On the reliable measurement of specific absorption rates and intrinsic loss parameters in magnetic hyperthermia materials

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Abstract
In the clinical application of magnetic hyperthermia, the heat generated by magnetic nanoparticles in an alternating magnetic field is used as a cancer treatment. The heating ability of the particles is quantified by the specific absorption rate (SAR), an extrinsic parameter based on the clinical response characteristic of power delivered per unit mass, and by the intrinsic loss parameter (ILP), an intrinsic parameter based on the heating capacity of the material. Even though both the SAR and ILP are widely used as comparative design parameters, they are almost always measured in non-adiabatic systems that make accurate measurements difficult. We present here the results of a systematic review of measurement methods for both SAR and ILP, leading to recommendations for a standardised, simple and reliable method for measurements using non-adiabatic systems. In a representative survey of 50 retrieved datasets taken from published papers, the derived SAR or ILP was found to be more than 5% overestimated in 24% of cases and more than 5% underestimated in 52% of cases.

Keywords: magnetic hyperthermia, specific absorption rate, intrinsic loss parameter

(Some figures may appear in colour only in the online journal)
hyperthermia technology should be safe and well tolerated by patients, while also being an effective cancer treatment. In particular, the AMF itself must be safe and well tolerated. In clinical terms, this means that the magnetic field strength and/or frequency must be low enough to avoid the induction of tissue-borne eddy currents strong enough to generate harmful levels of non-specific heating and/or unacceptably high levels of peripheral nerve stimulation [10, 11]. Thus, if a particle can be found which has the same heating characteristics as another, but with a lower requirement regarding field strength or frequency, it is clinically preferred.

Moreover, it may be difficult to deliver therapeutically sufficient concentrations of MNPs to a tumour site, especially in cases where direct injection of the particles into the tumour is not an option. In such cases, it is important that the MNPs display the best possible heating properties and generate as much heat as possible for a given AMF strength and frequency.

For these reasons, it is important to be able to make a physically robust and reliable assessment of the magnetic heating properties of any given MNP in its clinically useful state, i.e. in the form of a fluid suspension, as would be used for interstitial injection. A critical factor here and one that is not always taken into account, is that most measurements are performed under non-adiabatic experimental conditions. It is also important to be able to directly compare the results reported by different research teams, even when they are using substantially different measurement apparatus and experimental conditions.

Unfortunately, it is clear from inspection of the current scientific literature that neither of these conditions is being met and there is a chronic need for a more standardised approach. We hope here to contribute to meeting this need by reporting on a detailed assessment of the best available means for measuring the magnetic heating properties of MNPs and the preferred ways of reporting and comparing these.

2. Parameters for reporting magnetic heating properties

The most commonly quoted measure for magnetic heating ability of MNPs is the specific absorption rate (SAR), which is defined as the heating power (P, measured in W) generated per unit mass (m\text{MNP}, measured in g):

\[ \text{SAR} = \frac{P}{m_{\text{MNP}}} \]  

(1)

It may be argued that this definition of the SAR parameter can lead to confusion, especially in the clinical community where the SAR terminology is ingrained but has a rather different meaning. Clinically, SAR is used to denote the transfer of energy into the human body by radio frequency electromagnetic fields, such as that generated by mobile phone use or exposure to MRI scanners, and also by other means, such as ultrasound. In the clinical context, the SAR refers to the power dissipation per gram of living human tissue.

In the magnetic hyperthermia definition of SAR, the mass is that of the magnetic material alone. Although it can be said that the expected amount of heat transfer into human tissue should be small in comparison to that delivered to the MNPs, this does express an assumption that peripheral heating effects, such as eddy currents, are negligible. Furthermore, the SAR parameter as reported in the vast majority of magnetic hyperthermia papers is determined by suspending the MNPs in an \textit{in vitro} tissue analogue, which is almost always water. As such, the SAR values reported do not reflect the situation one might expect to find in human tissue, where heat dissipation by physiological means, such as increased blood flow, is to be expected.

Perhaps in recognition of this inherent difficulty with nomenclature, some authors refer to the parameter defined in (1) as the specific loss power (SLP), specific power loss (SPL) or specific heat power (SHP). However, it has been suggested that a distinctly different, more intrinsic parameter should be used for the special case of magnetic hyperthermia.

The power produced by any given MNP is determined by the physical and magnetic properties of that MNP, which is manifest in the imaginary part of its magnetic susceptibility \( \chi'' \) [12]. However, the power also scales linearly with the frequency (\( f \), measured in Hz) and quadratically with the strength of the AMF (\( H \), measured in A m\(^{-1}\)). Removing these extrinsic factors, one arrives at the intrinsic loss power (ILP, measured in Hm\(^2\)g\(^{-1}\)):

\[ \text{ILP} = \frac{\text{SAR}}{f H^2} \]  

(2)

which, in the rather more convenient units of nano–Henrys m\(^2\) per kg, computes as:

\[ \text{ILP} \ [\text{nHm}^2\text{kg}^{-1}] = \frac{\text{SAR} [\text{Wkg}^{-1}]}{f [\text{kHz}] \times H^2 [\text{kAm}^{-1}])^2} \]  

(3)

It should be noted that, due to the field and frequency dependence of \( \chi'' \), the ILP parameter can only be considered constant in relatively low field strength and low frequency regimes [5]. However, as these same conditions apply to the requirements for clinically acceptable limits in the AMF field and frequency, this is not a significant limitation for the comparison of materials intended for use in clinical magnetic hyperthermia.

