$$(1 + \alpha^2) \frac{\partial \mathbf{M}}{\partial t} = -\gamma \mathbf{M} \times \mathbf{H}_{\text{eff}} - \frac{\gamma \alpha}{M_s} \mathbf{M} \times (\mathbf{M} \times \mathbf{H}_{\text{eff}})$$

$$\mathbf{H}_{\text{eff}} = -\partial \mathcal{E}_{\text{tot}} / \partial \mathbf{M}$$

$$\mathcal{E}_{\text{tot}} = \mathcal{E}_{\text{ex}} + \mathcal{E}_{\text{K}} + \mathcal{E}_s + \dots$$

$$\mathcal{E}_{\text{ex}} = \frac{A}{M_s^2} [(\nabla M_x)^2 + (\nabla M_y)^2 + (\nabla M_z)^2]$$

$$\mathcal{E}_{\text{K}} = \frac{K_c}{M_s^2} (M_x^2 M_y^2 + M_y^2 M_z^2 + M_z^2 M_x^2)$$

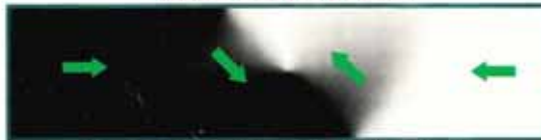
$$\mathcal{E}_s = -\frac{1}{2} \mathbf{M} \cdot \int_V (\nabla \cdot \mathbf{M}) G dv + \int_S \mathbf{M} \cdot \mathbf{n} G ds$$

Zoology of Domain Walls

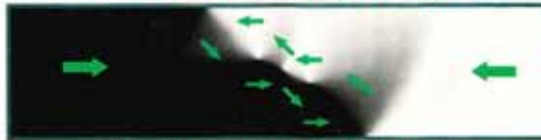
Transverse wall, 250 x 8 nm



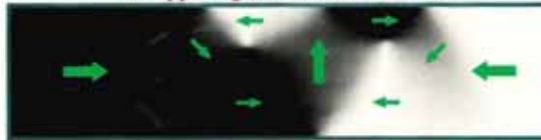
Vortex wall, 250 x 16 nm



Two vortices w/ cross tie, 500 x 16 nm



Two opposing vortices, 250 x 16 nm

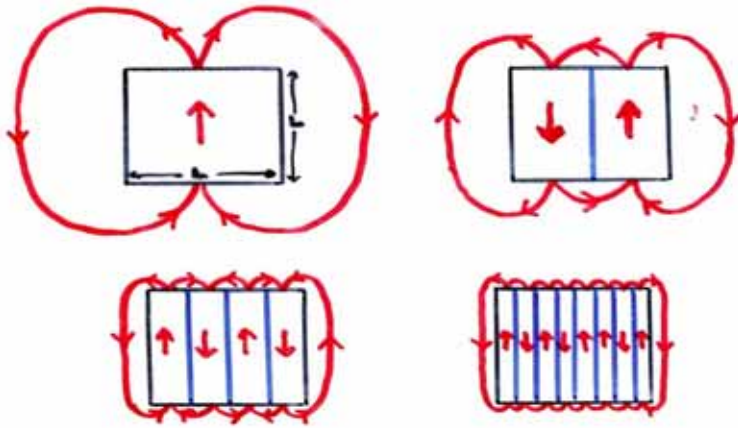


Walls Separating Magnetic Domains Change as the Domain Dimensions Change

This Changes the Way Domains Grow in Response to a Magnetic Field Application.

This Affects the Shape, Width, and Area Enclosed In the Hysteresis Loop of that Material.

DOMAINS



In a Ferromagnet, domains are a way to reduce the magnetostatic energy of the material.

Sooner or later, it costs too much energy to Create a wall.

Particles less than this minimum size are a single magnetic domain.

$$E = E_{\text{magnetostatic}} + E_{\text{wall}}$$

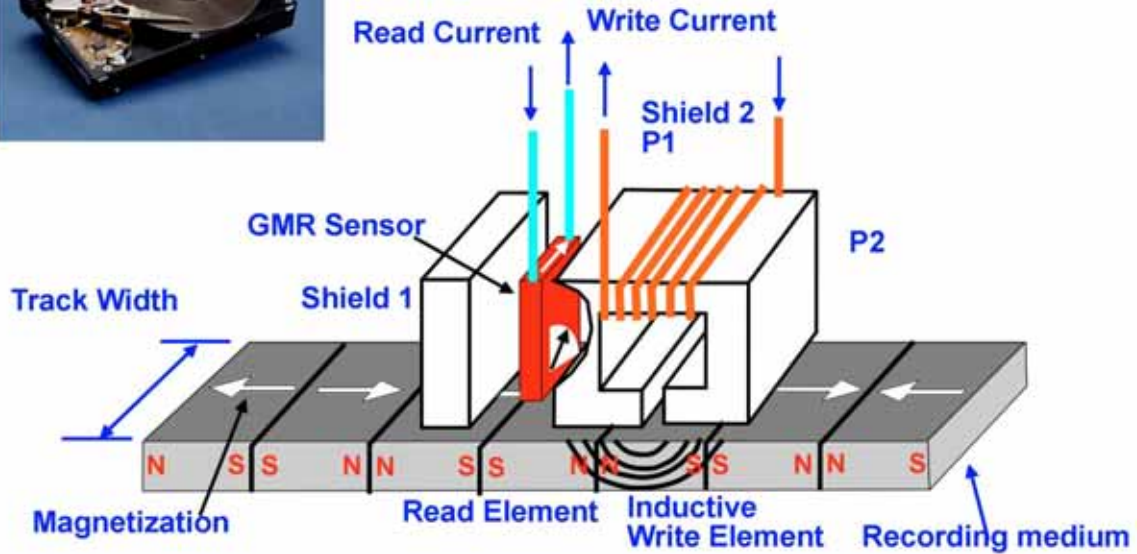
$$= \frac{1}{8\pi} \int_V (H_m)^2 dV + \gamma_{\text{wall}} \frac{L}{t}$$

$\sim L^3$ $\sim L$
thickness

at $\frac{\partial E}{\partial L} = 0$ $L_{\text{SD}} \leq \frac{1.7}{\pi^2} \frac{\gamma}{M_s^2}$ **Single Domain**

EXAMPLE:

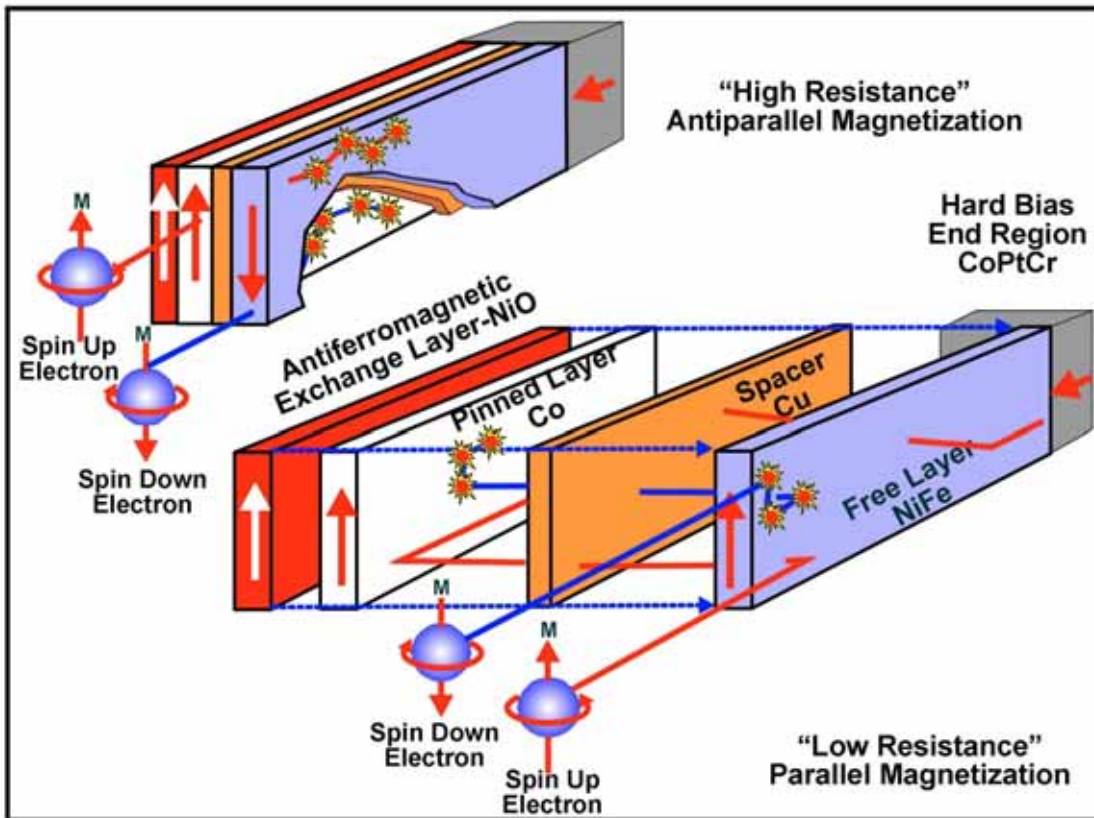
**CHANGE IN DOMAIN DYNAMICS
IN NANOCOMPOSITE SYSTEMS
- IN A SPIN VALVE READ HEAD**



Magnetic recording process.

Ed Grochowski
IBM Almaden Research Center

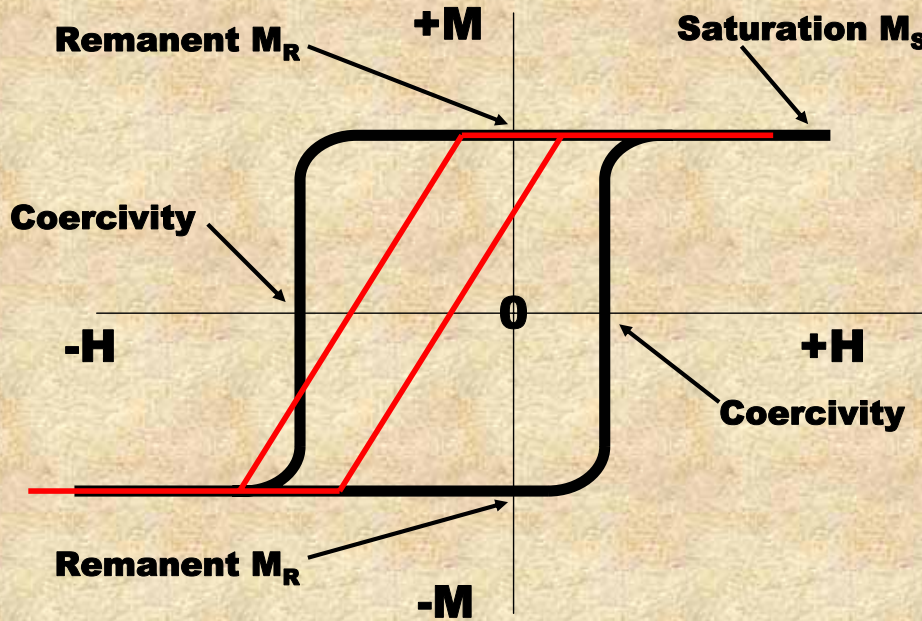
GMR/ Spin valve operation



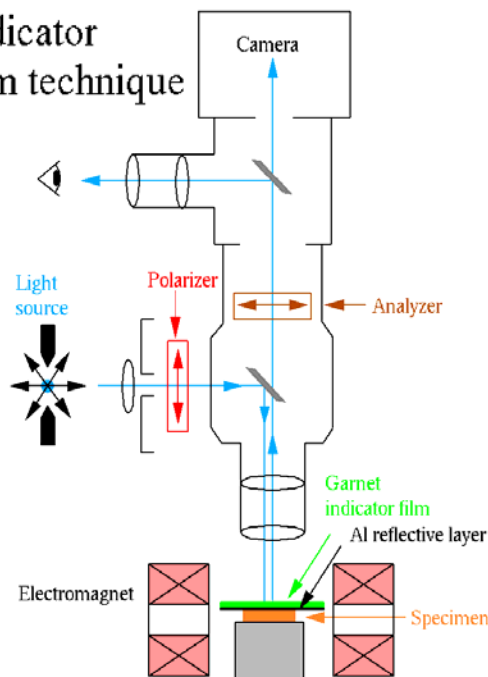
Ed Grochowski
IBM Almaden Research Center