In the remainder of this paper, we will refer to both the SAR and ILP parameters as defined in equations (1) and (2); however, it is our recommendation that the ILP parameter be used in preference to SAR when reporting the specific case of magnetic hyperthermia heating from ensembles of magnetic nanoparticles.

3. Measurements under non-adiabatic conditions

Both the SAR and the ILP parameters are essentially measures of power dissipation, and as such they are determined by calorimetric measurements that are best performed under adiabatic conditions in which there is very limited external heat transfer. However, such adiabatic measurement systems are difficult to build [13, 14] and the measurements themselves are time-consuming [15]. Consequently, adiabatic systems are seldom used, and almost all reported work on magnetic hyperthermia is performed on non-adiabatic apparatus.

While using non-adiabatic systems is in itself not problematic, neglecting or failing to take into account the attendant heat losses can be, and can result in the SAR/ILP values being underestimated—as shown by the comparison of SAR/
ILP values determined on identical samples using different calorimetric setups [14–16]. In one example, Natividad et al. found the non-adiabatic SAR value to be 21% lower than the adiabatic value [17]. Non-adiabaticity might also help explain a reported discrepancy between theoretical and experimental SARs, a factor two times difference for calculations using an experimental $\chi''$ and even more for those using a $\chi''$ found by Debye approximation [18].

Despite this potential problem, non-adiabatic systems can be used for quick and reliable SAR/ILP measurements, without the need for an extensive, time-consuming and expensive adiabatic setup. Using the experimental and analytical methods described below, we believe that accurate calorimetric measurements can be made, as long as the losses from the non-adiabatic setup are quantified and included in the calculation of results.

4. Theoretical background to SAR and ILP measurements

An adiabatic setup does not allow heat transfer between the MNP sample and its surroundings. Consequently, all heat produced by the MNPs is invested in the temperature rise of the sample. In this ideal case, the sample’s temperature is only produced by the MNPs and the heat deposited by the MNPs and the heat capacity of the sample ($C$, measured in J K$^{-1}$):

$$C \cdot \frac{dT(t)}{dt} = P \cdot \Delta T(t).$$

(4)

A measurement of the temperature rise during the application of an AMF will therefore yield a linear heating curve, as shown schematically in figure 1.

In non-adiabatic setups, however, the sample starts losing heat energy to the environment as soon as its temperature is higher than that of the space or materials surrounding it ($T_0$). There are several mechanisms of this heat loss:

- Conduction involves the heat transfer from the medium to adjoining materials and scales with the temperature difference $T - T_0$, surface area and thermal properties [19, 20].
- Convection, heat transfer by movement or diffusion of a heated medium, takes place in the air around the sample [19]. Usually one discriminates natural convection, movement that is solely caused by the temperature gradient, from forced convection which involves cooling by already-moving air [20].
- In the higher temperature difference ranges radiation becomes more dominant, when it increases with $T^4 - T_0^4$ [15, 19, 21].
- Eventually, the sample will also start losing energy due to evaporation or melting of the sample. This strongly non-linear energy loss appears when the temperature near the heat source approaches the boiling or melting point of one of the sample’s substances, even when the average temperature of the sample is well below that point. As these phase transitions cause cooling [19], the concentration changes and the thermal properties of another phase might be different, which can strongly influence the heating curve [22].

All these heat loss mechanisms cause the heating trend to curve downwards as the temperature increases (see figure 1).

In most studies in which the heating curve is used to estimate the power generated by MNPs, the heat loss is assumed to be linearly dependent on the difference in temperature between the sample and its surroundings. The temperature rise can then be elegantly described by the following differential equation [14]:

$$C \cdot \frac{d\Delta T(t)}{dt} = P - L \cdot \Delta T.$$

(5)

Here, $L$ (measured in W K$^{-1}$) is a constant that quantifies the proportionality between the temperature and the thermal losses and $\Delta T$ is the difference in temperature ($T - T_0$). This means that the slope of the heating curve decreases with the temperature of the sample until the lost energy per unit time is equal to the input, and the temperature saturates at a steady state. The solution to this differential equation is expressed by [14, 21]:

$$T - T_0 = \frac{P}{L} \left(1 - e^{-\frac{t-t_0}{\tau_L}}\right).$$

(6)

In the magnetic hyperthermia literature, this phenomenological equation is commonly referred to as the Box–Lucas equation [13, 23–25]. It should be noted that the linear-loss assumption is a relatively demanding one, and that it only holds for low temperature differences. If one takes into account all possible losses, the relation between temperature and losses becomes non-linear, especially for higher temperatures. A more comprehensive description of the heating curve would be:

$$C \cdot \frac{d\Delta T(t)}{dt} = P - P_L(T).$$

(7)

In this, $P_L(T)$ is a non-linear function that describes the power loss for each temperature. The presence of radiation and its fourth-power temperature dependence suggests that one would need at least a fourth-order polynomial to approach this function. In practice, as described in section 5.1, it is found that this is a good approximation.
For these equations to be valid, however, there is also another demanding assumption to be made, namely that the $T$ or $\Delta T$ that is measured should represent the temperature or change in temperature experienced by the entire sample. However, this is seldom the case, as even though the temperature is generally considered homogeneously distributed [14], it is governed by diffusion and convection within the sample and is therefore non-uniform [26, 27]. This leads to both temporal and spatial effects. Regarding temporal effects, discussion in the literature has focused on the time taken for heat to spread within the sample, compared to the time for the heat to spread to the surroundings [28], with some stating that the internal heat flow should be at least 10 times faster than that to the surroundings [14]. In practice, however, such effects are seldom encountered in magnetic hyperthermia experiments where the time constant of the thermal probe measurement is in the order of seconds—and indeed, we saw no evidence of them in our observations. Spatial effects are, however, much more pronounced, and in particular the location of the thermal probe within the sample is important (see section 5.3).

There are other aspects that may also contribute to the accuracy of the measurement:

- Delayed heating causes inaccuracy as it takes some time for the heat curve to take off after the heating has started [15]. When this delay is not taken into account, a linear fit from $t = 0$ underestimates the slope and the heating is perceived to be lower than it actually is. This is discussed in section 5.4.
- Temperature-dependence of the heat capacity might influence the heating behaviour in different temperature regimes [16]. The total heat capacity is the weighted average of all substances in the measurement container $C = \sum c_i \cdot m_i$ [14]. The heat capacity of water, however, scarcely changes in the relevant temperature range (<1%). Moreover, the heat capacity might include an unknown part of the container that also heats up during AMF application and confounds the results. In practice however, we find that these possible heat capacity related effects do not appear to be significant factors (see section 5.5).
- Magnetic field inhomogeneities may have a considerable effect on the total heat generated, especially since—at least under clinically applicable conditions—the SAR scales with the square of the field [26]. The solution to this is to ensure that the coil design used delivers as homogeneous a field as possible, e.g. by using a solenoid or Helmholtz configuration for the coils. Good homogeneity has also been reported from electromagnetic circuits [29].
- Inherent losses in the heating system must be considered, since no system has 100% efficiency and there are losses in any system where an electrical signal is translated into a magnetic field. Also, external sources can alter the calorimetric behaviour, since they can unintentionally heat up as well as cool down the sample. Both of these effects can lead to what we term ‘peripheral heating’, which is best determined experimentally on a system-by-system basis (see section 5.2).

5. Measuring SAR/ILP: experimental considerations

Experiments were performed in a custom-made setup that comprised a parafilm-covered plastic Eppendorf tube or glass vial containing the MNP sample, fibre-optic temperature measurement probes (Luxtron FOT Lab Kit, accuracy 0.2°C, sample frequency 1 Hz), and a water-cooled solenoid magnetic coil attached to a Magnetic AC Hyperthermia (MACH) system made by Resonant Circuits Ltd. Figure 2 shows a schematic drawing of the setup used, which conforms to published descriptions of ‘a typical experimental setup’ [14]. Indeed, many groups working on SAR/ILP measurements report similar non-adiabatic systems in their publications (e.g. [18, 22, 24, 26, 30–49]).

Some groups surround their samples with holders of varying insulating strengths, such as Styrofoam or other thermally insulating materials, while others do not [27]. We have chosen here to use no superficial insulation.

Experiments were performed using two commercially available magnetic nanoparticle suspensions. One was Ferucarbotran (Meito Sangyo Corp, Osaka), a biocompatible superparamagnetic iron oxide nanoparticle [50, 51] that has been used in several previous studies [52, 53]. The other was the 50 nm MNP fluid, FluidMAG-UC/A (Chemicell GmbH).

5.1 Linear loss regime

The degree of loss linearity was investigated in three different samples, comprising 1.0 ml, 0.5 ml and 0.25 ml respectively of Ferucarbotran at a concentration of 14 mg of iron per ml, measured under identical conditions. Each sample was heated to 75 °C, whereupon a cooling curve was obtained, i.e. the temperature $T$ was recorded as a function of time $t$. The numerical derivatives of the cooling curves were then computed,
assuming a heat capacity for the system of \( C = C_V \cdot V \), where \( C_V = 4.18 \text{ J K}^{-1} \text{ ml}^{-1} \) and \( V \) is the volume in ml. These were then plotted as \( C \cdot \Delta T / dt \) against the temperature difference \( \Delta T = T_{\text{max}} - T(t) \), as shown in figure 3.

For the 0.5 ml sample, a linear loss is observed for \( \Delta T \) values up to 35 °C, with a slope of ca. 6.7 mW K\(^{-1}\). The losses increase non-linearly for higher temperatures. Following the previously mentioned hypothesis for \( P_k(T) \) (in equation (7)), we expect that the losses might follow a non-linear relationship that is at least proportional to the temperature difference to the power four. Therefore, polynomial fits of the fourth order are also shown. On the face of it, these expressions describe the losses fairly well.

Since changing the sample volume changes the ratio of the sample volume to its surface area, it is to be expected that the behaviour of the losses would also change. This was clearly observed, as shown in figure 3, where the linear loss regime for the 1.0 ml sample was larger, at ca. 40 °C and for the 0.25 ml sample was smaller, at ca. 30 °C. The rates of loss were also different, being higher for the 1.0 ml sample, at ca. 8.5 mW K\(^{-1}\) and lower in the 0.25 ml sample, at ca. 4.2 mW K\(^{-1}\). This hierarchy is to be expected given that the larger the volume, the more heat there is to be dissipated for each degree K in cooling; but the shape effects are apparent in that the rates of loss do not simply scale with sample volume.