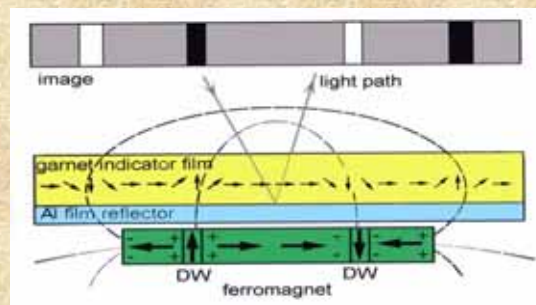
Exchange Bias Hysteresis Loops



Magneto-Optical Indicator Film technique

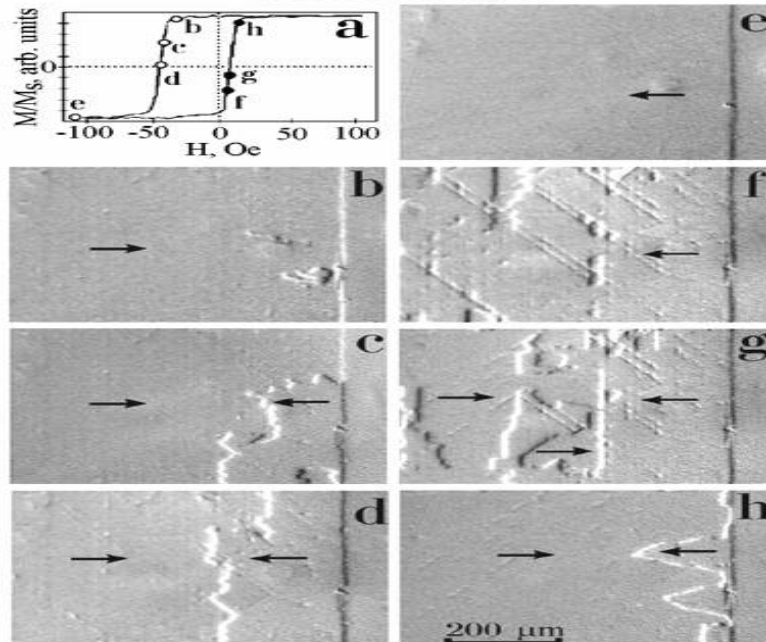


$Gd_3Ga_5O_{12}$	300-500 μm
$(YBiGd)_3(GaFe)_3O_{12}$	1-5 μm
Al	0.2-0.5 μm
SiO_2	0.2-0.5 μm





MOIF Images of the Remagnetization Process in an Exchange-Biased NiO/NiFe AF/FM Bilayer



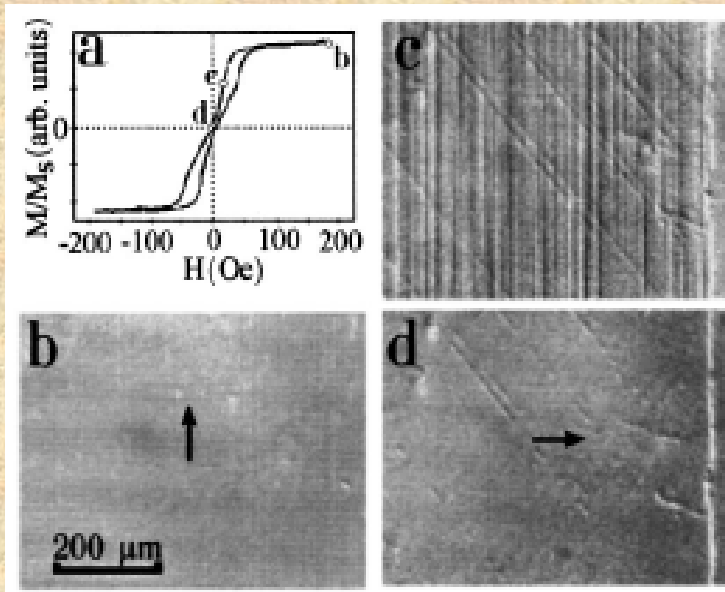
Nikitenko, Gornakov, Dedukh, Yu, Kabanov, Khapikov, Shapiro, Shull, Chaiken, Michel, PRB 57, R8111 (1998).

When layers become nanometer-thick, interface interactions become predominant.

- **In Antiferromagnetic/Ferromagnetic (AF/FM) bilayers:**
Domain nucleation is controlled by Magnetostatic Energy minimization during the application of a negative field.
But, Exchange Energy minimization controls the nucleation during field reduction!!!
- **In Normal Ferromagnets, domain nucleation occurs in the same place during forward and reverse cycles.**



Remagnetization with H Oriented Perpendicular to Exchange Bias In Epitaxial NiO/NiFe AF/FM Bilayer



Now, no wall Motion is observed while MOIF contrast appears and disappears as H is reduced and Reversed.

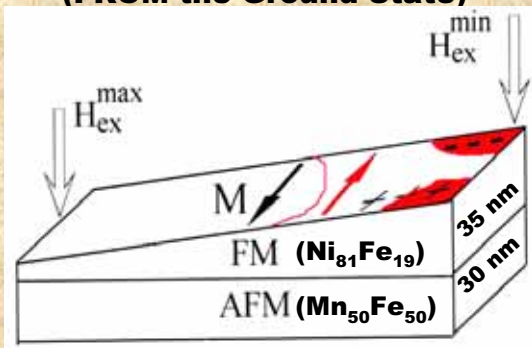
This indicates M reversal occurs by spin rotation and not by domain nucleation & growth.

[V. Nikitenko, V. Gornakov, L. Dedukh, Yu Kabanov, A. Khapikov, A. Shapiro, R. Shull, A. Chaiken, E. Michel, Phys. Rev. B 57, No. 14, R8111 (1998).]

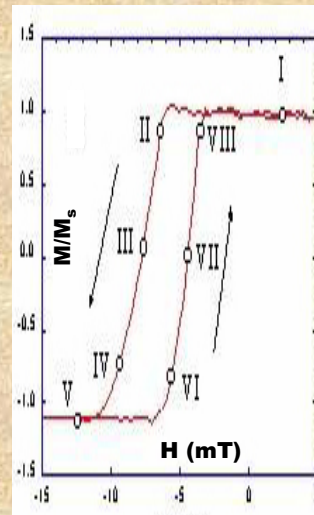
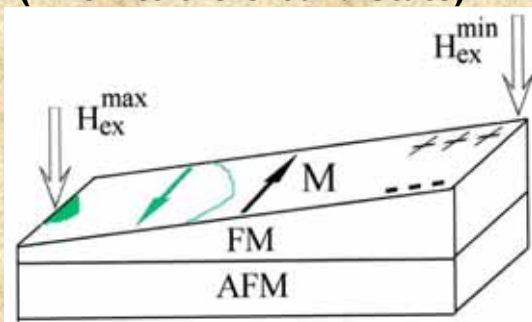


Asymmetry in Domain Nucleation in AF/FM Bilayer

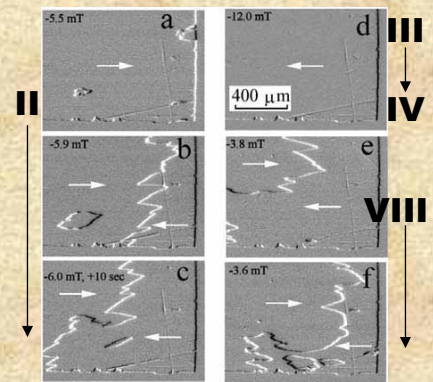
1st Reversal of M (FROM the Ground State)



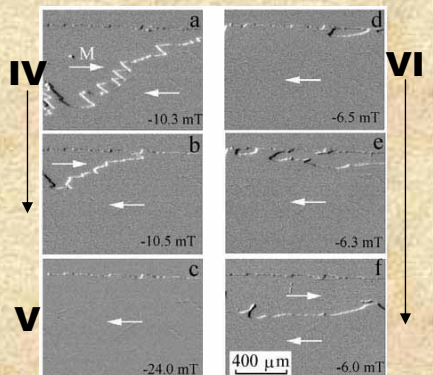
2nd Reversal of M (BACK to the Ground State)



Thick End



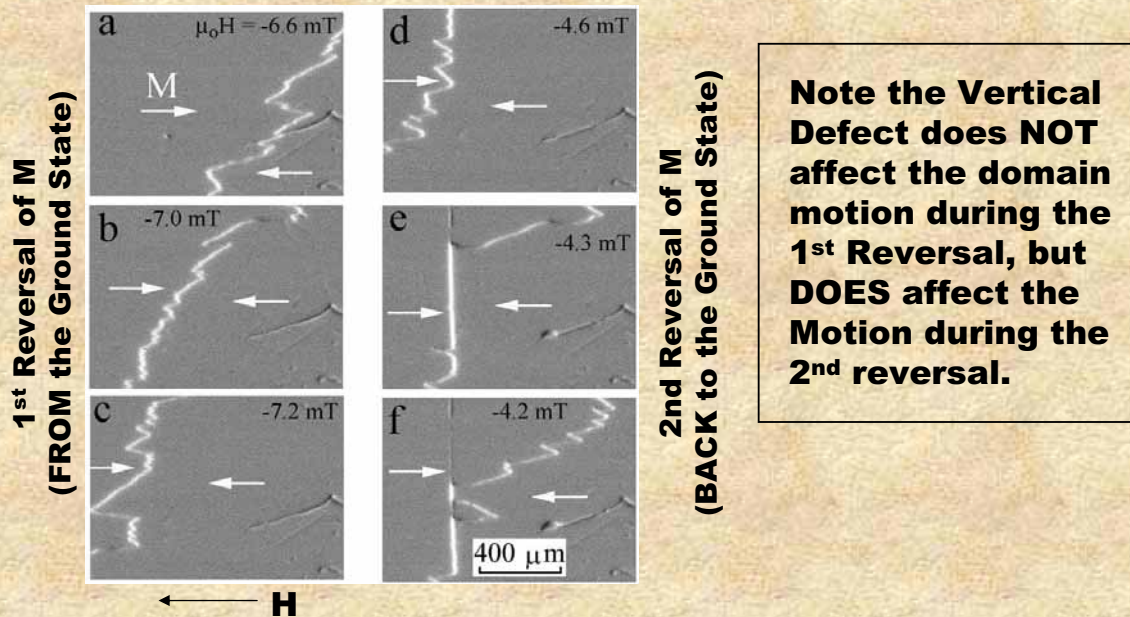
Thin End



[V. Nikitenko, et. al., Phys. Rev. Lett. 84, 765 (2000).]



Asymmetry in Domain Dynamics in AF/FM Bilayer



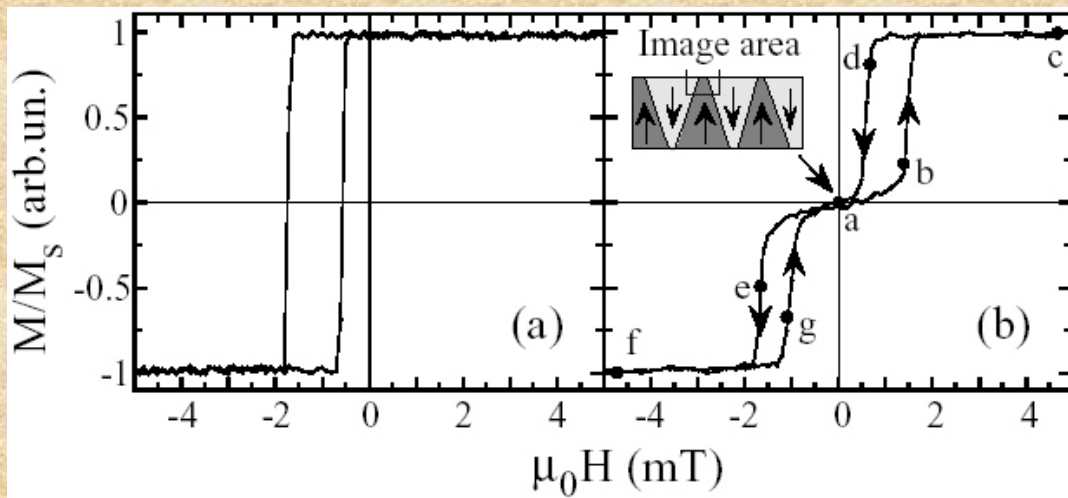
[V. Nikitenko, V. Gornakov, A. Shapiro, R. Shull, K. Liu, S. Zhou, C. Chien, Phys. Rev. Lett. **84**, 765 (2000).]



Domain Dynamics in FeMn/NiFe AF/FM Bilayer (AC Demagnetized at $T > T_{\text{Neel}}$ of AF)

Field Cooled (Exchange Biased)

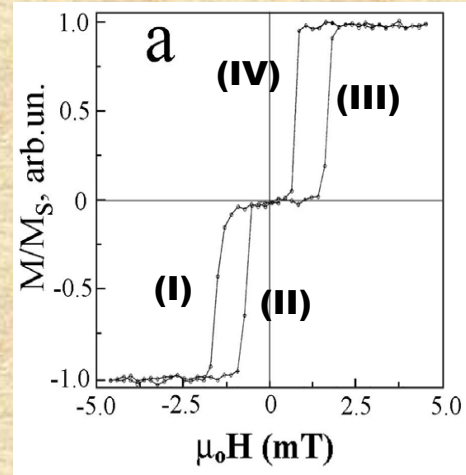
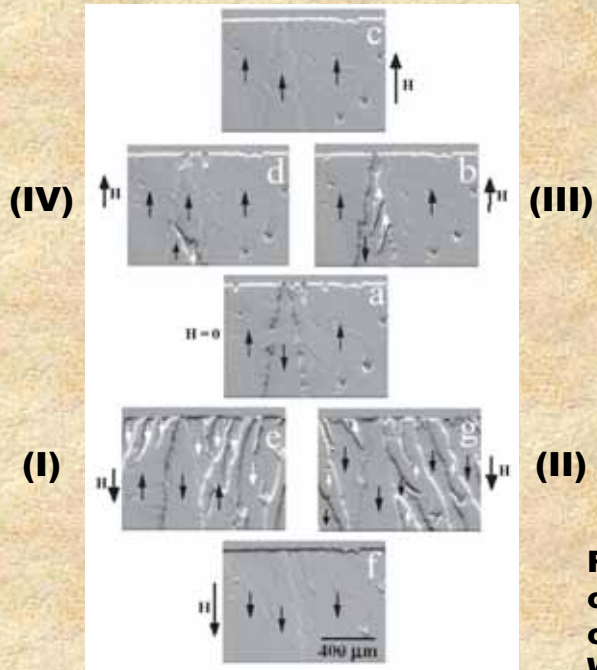
AC-Demagnetized



C. Chien, V. Gornakov, V. Nikitenko, A. Shapiro, R. Shull, IEEE Trans. Magnetics **38**, No. 5, 2736 (2002).]

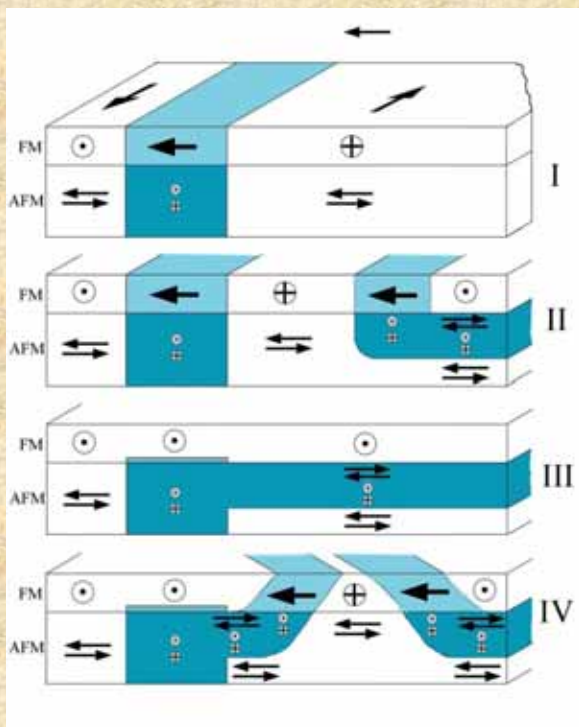


Domain Motion in AC Demagnetized FeMn/NiFe AF/FM Bilayer



Residual Image at top and bottom of original domain structure show original AF domains have not moved While the FM domains changed.

[Chien, Gornakov, Nikitenko, Shapiro, Shull, IEEE Trans. Magnetics 38, No. 5, 2736 (20002).]



Domain motion in AC-Demagnetized AF/FM Bilayer can be explained By the formation of an Exchange spring parallel To the AF/FM interface, Pinned at one end by the AF and at the other end by the FM

EXAMPLE:

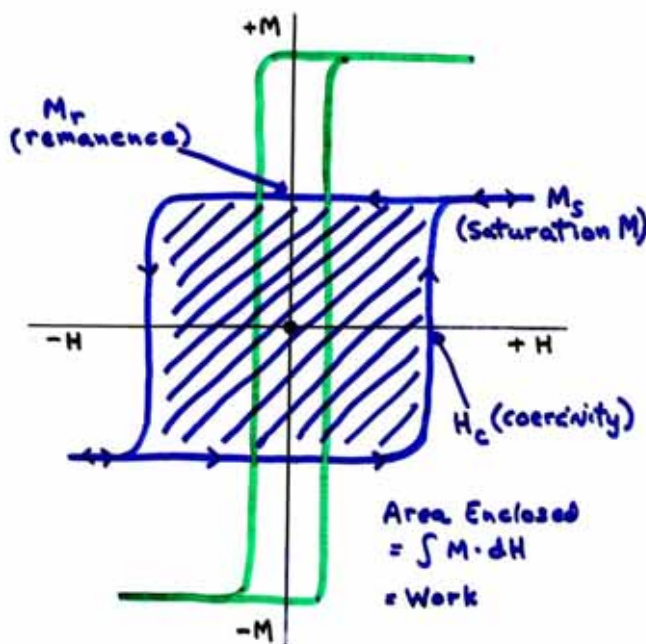
CHANGE IN DOMAIN DYNAMICS

IN NANOCOMPOSITE SYSTEMS

- IN AN IMPROVED PERMANENT MAGNET

Magnetic Materials Group

Hard/Soft Ferromagnetics



Composites of nm thick Hard & Soft Ferromagnets are thought to be the way to the future “Hardest” Ferromagnets.

This is because the magnetic Exchange interaction at the interface causes the Magnetization to change by the more difficult process of the coherent rotation of all the spins at one time, rather than by the nucleation & growth of domains. This results in a larger coercivity.

Substitution of Soft FMs Increase the saturation M, resulting in an increase in hysteresis loop area.

NIST

National Institute of Standards and Technology



HARD MAGNETIC MATERIALS

"Magnequench" Magnets

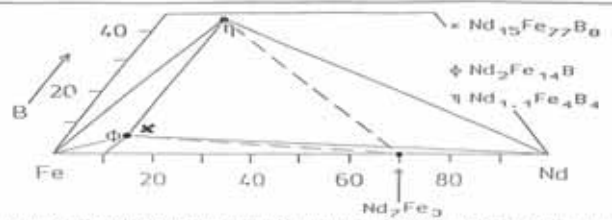


Figure 7. A comparison of the phase relations in the equilibrium phase diagram (solid line) and in the metastable phase diagram (dashed line).

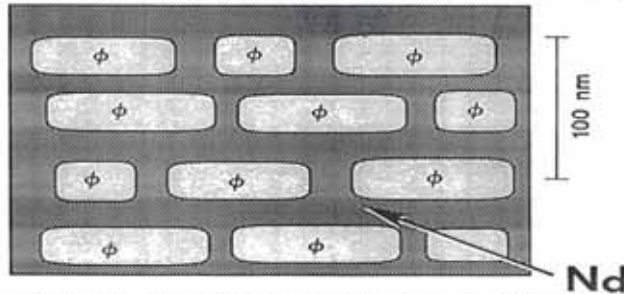


Figure 8. The ideal microstructure of a sintered magnet. The hard magnetic grains (ϕ) are decoupled by neodymium-rich nonmagnetic grain boundary phase.

A. Hutten, JOM (March, 1992) p. 11.

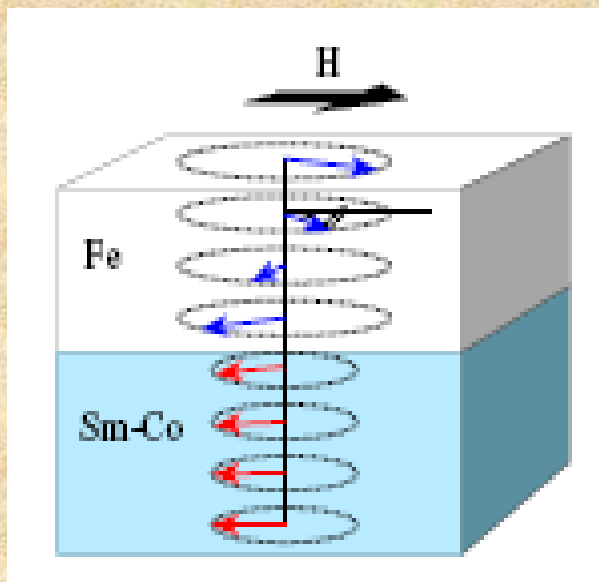
The make the "Hardest" Ferromagnetic materials (i.e., for the strongest permanent magnets), advantage is taken of the Interface effects.

The best Nd-Fe-B magnets are intentionally made off-stoichiometry in order to make them multiple phase so there are many interfaces.

The "Hard" phase is also made nanometer in size in order to increase the interface area.



Origin of High Coercivity in Hard/Soft Ferromagnetic Bilayer



Bottom Layer of the Soft Ferromagnet (Fe) is pinned by the top layer of the Hard Ferromagnet (SmCo).

Each successive layer in the Soft FM is bound to the layer below it causing its magnetic moment to be closely aligned to it. The further away each Soft FM layer is from the AF interface, the easier it is to align with the external field, thereby creating a "spin spiral". This keeps domain walls perpendicular to the interface from forming.