It is clear therefore that both the extent of the linear loss regime and the rate of loss within that regime are setup-dependent parameters that should be expected to vary between different measurement systems, and even for a given system, will also vary as a function of sample volume and morphology. Nevertheless, it is also clear that the linear loss approximation embodied in equation (5) is an attainable experimental condition, so that reliable measurements of both SAR and ILP should be readily achievable.

5.2. Peripheral heating

To assess the extent to which there might be a peripheral heating effect on water-borne MNP dispersions placed within the magnetic heating apparatus, a pure water sample of 0.5 ml, containing no magnetic particles at all, was brought into the setup. The water temperature was measured for a period of 25 min during the application of an AMF of different field amplitudes (5–14 kA m\(^{-1}\)), corresponding to different currents (see figure 4). Significant heat rises of 1 °C or more were seen for all but the smallest AMF.

The origin of this peripheral heating effect is not precisely known, but it is likely to be a combination of an induced eddy current effect in the polar fluid and a radiative heating effect from the AMF system itself. It is therefore likely also to be an effect that will vary from system to system in different laboratories. In our laboratory setup, we conducted some exploratory tests (not shown) on both pure water and a salt solution at physiological concentrations, which indicated that after 10 min of heating the temperature difference between the two was no more than 0.1 K. Given that the induced eddy current effect should be strongly dependent on the electrical conductivity of the sample, we infer that at least in our setup, the peripheral heating effect is dominated by radiated heat from the apparatus itself. In any case, from the observations in figure 4 one can conclude that peripheral heating can be a significant factor in the measured heating curves, and that, in particular, the initial heating slope may be affected. This is significant as the initial slope is often used as the key determinant of the SAR/ILP measurement (see below).

Various strategies may be adopted to minimise the influence of the peripheral heating effect. We explored the possibility of using a water-only heating curve as a calibration curve, measured immediately before the sample of interest and then subtracted from the obtained \( T(t) \) curve. However, in practice this leads to delays and uncertainties as one needs to allow the heating apparatus to return to the same initial state before each measurement. A better and more elegant solution would be to measure both the water and the sample simultaneously and record the difference between the temperatures of the two [29]. However, this requires that the heating apparatus be able to accommodate the water and the sample under identical conditions, which in many cases (including ours) is not feasible. For
this reason, we have adopted a third approach which is to allow the system to ‘warm up’ (i.e. equilibrate) to the temperature it will reach when the specific field is applied (i.e. the baseline), before starting a measurement. This procedure was adopted for all subsequent measurements reported below.

5.3. Temperature distribution

An inhomogeneous spatial distribution of temperature is to be expected in any sample that is heated in a non-adiabatic system. The causes for this include steady-state diffusion and convection effects, as well as the inhomogeneous dissipation of heat from the sample into its environment, either from its surface or through the walls of the sample container.

These temperature distributions may be significant, as illustrated in the thermal camera images shown in figure 5 for the case of two commonly used sample holders—a plastic Eppendorf tube with a tapered bottom section and a glass flat-bottomed cylindrical vial. It is clear therefore that the location of the thermal probe within the sample is an important factor to consider when measuring the temperature of the sample. Indeed, it has been suggested that the most accurate measurements are carried out just beneath the sample surface [26]; however, since the temperature is the highest at that location, the average temperature rise of the entire sample might be overestimated.

To further investigate the temperature distributions in the samples, heating curves were recorded from identical 0.5 ml volume samples of Ferucarbotran (diluted in water to 7 mg ml⁻¹ of iron oxide) using multiple fluoroptic probes placed at different locations in the sample holders (see figure 6).

Two configurations were examined: one corresponding to the differences in temperature vertically, on the cylindrical axis of the holders, between the top and bottom of the fluid; and one radially, at the top of the fluid, just below the meniscus, between the centre and the edge of the sample (see figure 7). The data show that, in the 25 to 65°C range in which most SAR/ILP measurements are made, differences of 1–2°C appear in both containers for radial displacement of the fluoroptic probe and in the glass vial for vertical displacement. Larger temperature differences of up to 7.5°C were measured between the top and the bottom of the fluid in the Eppendorf tube.

These results show that in the case of the flat-bottomed vial, any probe that is positioned more or less centrally within the fluid will record a local temperature that is representative (within ± 1°C) of the mean temperature of the entire volume. However, in the case of the conical Eppendorf holder, significant differences in the recorded temperature may appear, dependent on the probe position. If this is not appropriately accounted for, inaccurate or misleading results might be obtained.
For this reason, we examined further the local temperatures \( T_x \) recorded by the fluoroptic probe as a function of its displacement \( x \) along the central axis of the Eppendorf tube (see figure 8). The sample was heated and held in steady state by balancing the AMF-supplied magnetic heating to the ambient thermal losses to the environment. \( T_x \) was found to vary smoothly from ca. 54 °C at the bottom of the tube, to ca. 62 °C at the top of the tube. The mean temperature of the entire 0.5 ml sample was then estimated numerically as 

\[
T_{\text{mean}} = \frac{\sum T(x_i) \cdot V(x_i)}{\sum V(x_i)},
\]

where \( V(x_i) \) is the volume of a horizontal slice of the container at position \( x_i \). This calculation gave \( T_{\text{mean}} \approx 61 ^\circ C \), corresponding to the temperature measured at \( x \approx 10 \text{ mm} \), a point ca. one-third of the distance from the meniscus of the liquid sample to the bottom of the Eppendorf tube.

In light of these findings, we recommend the use of two temperature probes at different locations in the sample as a way of both monitoring and correcting for the non-uniform temperature distribution. In the case of the 0.5 ml sample in an Eppendorf tube, we find that the mean of the temperatures recorded from fluoroptic probes positioned just underneath the meniscus and two-thirds of the way towards the bottom of the tube, represents the average temperature very well. Alternatively, one probe placed at one-third distance below the sample’s surface can be used. In the case of an 0.5 ml sample in a cylindrical flat-bottomed container, the temperature distribution is almost homogeneous, so that a centrally placed probe or pair of probes gives a good measure of the average temperature.

5.4. Delayed heating

Temporal effects are to be expected at the outset of any experiment. In the case of magnetic heating, there may be many causes, including the time constant associated with the inductive heating mechanism, the time associated with the establishment of any diffusion or convection within the fluid and the intrinsic response time of the temperature probes.

We have observed such effects in our system, as illustrated in figure 9, which shows a typical instance in which a time delay of ca. 5s was measured between the time that the MACH heating system was switched on and the time that an observable thermal response was recorded.

Delayed heating is not necessarily a confounding factor in the measurement of heating effects, so long as it is known and accounted for. However, as discussed in section 6.1, there are some analytical approaches to computing SAR/ILP that rely on estimating the initial slope of the heating curve, in which case the possibility of incorrect measurement becomes more likely.
5.5. Total heat capacity

Lastly, we consider which heat capacity value should be used in the SAR/ILP calculations. In the literature, it is often assumed (either explicitly or implicitly) that the heat capacity of a sample equals the heat capacity of an equivalent volume of pure water. However, this neglects any possible contribution to the heat capacity from the sample holder or the sample environment.

To test whether the contributions of the container to the heat capacity are indeed negligible, the ILP values of an 0.5 ml (20 mg ml⁻¹ iron oxide) FluidMAG UC/A sample were obtained from a sample in a flat-bottomed glass vial, and from the same sample in a geometrically identical, 3D-printed poly(lactic acid) (PLA) vial. The glass vial was of mass 2.4 g and heat capacity 1.70 J K⁻¹, while the PLA was lighter, at 1.4 g and had a higher heat capacity of 2.35 J K⁻¹ [54].

To test the hypothesis that the only heat capacity that need be considered is that of the suspension medium, i.e. water, the ILP vales were calculated assuming that to be the case. In three separate measurements in each vial, ILP values of 1.68 ± 0.10 nHm² kg⁻¹ and 1.66 ± 0.03 nHm² kg⁻¹ were measured for glass and plastic, respectively, under application of a 3.8 kA m⁻¹ and 989 kHz AMF. Given that the differences between the values obtained in the two containers are well within their respective standard deviations, it appears that the assumption is indeed valid.

6. Measuring SAR/ILP: analytical models

We turn our attention now to the analytical models and methods used to extract the SAR and/or ILP parameters from magnetic heating (and cooling) measurements. We have identified five such distinguishable methods, some of which are simple but prone to error, and others that are reliable but, as yet, seldom used by practitioners. Given the importance attached to getting this analytical aspect of the SAR/ILP determination right, we will describe and discuss each method in turn, then provide a comparative test to establish which are best suited to general use.

6.1. Initial slope method

In this most commonly used method, one tries to approximate the slope of the initial heat rise, β [15]. The underlying assumption is that the initial slope of the curve does not suffer from losses since the sample is at its baseline temperature:

\[ \beta = \lim_{t \to 0} \frac{dT}{dt} = \frac{d}{dt} \left( \frac{P}{C} \left( 1 - e^{-t/T_C} \right) \right) \bigg|_{t \to 0} = \frac{P}{C} . \]  

Therefore, the SAR can be computed using:

\[ \text{SAR}_{\text{initial-slope}} = \beta C / m_{\text{MNP}} . \]  

However, since heat transfer mechanisms may already be significant at the onset of the heating curve, e.g. because the temperature of the sample may already be above the baseline temperature, this method might be sensitive to inaccuracies [15]. Also, as seen in section 5.4, delayed heating effects might complicate the initial slope measurement.

Furthermore, as Andreu and Natividad (2013) found in their review, even within this method, there are several different computation methods that have been applied [14]. Expanding on their overview of the literature, in a representative random survey we found seven groups with a linear fit to the first tens of seconds of the heating curve [17, 42, 55–59], the intervals ranging from 10 to 100s [27]; three groups with an extrapolated polynomial fit [60–62]; nine groups directly calculating the slope from the \( \Delta T \) and \( \Delta t \) in a particular interval [26, 32, 36, 38, 41, 44, 63–65]; and nine groups taking a numerical derivative of the entire \( \Delta T(t) \) curve, of which three used the constant slope [25, 34, 43] and six the maximum slope [21, 30, 35, 66–68] to calculate β. This variety of approaches is likely to result in a variety of results.