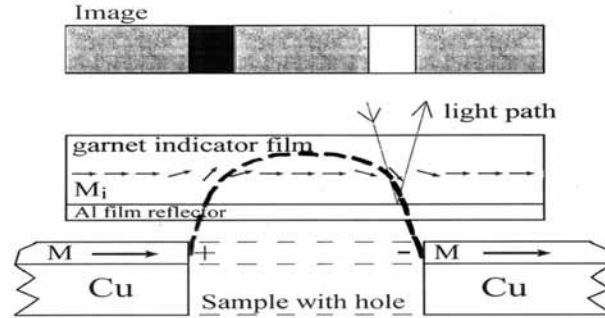
[E. Kneller & R. Hawig, IEEE Trans. Mag. 27, 3588 (1991).]



**Domain Imaging
Of a SmCo/Fe
Hard/Soft FM
Bilayer**

Since No MOIF image contrast was observed on the top of the soft FM (Fe) in a SmCo/Fe Bilayer During field reversal, a Trick was employed. A small hole was drilled through the bilayer, and the magnetization in the area was determined by the magnetic poles of opposite sign which formed on the opposite inside edges of the hole.

Schematic Illustrating the MOIF Technique for Investigation of Stray Magnetic Fields Around a Hole in a Multilayer Sample.

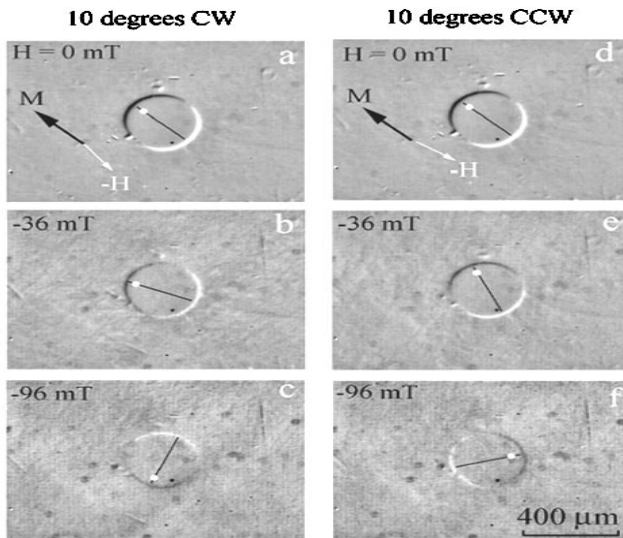


Magneto-Optical Image of Stray Fields Around a Hole in a 1 nm Multilayer Sample with Opposite Magnetization Directions.



Proof of Rotation Reversal Process in SmCo/Fe Bilayer

Remagnetization During H Reversal
(H aligned off Easy Magnetization axis)



Fe/SmCo Exchange Spring

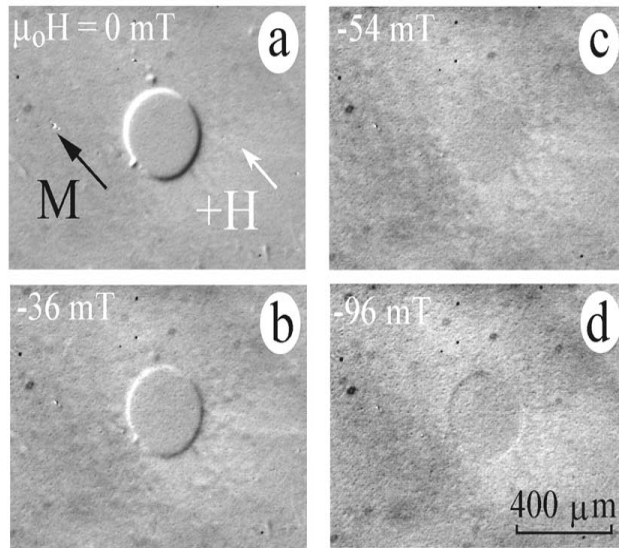
R.D. Shull, A.J. Shapiro, V.S. Gornakov, V.I. Nikitenko, J.S. Jiang, H. Kaper, G. Leaf, S.D. Bader, IEEE Trans. Magn. 37, 2576 (2001).

Application of a reversed field is shown by the rotation of the MOIF image contrast at the hole edges to be accompanied by a rotation of M, when H is aligned just slightly off the easy axis of Magnetization of the Fe.

MOIF images with no hole present showed no contrast, indicating no domain walls perpendicular to the surface as would be expected for a normal FM.

New Feature in the Reversal Process in SmCo/Fe Bilayer

H Aligned Along Easy Magnetization Direction



When H is aligned along the easy axis of magnetization of the Fe, reversal of H does not result in a rotation in the contrast at the hole edge, but it is accompanied by an overall reduction in image contrast.

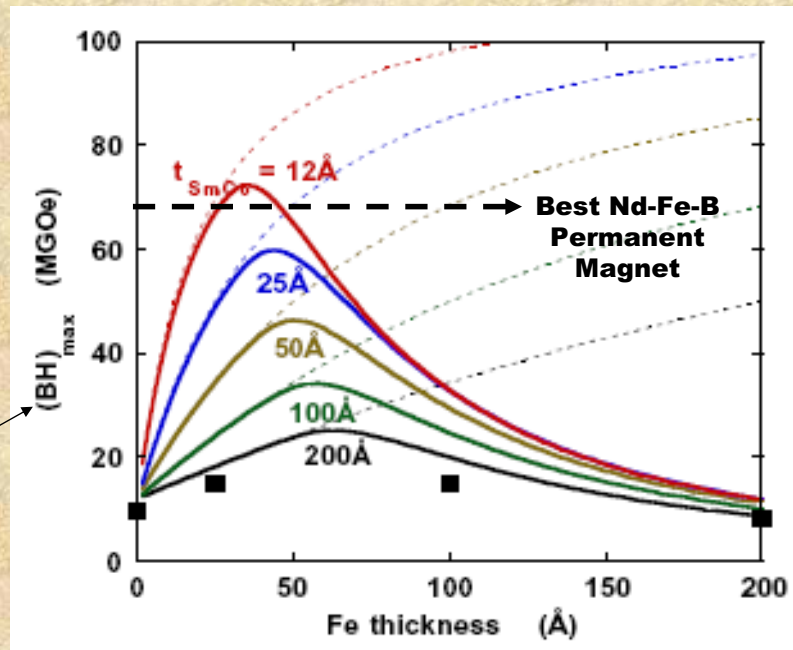
This effect is caused by a distribution in directions of the easy axes of magnetization in the small grains of the material: some rotating clockwise & some rotating CCW in response to H.

Fe/SmCo Exchange Spring

R.D. Shull, A.J. Shapiro, V.S. Gornakov, V.I. Nikitenko, J.S. Jiang, H. Kaper, G. Leaf, S.D. Bader, IEEE Trans. Magn. 37, 2576 (2001).

Improved Permanent Magnet By Multilayers of nm-thick SmCo & Fe

Hysteresis Loop Area



[J. Jiang, E. Fullerton, C. Sowers, I. Inomata, S. Bader, A. Shapiro, R. Shull, V. Gornakov, V. Nikitenko, IEEE Trans. Magnetics 35, 3229 (1999).]

Summary

- **The usefulness of a material for a particular application depends on how easily or hard it is to change its magnetization.**
- **Observation of Domain patterns is critical to understanding how a material changes its magnetization.**
- **Increased surface/volume ratio of nanomagnets makes domain motion more susceptible to interaction effects with neighboring magnetic materials.**
- **AF/FM Exchange Biased films possess a novel asymmetry in their reversal behavior**
- **Nanocomposites provide a means for designing better Hard ferromagnets (i.e., permanent magnets)**

OUTLINE

- (I). **Magnetocaloric Effect (dT)**
Definition
- (II). **Basic dT and dS Equations**
- (III). **Dependence on Magnetic State**
In Paramagnets
In Ferromagnets
In Magnetic Nanocomposites
- (IV). **Measurement Methods**
Direct Method
Indirect Method
- (V). **dT and dS Data**
11%Fe+Silica Gel Nanocomposite
Garnet Nanocomposites
- (VI). **Summary**

NANOMAGNETISM (III)

MAGNETIC REFRIGERATION

Robert D. Shull

(Group Leader:
Magnetic Materials Group)

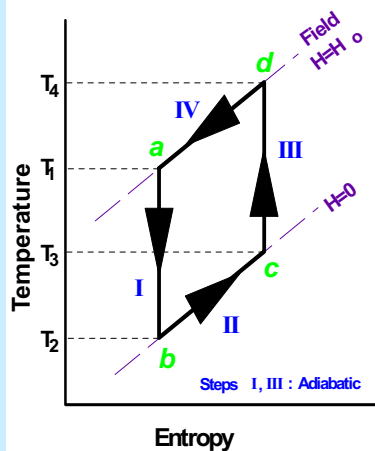
National Institute
of Standards and Technology
Gaithersburg, Maryland
USA

**Member: OSTP Nanoscale Science, Engineering,
and Technology Subcommittee (NSET)**

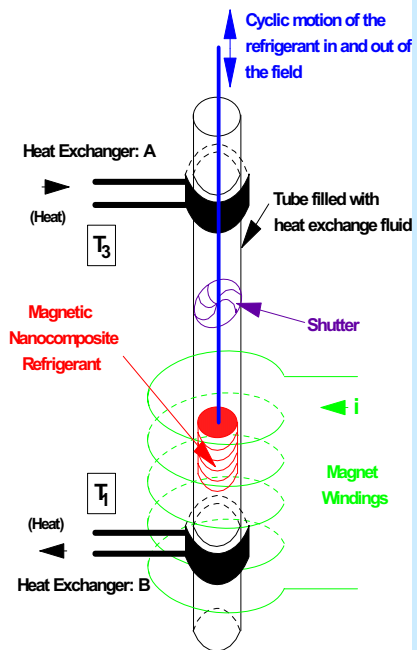
**V. President: The Minerals, Metals, &
Materials Society (TMS) of AIME**

MAGNETIC REFRIGERATION

Refrigeration Cycle

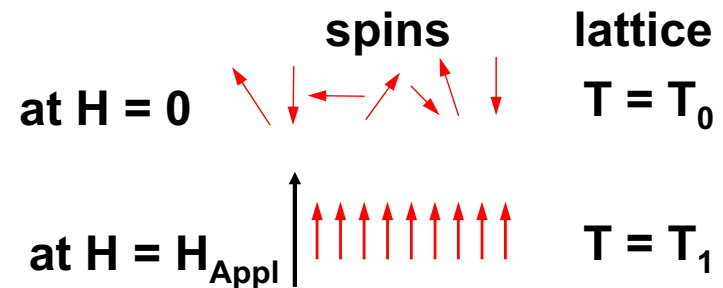


Refrigerator



MAGNETOCALORIC EFFECT

SYSTEM = SPIN + LATTICE



Total entropy change of the (Spin + Lattice) system upon application of a magnetic field, H_{Appl} , (reversibly) is ZERO.

Decrease in spin entropy causes an increase in lattice entropy, $C_H dT/T$.

Magnetocaloric effect = $dT = (T_1 - T_0)$.