To explore this further, we recorded the first 30 s (taking account of the delayed heating effect) of a typical magnetic heating curve and made five different linear approximations to its slope (see figure 10). These were: the linear part of a polynomial fit to the curve; a ‘direct’ estimate \( \Delta T(t = 30 \text{ s}) - \Delta T(t = 0) \) / \( \Delta t \) where \( \Delta t = 30 \text{ s} \); the maximum and median slopes calculated numerically in 3s rolling intervals over the range; and a simple linear fit to the full dataset. Three of these methods yielded similar values and on inspection appear to accurately reflect the actual slope of the curve, but the linear part of the polynomial fit gave a 20% larger value and the maximum numerical derivative estimate was 60% larger. We conclude that the latter two methods are not appropriate for use in this way.

6.2. Decay method

This relatively uncommon method uses the steady state temperature \( T_{ss} = P / L \) as well as the characteristic time of the system cooling down (\( \tau = C / L \)) to determine SAR [14, 21]:

\[ \text{SAR}_{\text{Decay}} = \left( \frac{T_{ss}}{\tau} \right) \left( \frac{C}{m_{\text{MNP}}} \right) . \]  

As with the initial slope method, uncertainty in the decay method arises from the many ways to determine \( \tau \), either by fitting or using numerical derivatives. Moreover, it is not always verifiable whether the steady state temperature has been reached in a reasonable amount of time–and even if it has, the system must be in the domain for which linear loss can be assumed, and \( T_{ss} = P / L \) holds.

6.3. Corrected slope method

This new method, derived by the authors, corrects the value determined by the (initial) slope method for any linear losses already apparent at that temperature \( (P = C (dT / dt) + \Delta T) \). When the value of thermal loss \( L \) of the system is known, one can calculate the SAR using:

\[ \text{SAR}_{\text{Corrected-slope}} = \left( \frac{C (dT / dt) + \Delta T}{L} \right) / m_{\text{MNP}} . \]  

In this equation \( \Delta T \) is the (mean) temperature difference between the sample and baseline, which, of course, must be within the bounds of the linear-loss regime. Even when the loss \( L \) is not known, it is possible to calculate its most
probable value by determining the slope for multiple temperatures along the heating curves (appendix 1).

6.4. **Box–Lucas method**

As described in equation (7), in the linear-loss regime the heating curve should follow a Box–Lucas equation. Therefore, a least-squares fit to the following expression can be used [13, 21, 24, 25]:

\[
\Delta T = A \left(1 - \exp \left(-\lambda t + t_0\right)\right). \tag{12}
\]

One can then use the fitting parameters \(A\) and \(\lambda\) to compute the SAR, since \(A\lambda = T_{\text{sat}}^{-1} = P / C\):

\[
\text{SAR}_{\text{Box–Lucas}} = A\lambda C / m_{\text{MNP}}. \tag{13}
\]

The \(t_0\) parameter, correcting for a non-zero start of the curve, is generally not needed or used.

6.5. **Steady state method**

Lastly, one can wait for the system to reach the steady state temperature and calculate the losses that are associated with that temperature. Since the input power equals the dissipated losses in the steady state condition \((T_{\text{ss}} = P / L)\), the SAR is then:

\[
\text{SAR}_{\text{steady-state}} = T_{\text{ss}} L / m_{\text{MNP}}. \tag{14}
\]

In this method, the loss parameter \(L\) has to be determined. This can be done using the corrected slope method described above or through an experiment similar to that presented in figure 3.

7. **Discussion**

Even after taking into account all of the experimental considerations in section 5, it is apparent that the determination of the SAR or ILP value is dependent on the choice of analytical method in section 6. This was clearly seen in the ILP determinations using the initial slope method in figure 10, where in an extreme case the slope was overestimated by 60%.

To assess the relative accuracy of the different methods, we have tested them against a calibration standard based on the heating of a 10 ml water sample using an immersed 56Ω electrical resistor. A current of 90 mA was passed through the resistor, delivering \(P = 0.45\) W of power. The \(\Delta T(t)\) curve was recorded and then analysed as if it were a magnetic heating curve. The resulting ‘SAR'/\(P\) values thus obtained are shown in figure 11, where it is clear that of the five methods, only the corrected slope and the Box–Lucas fit methods gave ratios of unity. The others all underestimated the ‘SAR’, by ca. 11%, 17% and 24% for the steady state, initial slope and decay methods, respectively.

To assess the robustness of the corrected slope and Box–Lucas methods, we then measured the magnetic heating in Ferucarbotran using selected experimental conditions to test the importance (a) of the starting temperature, \(T_{\text{start}}\), relative to the baseline temperature, \(T_{\text{B}}\) and (b) of the measurement time, \(t_{\text{max}}\) (see figure 12). On inspection, it is apparent that neither method was particularly sensitive to \(T_{\text{start}}\), as evidenced by the small standard deviations obtained over 15 separate measurements (figure 12(a)), but that the Box–Lucas method was sensitive to variations in \(t_{\text{max}}\) (figure 12(b)). This may indicate that longer measurement times are preferable for the
Box–Lucas method so that the heating curve can saturate fully and be more easily fitted.

It is also noticeable in figure 12(a) that the Box–Lucas ILP value is ca. 8% lower than the corrected slope ILP value. A similar trend, albeit not so pronounced, was evident in the calibration data in figure 11. This may be an indication that in absolute terms the corrected slope method is the more accurate of the two.