Basic dS and dT Equations:

$$(1) \quad dU = \delta Q - \delta W \quad [\text{System} = \text{Spin} + \text{Lattice}]$$

$$(2) \quad = TdS - PdV + \sum_i \mu_i dN_i + \mu_0 V_M H \cdot dM$$

$$(3) \quad = TdS + \mu_0 V_M H \cdot dM$$

if Volume and Material
are Not changed

Creating the Maxwell relation
from the Exact differential of (3):

$$(4) \quad \left(\frac{\partial S}{\partial H} \right)_T = \mu_0 V_M \left(\frac{\partial M}{\partial T} \right)_H$$

To obtain dT , express $dS(H, T)$:

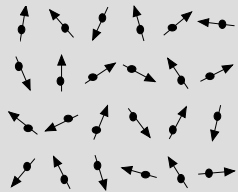
$$(5) \quad dS = \left(\frac{\partial S}{\partial T} \right)_H dT + \left(\frac{\partial S}{\partial H} \right)_T dH$$

For a Reversible change in T :

$$(6) \quad \left(\frac{\partial S}{\partial T} \right)_H = \frac{C_H}{T}$$

WHY MAGNETIC REFRIGERATORS ?????

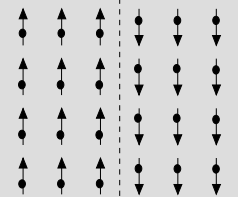
- **Large Entropy Change in Ordering**
(40-200 times that of a gas)
- **Based on a REVERSIBLE Process**
(Carnot efficiencies conceivable)
- **Refrigerant and Heat Transfer Media**
are **DIFFERENT**
(No chlorofluorocarbons)
- **No Compressor & Few Moving Parts**
(Low vibration, High durability)



Paramagnetic Material:

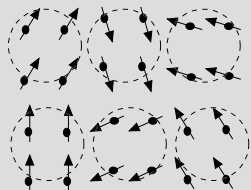
Assembly of elemental moments, each of magnitude μ acting independently

Domain 1 | Domain 2



Ferromagnetic Material:

Assembly of magnetic domains (each comprised of many elemental moments of magnitude μ) aligned in the field direction in concert with the other domains



Superparamagnetic Material:

Assembly of magnetic clusters (each comprised of many ferromagnetically-aligned elemental moments of magnitude μ) acting independently.

Substituting (4) and (6) into equation (5):

$$(7) \quad dS = \left(\frac{C_H}{T}\right) dT + \mu_0 V_M \left(\frac{\partial M}{\partial T}\right)_H dH$$

$$= 0 \quad \text{for an adiabatic process}$$

$$(8) \quad \therefore \boxed{dT = -\left(\frac{T}{C_H}\right) \mu_0 V_M \left(\frac{\partial M}{\partial T}\right)_H dH}$$

for a given ΔH :

$$\text{Total } \Delta T = \int dT = \int_0^H -\left(\frac{T}{C_H}\right) \mu_0 V_M \left(\frac{\partial M}{\partial T}\right)_H dH$$

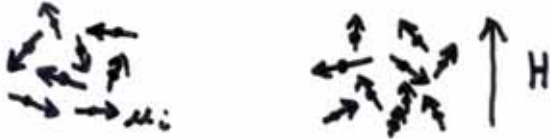
and

$$\boxed{\text{Total } \Delta S = \int_0^H \mu_0 V_M \left(\frac{\partial M}{\partial T}\right)_H dH}$$

in general: $\left(\frac{\partial M}{\partial T}\right)_H = f(H, T)$

For an Ideal Paramagnet:

(An assembly of N non-interacting spins of magnetic moment μ)



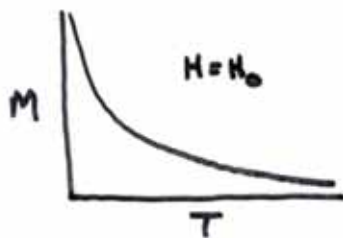
$$M = \sum \mu_i$$

$$\frac{M}{M_0} = \coth(a) - \frac{1}{a}$$

where $a = \frac{\mu H}{kT}$
 $M_0 = N\mu$

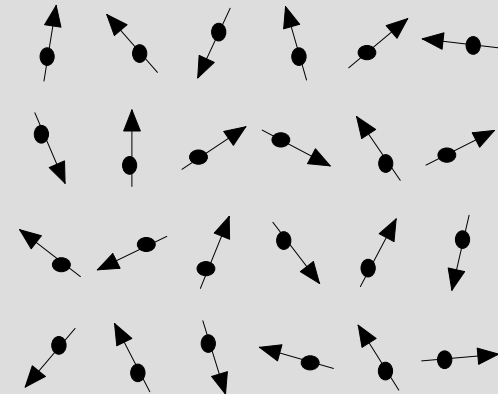
Low Field Limit:

$$M = \frac{N\mu^2 H}{3kT} \quad \text{Curie Law}$$



$$\left[\begin{aligned} \Delta S &= Nk_B \left[1 - a \coth(a) \right. \\ &\quad \left. + \ln \left(\frac{\sinh(a)}{a} \right) \right] \\ &= \frac{N\mu^2 H^2}{6k_B T^2} \end{aligned} \right]$$

VERY SMALL PARTICLE LIMIT

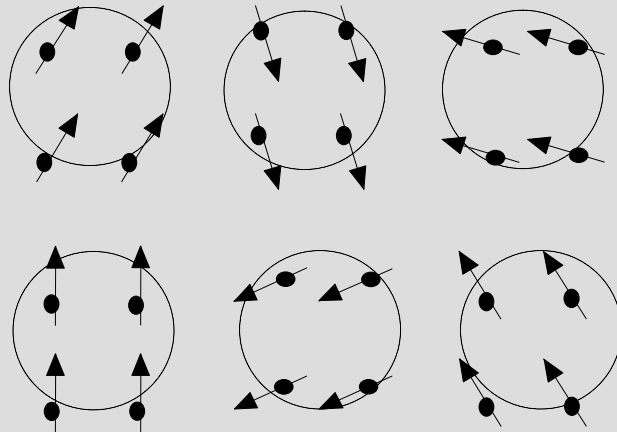


Assembly of elemental moments, each of magnitude μ , acting independently

Paramagnetic Material:



SMALL PARTICLE BEHAVIOR



**Assembly of magnetic clusters
(each comprised of many
ferromagnetically-aligned elemental
moments of magnitude μ) acting
independently.**

Superparamagnetic Material:

["The Magnetocaloric Effect in Nanocomposites", R. Shull, L. Swartzendruber, L. Bennett, Proc. of the 6th Int'l. Cryocoolers Conf., eds. G. Green, M. Knox, David Taylor Res. Cntr. Publ. #DTRC-91/002, Annapolis, MD (1991) 231.]



$$M = N\mu^2 H / 3k_B T$$

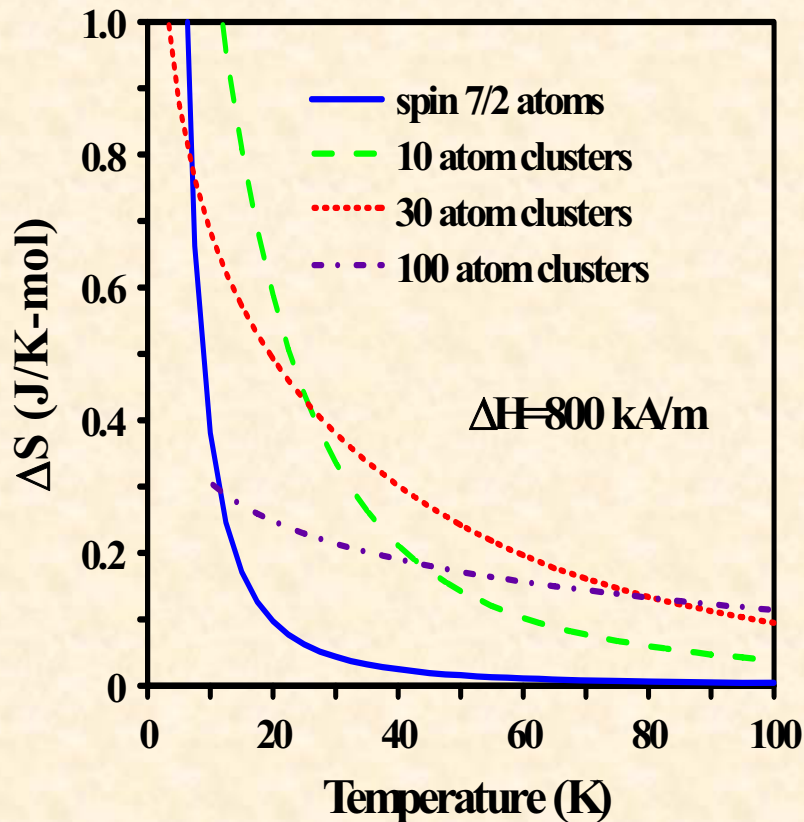
$$\partial M / \partial T = -N\mu^2 H / 3k_B T^2$$

$$\partial T = -(T/C_H)\mu_0 V_M (\partial M / \partial T)_H \partial H$$

$$\partial T = (1/C_H)\mu_0 V_M (N\mu^2 H / 3k_B T) \partial H$$

The temperature change for a **paramagnet**
Is inversely proportional to the temperature
And proportional to the field change.

Entropy Enhancement in Nanocomposites



Grouping the atoms together in clusters gives larger entropy changes than single atoms in the $\Delta H, T$ regimes accessible by refrigerators.

For a Nanocomposite

-possessing superparamagnetic behavior (without interaction):

"N" spins in "n" ferromagnetic regions

$$\mu_{\text{region}} = \left(\frac{N}{n}\right) \mu_{\text{spin}}$$

$$\frac{M}{N\mu} = \coth\left(\frac{\mu H}{kT}\right) - \frac{kT}{\mu H}$$

low field limit:

$$M = \frac{N\mu^2 H}{3kT} \Rightarrow \frac{n\left(\frac{N}{n}\right)^2 H}{3kT}$$

Magneto-caloric Effect: $dT = -\left(\frac{I}{C_H}\right) \mu_0 V n \left(\frac{\partial H}{\partial T}\right)_H dH$

$$dT_{\text{nano. (r.i)}} = \left(\frac{\mu_0 V n}{C_H}\right) n \left(\frac{N}{n}\right)^2 \frac{\mu_{\text{spin}}^2 H}{3k} \frac{1}{T} dH$$

compared to paramagnetism:

$$dT_{\text{para}} = \left(\frac{\mu_0 V n}{C_H}\right) N \frac{\mu_{\text{spin}}^2 H}{3k} \frac{1}{T} dH$$

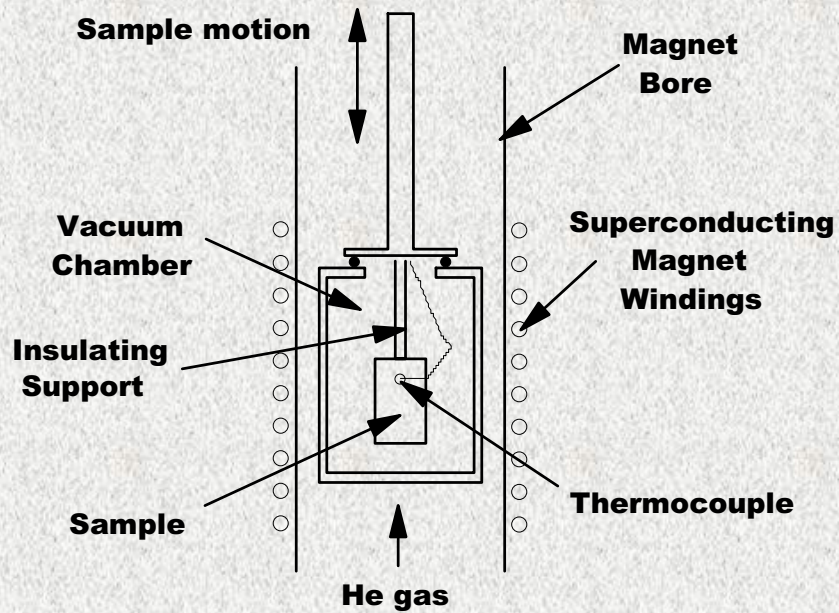
$$n\left(\frac{N}{n}\right)^2 = \frac{N^2}{n} \gg N$$

$$\therefore dT_{\text{nano. (r.i)}} \gg dT_{\text{para}}$$

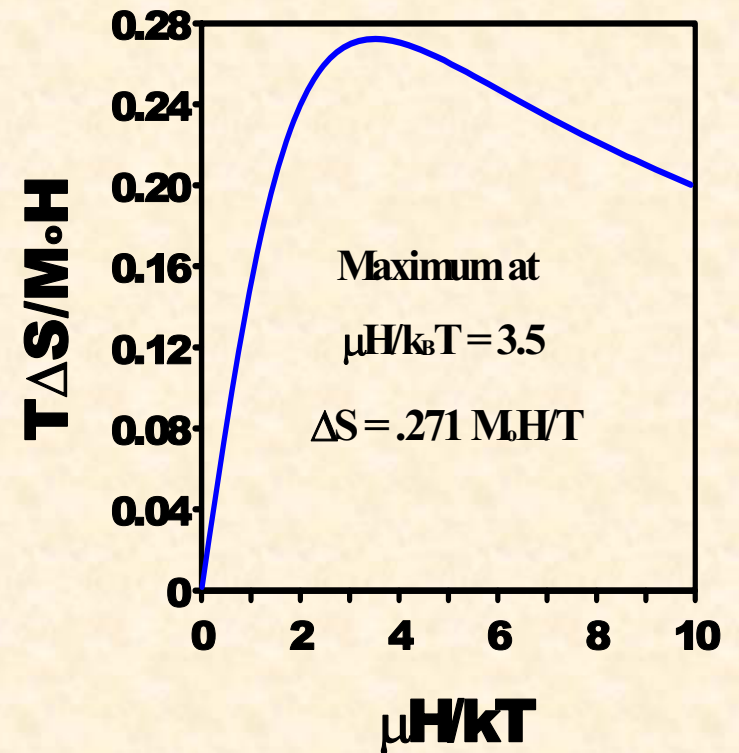


Measurement of the Magnetocaloric Effect (MCE)

CALORIMETER



"Universal" Entropy Change Curve

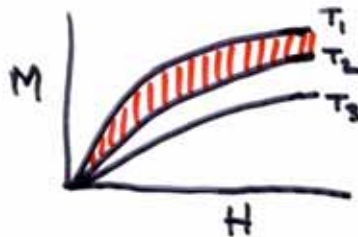


[R. McMichael, R. Shull, L. Swartzendruber, L. Bennett, R.E. Watson, J. Mag. & Magn. Mat. **111**, 29 (1992)]

Calculation of the MCE
from Magnetization Data

$$\left(\frac{\partial S}{\partial H}\right)_T = \left(\frac{\partial M}{\partial T}\right)_H$$

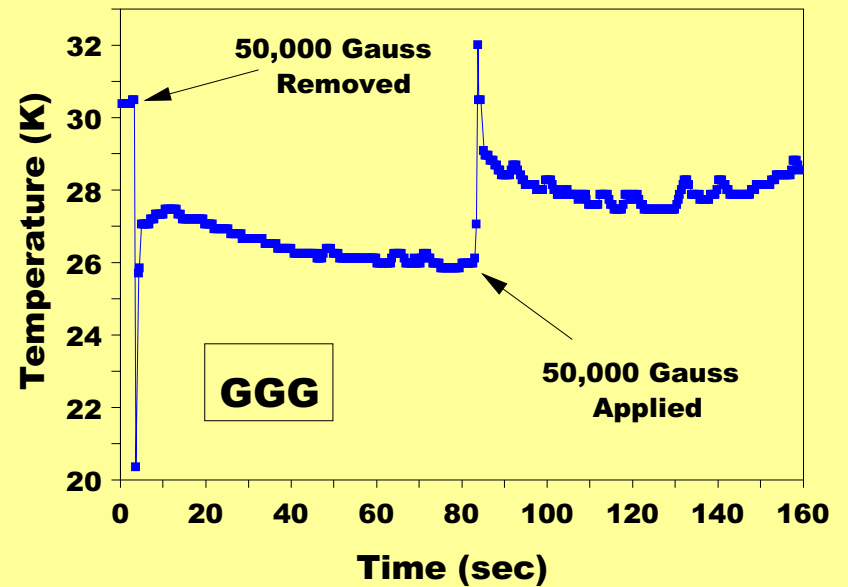
$$\Delta S = \int_0^H \left(\frac{\partial M}{\partial T}\right)_H dH$$



$$\Delta S_i = \frac{1}{\Delta T_i} \int_0^H [M(T_{i+1}, H) - M(T_i, H)] dH$$

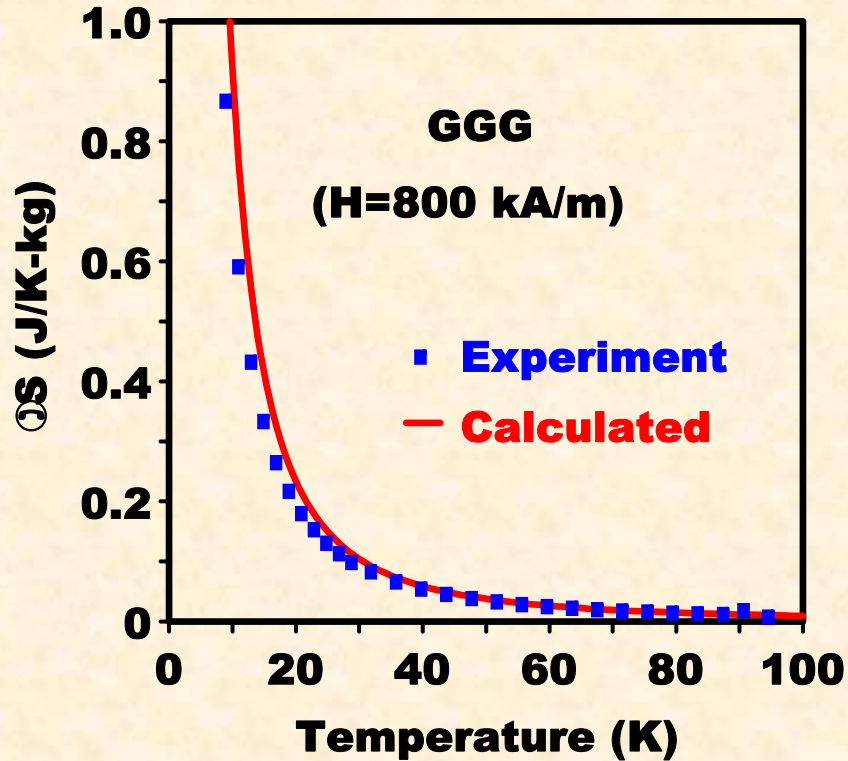
where $\Delta T_i = T_{i+1} - T_i$

**Magnetocaloric Effect
in
Gadolinium Gallium Garnet**



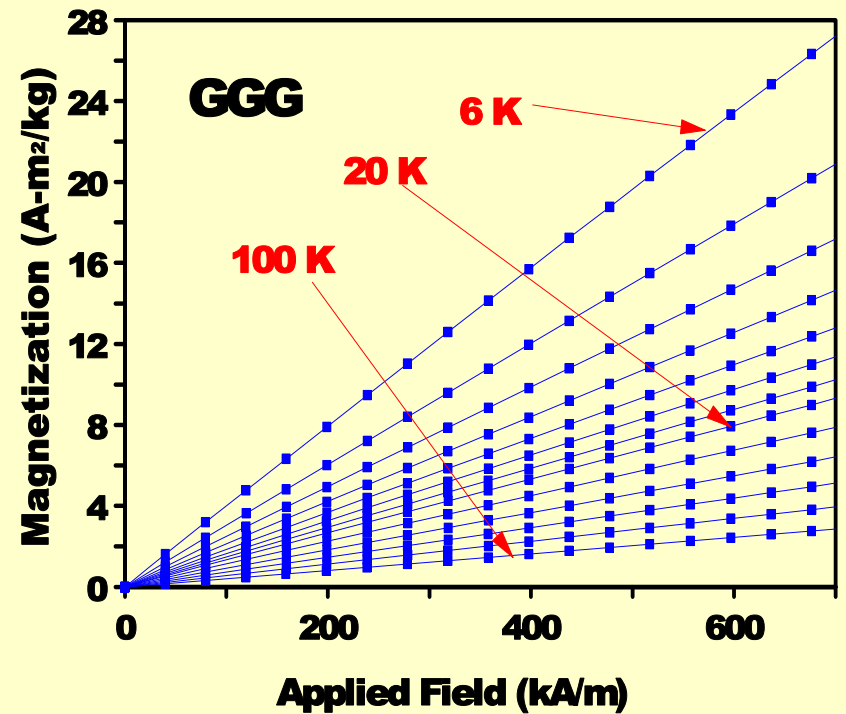
(This is the material with the largest magnetocaloric effect at low temperatures and is useful as a magnetic refrigerant up to 15 K)

Gd₃Ga₅O₁₂
Magnetocaloric Effect

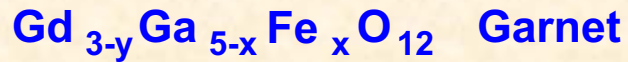


Calculation of the MCE values from magnetization data is a good way to determine MCE (& it is much faster).

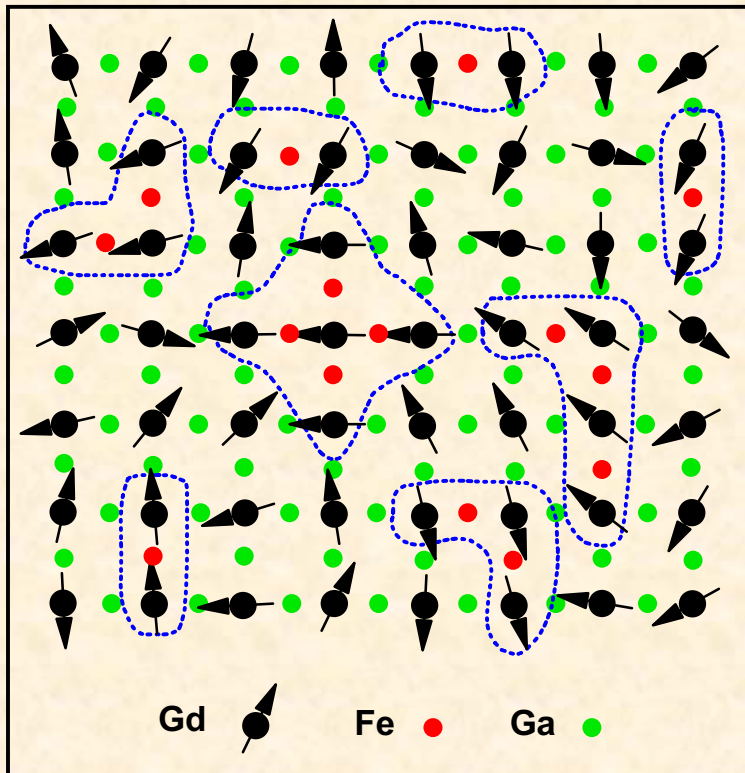
Gd₃Ga₅O₁₂
Magnetization Isotherms
(for Entropy Calculations)