To test this hypothesis, heating data were recorded on a 0.5 ml sample of 20 mg ml⁻¹ FluidMag-UC/A. This is a commercially available ferrofluid whose ILP has been previously measured in adiabatic systems. In one reported experiment, conducted in an AMF of amplitude $H = 2.0$ kA m⁻¹ and frequency $f = 109$ kHz, the ILP was $1.65 \pm 0.03$ nHm² kg⁻¹ [15]. A similar figure was obtained in a second adiabatic experiment using $H = 1.1$ kA m⁻¹ and $f = 108$ kHz, where the ILP was $1.66 \pm 0.07$ nHm² kg⁻¹ [17]. In our measurement, we found an ILP of $1.68 \pm 0.03$ nHm² kg⁻¹ at $H = 3.7$ kA m⁻¹ and $f = 988$ kHz, for the sample mounted in an Eppendorf tube and $1.68 \pm 0.08$ nHm² kg⁻¹ when the sample was mounted in a flat-bottomed glass vial. Both values are well within experimental error of the adiabatic values, hence we conclude that the corrected slope method is indeed the most accurate and reliable method of determining SAR/ILP in a non-adiabatic system.

It is interesting to reflect on the implications of this conclusion with regard to the many previously published values of SAR and ILP in magnetic hyperthermia materials. We have conducted a survey of a representative set of 50 datasets retrieved from published plots of $\Delta T(t)$ curves [18, 21, 24, 25, 30, 31, 33–38, 41, 55, 57, 58, 60, 67, 69–75]. All but three datasets had been analysed using the initial slope method, albeit using a variety of different linear approximations of the type surveyed in section 6.1, leading to both over- and under-estimations of the slope. Figure 13 shows the ratio between the reported SAR value and the corrected slope value (calculated using the method described in section 6.3) for each of the fifty curves.
Naturally, the measurement time differed from one dataset to the next, but in every case as much of the curve as possible was used for the corrected slope calculation. If the measurement time allowed it, the slope was computed every 15 s over an interval of 60 s. (For a 5 min heating curve this resulted in 17 corrected slope values, computed over the intervals 0–60 s, 15–75 s, 30–90 s, … 240–300 s, respectively.) Furthermore, in some cases, where the complete data were not reported, assumptions had to be made regarding the baseline temperatures of the measurement systems used and the heat capacities of the samples measured. However, our calculations show these assumptions to be of relatively minor significance, affecting the derived SAR values by a few percent at most. As shown in figure 13, the variability was much more pronounced than that, with only 24% of the reported values falling within 5% of the corrected slope value.

Given that these are errors associated with the analytical process only and that in many reports little or no attention is paid to experimental errors regarding probe positioning, peripheral heating and the delayed heating effect, the total variation between reported and actual SAR/ILP values is likely to be much more.

8. Conclusions

The experimental conditions under which reliable measurements of both the SAR and ILP parameters of magnetic hyperthermia materials may be performed in a non-adiabatic system have been comprehensively reviewed and quantified. These conditions are listed in Appendix 1 in the form of a set of recommendations that we hope will be applicable in most laboratories and will enable others to avoid the pitfalls that could otherwise make the measurements unreliable.

Similarly, the analytical methods by which the SAR and ILP values are extracted from the heating curves have been reviewed and tested against robust standards. We find that the most commonly used ‘initial slope’ method is sensitive to the experimental conditions and prone to underestimation by up to 25%. A better approximation is the full-curve fit of the ‘Box–Lucas’ method, although even here underestimation by up to 10% can be expected. We find that the ‘corrected slope’ method provides the most accurate results under the greatest range of experimental conditions and we therefore recommend that it be adopted as a standard method for SAR and ILP measurements. To assist this, details of the implementation of the corrected slope method are given in Appendix 1. In addition, a simple-to-use computer program, written as an executable file in two commonly used formats (Microsoft Excel and MATLAB), is available online for free download and use [76].

Given the importance placed on the SAR and ILP parameters as determinants of good and bad materials for magnetic hyperthermia, we believe that it is essential that the experimental methods used should be scrutinised and standardised. Furthermore, given the clinical safety imperative that all materials that may be destined for medical use must be fully characterised and quantitatively analysed, it is incumbent on the hyperthermia research community to address the issue. It is in this context that we hope that this paper will be received as a useful contribution to the field.

Appendix 1: Recommended experimental and analysis methods for SAR and ILP measurements using a non-adiabatic system.

To perform SAR and ILP measurements in a non-adiabatic system, the protocol summarized in Table A1 is recommended.

It is especially important to identify the linear loss regime for any given measurement system. This is a characteristic not just of the experiment apparatus, but also of the sample surface area and volume. To do this, one should heat an MNP suspension to $\Delta T \approx 60^\circ$C above room temperature, switch off the AMF and then measure the cooling curve as the sample’s temperature drops back to room temperature. The numerical derivative of the cooling curve, plotted against $\Delta T$, should resemble figure 3. The maximum $\Delta T$ beyond which the curve is no longer linear represents the extent of the linear loss regime and no measurements should be performed beyond that value.

After calibration, one has to choose the magnetic field, frequency and particle concentration so that the heating curve will not reach temperatures that exceed the regime in which the assumption of linear losses holds. As a rule of thumb, one can estimate this by using the following criterion:

$$P = SAR \cdot m = ILP \cdot H^2 m < L \Delta T_{lim}, \quad (A1)$$

in which $ILP$ is the expected ILP ($H m^2 kg^{-1}$), $f$ is the frequency (Hz), $H$ is the magnetic field strength ($A m^{-1}$), $m$ is the total particle mass (kg), $L$ is the linear loss parameter (W K$^{-1}$), and $\Delta T_{lim}$ is the upper limit of the linear temperature regime (K above baseline). Both $L$ and $\Delta T_{lim}$ may be deduced from figure 3 style cooling curve.