Schematic Picture of

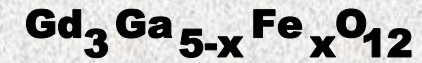


Magnetic Nanocomposites



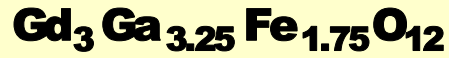
Fe spins create magnetic clusters (dashed areas)

Bulk

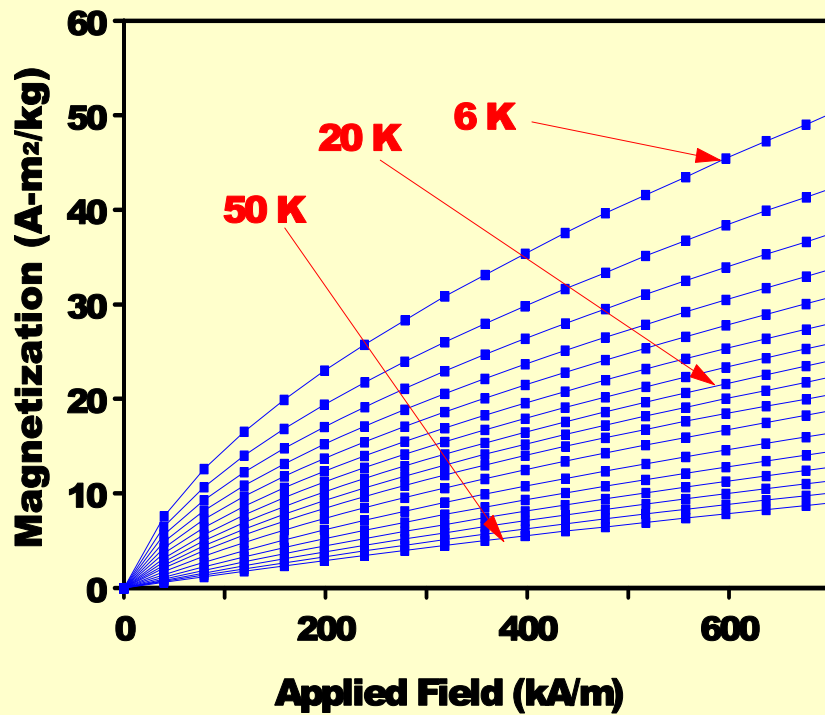


Nanocomposites

- Prepared nanocomposites by adding aqueous solutions of the mixed metal nitrates to excess tartaric acid (for complexing)
- Air dried (200-325 C)
- Formed Garnet Structure (1) Air (950 C)
- Samples characterized
 - X-ray diffraction
 - Mossbauer Effect
 - Ferromagnetic Resonance
 - Magnetic susceptibility



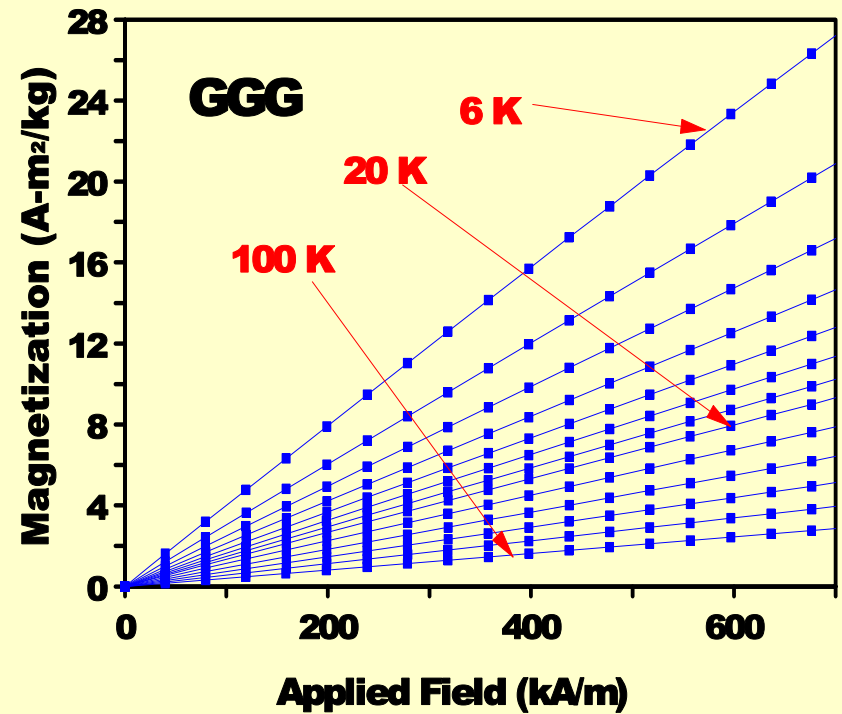
**Magnetization Isotherms
(for Entropy Calculations)**



Curved isotherms show superparamagnetic behavior & therefore the presence of magnetic clusters

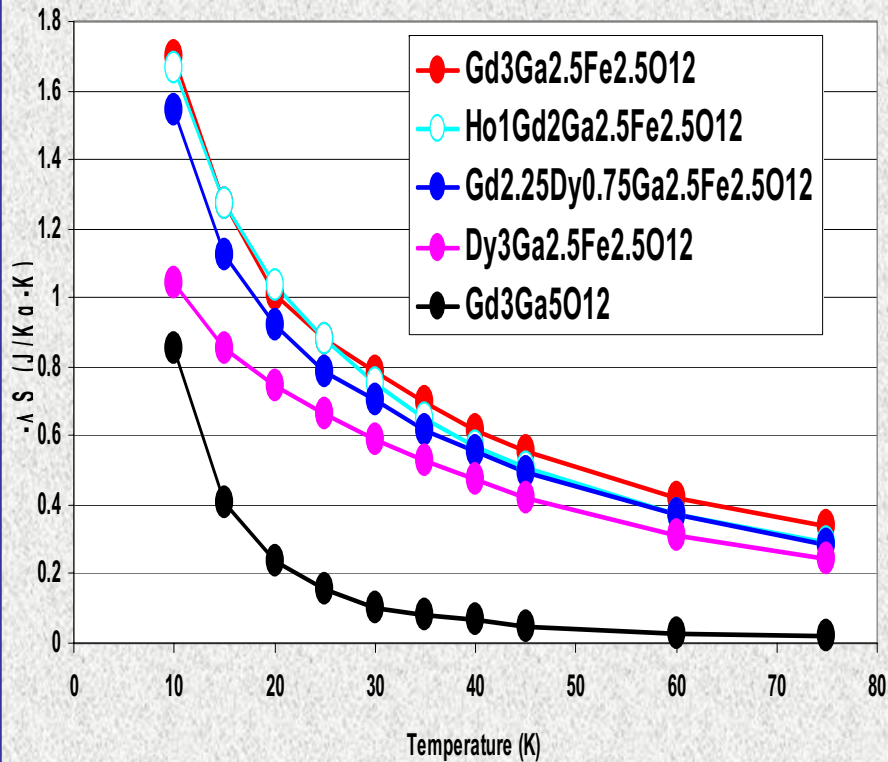


**Magnetization Isotherms
(for Entropy Calculations)**



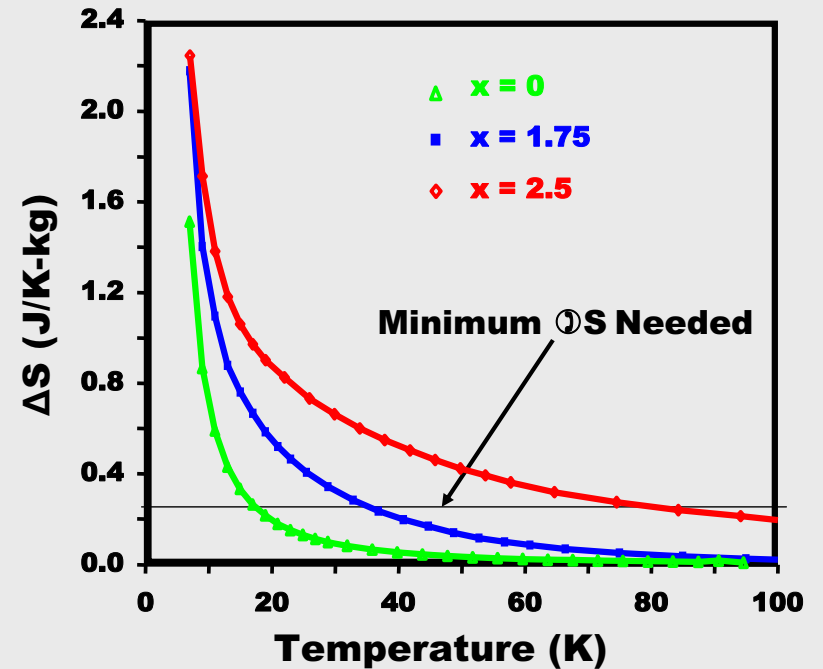
Straight line isotherms show paramagnetic behavior & therefore no interaction between magnetic spins

$-\Delta S$ vs T for GGI, HGGI, GDGI, DGI Garnet Nanocomposites and GGG Heat Treated for 15 h at 1200°C ($\Delta H=1T$)



[V. Provenzano, J. Li, T. King, E. Canavan, P. Shirron, M. DiPirro, and R.D. Shull, JMMM 266, 185 (2003)]

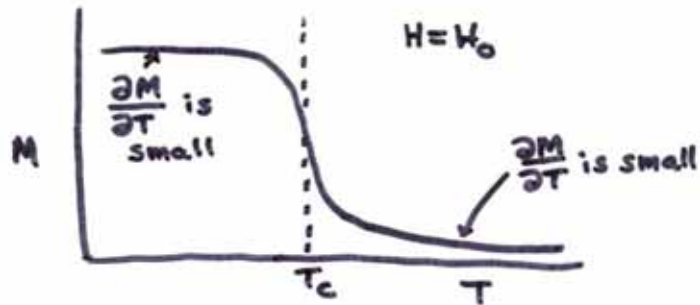
Magnetocaloric Effect Entropy Changes for $Gd_3Ga_{5-x}Fe_xO_{12}$ Nanocomposites ($\Delta H=800$ kA/m)



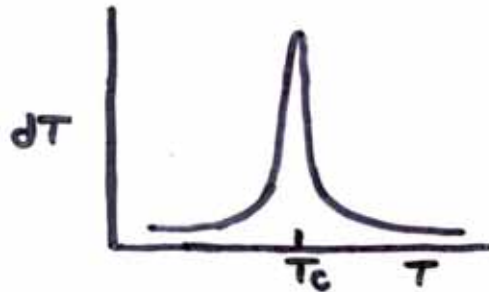
[R.D. McMichael, J.J. Ritter, and R.D. Shull, J. Appl. Phys. 73(10), 6946 (1993)]

Nanocomposites show one way to move the technology up in temperature at reduced fields

For a Ferromagnet:



$$dT = -\left(\frac{T}{CH}\right) \mu_0 V_M \left(\frac{\partial M}{\partial T}\right)_H dH$$

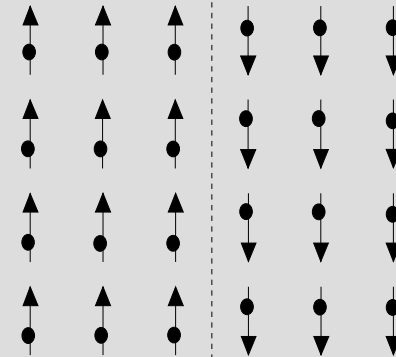


for $T < T_c$:

- H (1) orders spins within domains
- (2) eliminates domain walls

LARGE PARTICLE LIMIT

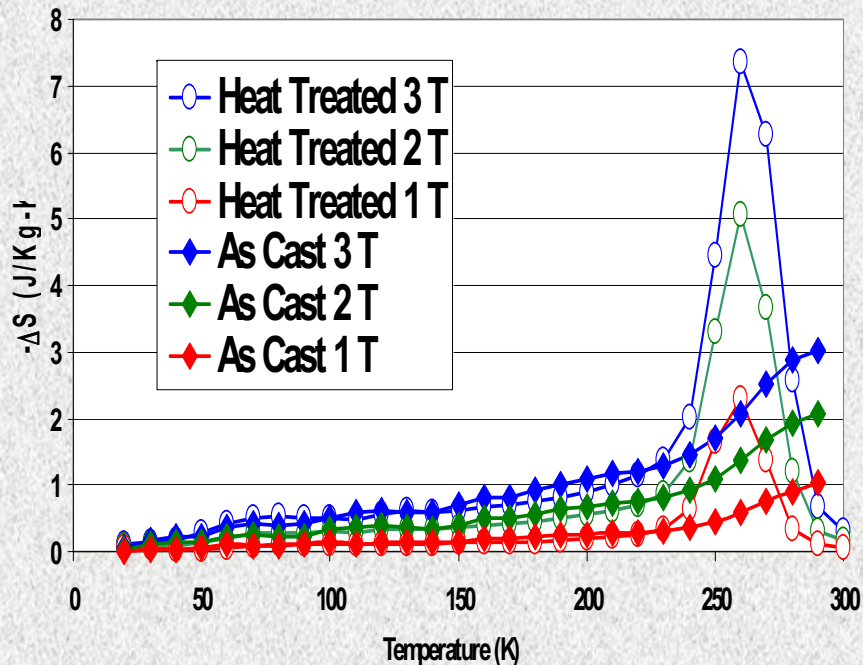
Domain 1 Domain 2



**Assembly of magnetic domains
(each comprised of many elemental
moments of magnitude μ) aligned
in the field direction in concert
with the other domains**

Ferromagnetic Material:

① ΔS vs T for $Gd_5Ge_2Si_2$: As-Cast and Heat Treated (1100°C, 1 h + 1400°C, .2 h)



[V. Provenzano, A.J. Shapiro, and R.D. Shull, Nature 429, 853 (2004)]

for $T > T_c$:

(N weakly interacting spins)

$$M = \frac{N \mu^2 H}{3k_B(T - T_c)}$$

$$\therefore \left(\frac{\partial M}{\partial T}\right)_H = -\frac{N \mu^2 H}{3k_B(T - T_c)^2}$$

$$\therefore dT_{ferromagnet} = \left(\frac{\mu_0 V_M}{C_H}\right) \frac{Ng^2 J(J+1) \mu_B^2}{3k_B} \frac{T}{(T - T_c)^2} H dH$$

$$\frac{T}{(T - T_c)^2} \gg \frac{1}{T}$$

$$\therefore dT_{ferro}(\text{above } T_c) \gg dT_{para}$$

$$\left(dT_{para} = \left(\frac{\mu_0 V_M}{C_H}\right) \frac{Ng^2 J(J+1) \mu_B^2}{3k_B} \frac{1}{T} H dH \right)$$

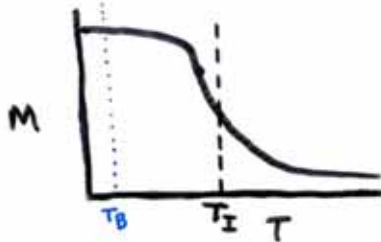
For a Nanocomposite :

-possessing superparamagnetic behavior with interaction :

n ferromagnetic regions weakly interacting with each other

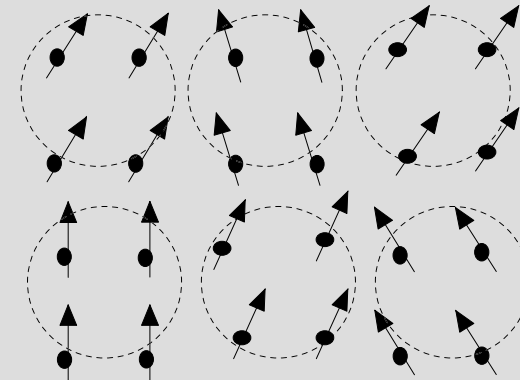
$$\mu_{\text{region}} = \left(\frac{N}{n}\right) \mu$$

$$M = \frac{n \left(\frac{N}{n} \mu\right)^2 H}{3k(T-T_I)}$$



$$\therefore \left(\frac{\partial M}{\partial T}\right)_H = - \frac{n \left(\frac{N}{n} \mu\right)^2 H}{k(T-T_I)^2}$$

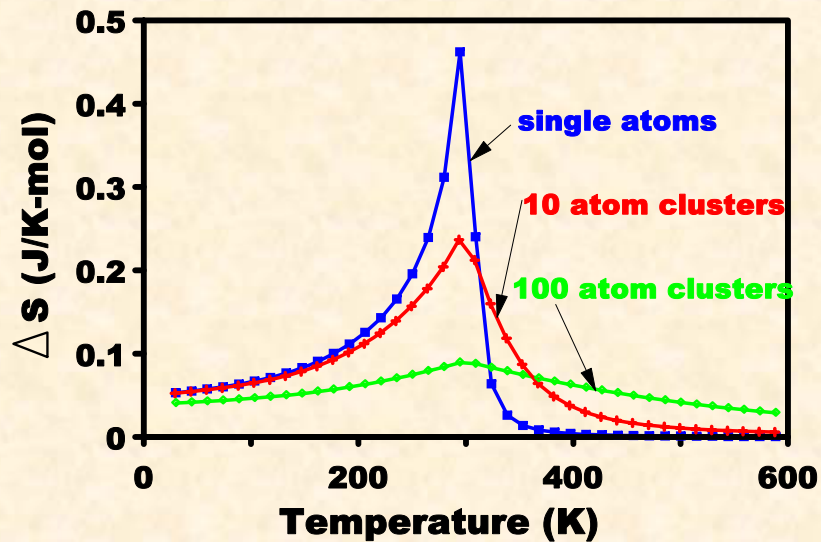
INTERACTING SMALL-PARTICLE BEHAVIOR



Assembly of magnetic clusters (each comprised of many ferromagnetically-aligned elemental moments of magnitude μ) acting in concert with other clusters.

Superferromagnetic Material:

Entropy Change for Interacting Clusters of Spin 7/2 Atoms ($H=1T$)



[R.D. Shull, IEEE Trans. on Magnetics 29, 2614 (1993)]

Interacting clusters of atoms possess smaller MCE values at the critical temperature, but larger MCE values at all higher temperatures.

$$\therefore dT_{\text{nano}} = \left(\frac{\mu_0 V_M}{C_H} \right) n \left(\frac{N}{n} \right)^2 \frac{\mu^2 H}{3k} \frac{I}{(T-T_I)^2} dH$$

$$n \left(\frac{N}{n} \right)^2 \gg N$$

$$\therefore \text{for } T_I \approx T_c$$

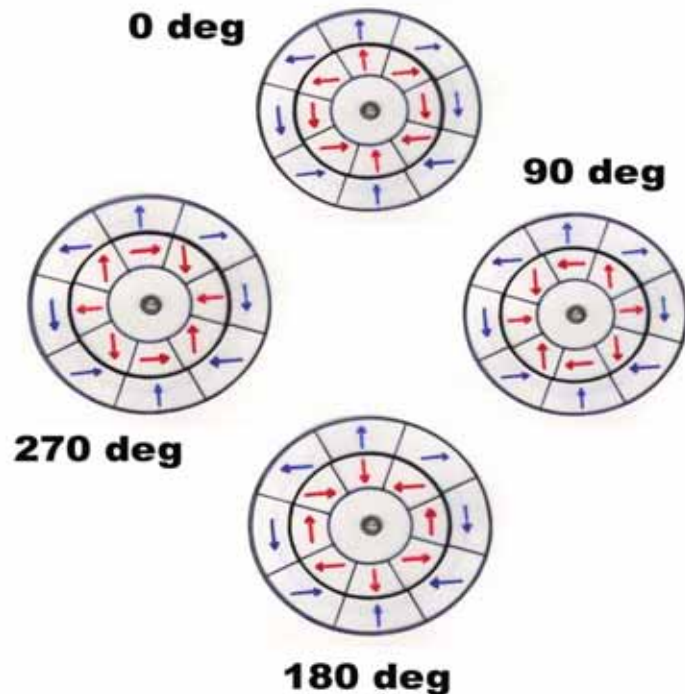
$$dT_{\text{nano}} \gg dT_{\text{ferro}} \gg dT_{\text{para}}$$

$$dT_{\text{para}} = \left(\frac{\mu_0 V_M}{C_H} \right) N \frac{\mu^2 H}{3k} \frac{1}{T} dH$$

$$dT_{\text{ferro}} = \left(\frac{\mu_0 V_M}{C_H} \right) N \frac{\mu^2 H}{3k} \frac{I}{(T-T_c)^2} dH$$



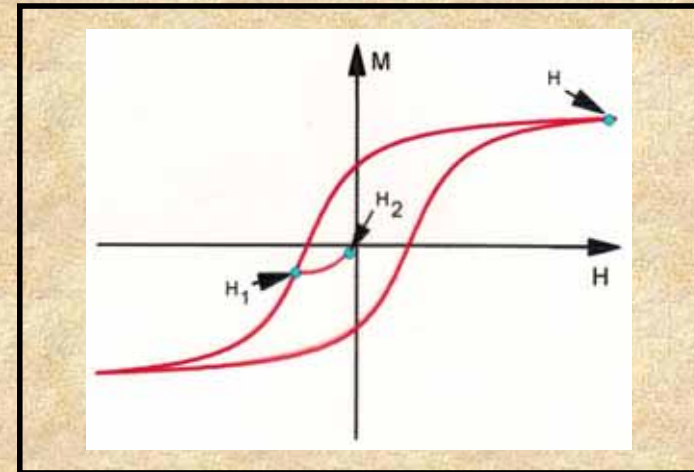
MAGIC RING (VARIABLE PERMANENT MAGNET)



This is a good way to vary the magnetic field from a permanent magnet in a compact volume. Perhaps for a magnetic refrigerator???



WHAT ABOUT MCE CALCULATION FOR A FERROMAGNET???



M is NOT a Single Valued Function!

M is No Longer a Good Order Parameter !!!

Hysteresis Loss NEEDS to be subtracted from the MCE!!!

[V. Provenzano, A.J. Shapiro, and R.D. Shull, Nature 429, 853 (2004); V. Provenzano, B. Baumgold, R.D. Shull, A.J. Shapiro, K. Koyama, K. Watanabe, N.K. Singh, K.G. Suresh, A.K. Nigam, and S.K. Malik, J. Appl. Phys. 99, 08K906 (2006)]

Conclusions

- Magnetocaloric effects are **dependent** on particle size and distribution
- **Enhanced** Magnetocaloric Effects can be obtained in **small particle** materials (e.g., in magnetic nanocomposites)
- Their maximum enhancements are at **LOW** fields and/or **HIGH** temperatures
- **Gd₃ Ga_{5-x} Fe_xO₁₂** nanocomposites may be usable now as a magnetic refrigerant at low temperatures
- **RSP: Nd_{13.75} (Fe_{1-x} Al_x)_{80.25} B₆** nanocomposites:
 - show predicted systematics
 - are potentially usable near 300 K
- For ferromagnets, hysteresis loops should Always be shown if magnetic data is used to calculate the MCE