Since peripheral heating can affect the natural baseline temperature for measurements, one should ensure that the heating curve starts at the temperature a water sample (of the same volume as the ferrofluid being measured) would have when a magnetic field is applied. This can be done by heating the ferrofluid for a few seconds and letting it reach a steady state before the actual measurement. For the SAR/ILP measurement itself, recording the heating curve for 5 to 10 min is usually sufficient. It does not matter whether a steady temperature state is reached during the measurement period.

With the data recorded, the SAR (and ILP) can then be calculated using the corrected slope method. We recommend that the parameter be calculated over an interval of 30–60 s, at $N$ intervals along the heating curve. This allows one to compute both the SAR/ILP parameter and the linear-loss parameter $L$. The following formula describes the mathematical operation of the corrected slope method:

$$SAR = \frac{1}{N} \sum_{i}^N C \left( \frac{dT}{dt} \right) + L(\Delta T)_i, \quad (A2)$$

in which $C$ is the heat capacity of the sample (J K$^{-1}$), $(dT / dt)$ is the slope determined by a linear fit of the data in interval
i and $\Delta T_i$ is the difference between the mean temperature of interval $i$ and the baseline temperature. Calculating the slope at different positions on the heating curve gives one an estimate of the accuracy of the measurement and is also a useful way to check that a reliable experiment has been performed. This is illustrated in figure A1 for a 0.5 ml sample of Ferucarbotran (28 mg ml$^{-1}$ iron), for which the ILP was calculated at 12 points in the first 3 min of the heating curve. The reliable measurement is largely flat, while the unreliable one is clearly curved.

The corrected slope fits also provide an estimate of the linear loss parameter, $L$. Typical values that we have measured for $L$ have been ca. 6 mW K$^{-1}$ for a plastic Eppendorf tube, 11 mW K$^{-1}$ for a flat-bottomed glass vial and 9 mW K$^{-1}$ for a flat-bottomed vial made from PLA. These values roughly follow the container material’s conductance coefficient (0.25 W mK$^{-1}$ [77], 1.1 W mK$^{-1}$ [78] and 0.12 W mK$^{-1}$ [54] for polypropylene, glass and PLA, respectively), but shape and wall thickness also contribute to the measured $L$. This underlines the need to measure $L$ on a case-by-case basis.

### Table A1. Recommended procedure for non-adiabatic measurements of SAR and ILP.

1. **Define the linear-loss regime**
   
   This is system-dependent, and also affected by the sample volume and container shape. It is found by recording the cooling curve after heating a MNP sample to ca. 60°C above room temperature. Plotting the numerical derivative $dT/dt$ versus $\Delta T$, as in figure 3, allows one to identify the linear-loss regime. All subsequent measurements should fall within this range.

2. **Choose the measurement parameters**
   
   Use equation A1 to choose the field amplitude, frequency and MNP concentration so that the temperature will stay within the linear-loss regime. If an estimate of the ILP is not available, a trial measurement is required.

3. **Determine the baseline temperature**
   
   The baseline temperature is the equilibrium temperature of a sample, taking into account peripheral heating. It is found by applying an AMF of the chosen amplitude and frequency to a sample of the MNP solvent alone (e.g. water), without any MNPs present. Usually the baseline temperature reaches ca. 1–3°C above room temperature within 10–20 min.

4. **Choose the probe configuration**
   
   Multiple probes are recommended, but a single probe can be used. If two probes are used, take the mean of both as the average sample temperature. For a flat-bottomed cylindrical container use one probe, placed in the middle of the sample; or two probes, one just under and one just above the middle. For a quasi-conical container such as an Eppendorf tube use one probe, placed at 1/3 of the height below the surface; or two probes, one just below the surface and one 2/3 down.

5. **Equilibrate before the measurement**
   
   Magnetic heat the sample a few degrees in order for the system to ‘warm up’ before the start of actual measurement. The measurement can be performed once the sample has cooled down to the baseline temperature, as defined in step 3.

6. **Perform the measurement**
   
   Record the temperature for 1 to 2 min before applying the AMF, so that the baseline temperature is noted and any time delay effects are captured. It is usually sufficient to measure the temperature once every 1 to 5 s during a AMF application of 5 to 10 min.

7. **Calculate the heating ability**
   
   Use the Matlab or Excel programme provided to calculate the heating ability (either the SAR or the ILP) using the corrected slope method. In most cases it is safe to assume a heat capacity equal to that of the MNP solvent. Making a few repeated measurements may help to estimate the experimental error.

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**Figure A1.** ILP measurement for a Ferucarbotran sample calculated by the corrected slope method at twelve points along the heating curve: (left) for an accurate measurement within the linear-loss region and (right) for an inappropriate measurement design for which the rate and extent of heating exceeded the linear-loss regime.
The authors have written and made available for free download and use a corrected slope data analysis program [76]. Versions are provided in both MATLAB (Mathworks 2013b, Natik, MA) and in Excel (Microsoft Office 2007).

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