



## Research articles

## Magnetic parameters evaluation of magnetic nanoparticles for use in biomedical applications

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## ARTICLE INFO

## Keywords:

Magnetic nanoparticle  
Magnetization curve  
AC susceptibility  
Magnetic-core size distribution  
Anisotropy energy constant  
Néel relaxation

## ABSTRACT

We present a procedure for the comprehensive evaluation of parameters of magnetic nanoparticles (MNPs), such as saturation magnetization, core-size distribution, anisotropy energy constant, and characteristic time for Néel relaxation for use in biomedical applications and fundamental MNPs research. The static magnetization curve of suspended and immobilized MNP samples and the AC susceptibility of immobilized samples were used for the evaluation of these parameters. The magnetic properties reconstructed from the obtained parameters agreed with the experimental results, indicating the accuracy of the estimation procedure. Using the procedure, the parameters of the commercial Resovist MNP sample were evaluated. Then, the Resovist sample was magnetically fractionated into two MNP samples with large and small core sizes, and the parameters of the two fractionated samples were evaluated. It was demonstrated that the parameters of the Resovist sample are given by the volume-weighted average for those of the fractionated samples.

## 1. Introduction

Magnetic nanoparticles (MNP) have been widely studied for use in biomedical applications, such as hyperthermia and magnetic particle imaging (MPI) [1–4]. The key parameters that determine MNP performance in these applications are their magnetic moment  $m$  and relaxation time  $\tau$  [5,6]. The value of  $m$  determines the signal strength and nonlinearity. Large  $m$  value is desired to obtain rich harmonic signals in MPI and large hysteresis loss in hyperthermia. The value of  $\tau$  determines the response to high-frequency field, and appropriate  $\tau$  value is required depending on the frequency of the external field used. Therefore, it is necessary to choose MNP with proper values of  $m$  and  $\tau$  for specific biomedical application.

It is known that  $m$  and  $\tau$  values are determined by the parameters of the MNP. The value of  $m$  is determined by the saturation magnetization  $M_s$  and magnetic core size  $d_c$ . The relaxation time  $\tau$  is determined by the Brownian relaxation time  $\tau_B$  or the Néel relaxation time  $\tau_N$ . The Brownian relaxation time  $\tau_B$  is governed by the hydrodynamic diameter  $d_H$  of particle, viscosity  $\eta$  of surrounding medium, and temperature  $T$ . The  $\tau_N$  value is determined by the anisotropy energy constant  $K$ ,  $d_c$ ,  $T$ , and the characteristic time  $\tau_0$ . Therefore, it is necessary to obtain these parameters to quantitatively evaluate  $m$  and  $\tau$ .

Among these parameters,  $\eta$  and  $T$  are usually known. The hydrodynamic diameter  $d_H$  can be obtained using an optical method, such as

dynamic light scattering (DLS) method [7,8]. The remaining parameters  $M_s$ ,  $d_c$ ,  $K$ , and  $\tau_0$  are estimated from the magnetic properties of MNP sample. The  $M$ - $H$  curve of suspended MNP sample can be used to evaluate the values of  $M_s$  and  $d_c$ . The distribution of  $d_c$  in MNP sample can also be evaluated by comparing the experimental  $M$ - $H$  curve with the theoretical one based on the Langevin function [7–11]. The value of  $K$  can be evaluated from the temperature and frequency dependence of the susceptibility of immobilized MNP sample [12–14]. The  $M$ - $H$  curve of immobilized MNP sample can also be used to evaluate  $K$  [15–17].

In this paper, we present a procedure for the comprehensive evaluation of the magnetic parameters  $M_s$ ,  $d_c$ ,  $K$ , and  $\tau_0$ . For this purpose, we use the  $M$ - $H$  curve of suspended and immobilized MNP samples to evaluate the values of  $M_s$ ,  $d_c$ , and  $K$ . We also use the AC susceptibility (ACS) of immobilized MNP sample to evaluate the value of  $\tau_0$ . First, we explain the evaluation procedure using a single-core SHP20 MNP sample (Ocean Nanotech), which has narrow size distribution. The validity of the evaluation procedure was demonstrated using this sample.

Then, we use the proposed procedure to evaluate the parameters of a multi-core Resovist MNP sample (FUJIFILM RI Pharma), which is known to have admirable performance in both hyperthermia and MPI applications [18,19]. As the Resovist MNP sample has wide size distribution, the original Resovist sample was magnetically fractionated into two MNP samples with narrow size distributions: one sample with

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smaller core size and another sample with larger core size. The parameters of the two fractionated samples were evaluated using the proposed procedure. It was demonstrated that the parameters of Resovist MNP are given by volume-weighted average for those of the fractionated samples.

## 2. Evaluation procedure of MNP magnetic parameters

For homogeneously magnetized spherical MNP, the magnetic moment  $m$  and the Néel relaxation time  $\tau_N$  are expressed as [20,21]

$$m = M_s V_c \quad (1)$$

$$\tau_N = \tau_0 \frac{\sqrt{\pi}}{2} \frac{1}{\sqrt{\sigma}} \exp(\sigma) \text{ for } \sigma > 2 \quad (2)$$

where,

$$\sigma = \frac{KV_c}{k_B T}, \quad V_c = \frac{\pi}{6} d_c^3 \quad (3)$$

We note that MNP with relatively large core size are used for MPI and hyperthermia applications, and the condition  $\sigma > 2$  in Eq. (2) can be satisfied for these MNP.

We start with evaluating the parameters  $M_s$ ,  $d_c$ ,  $K$ , and  $\tau_0$ , which determine  $m$  and  $\tau_N$  as shown in Eqs. (1)–(3). In the experiment, we used the commercial SHP20 MNP sample. The nominal core size was  $d_c = 20$  nm, and the iron concentration of the original sample was 5 mg (Fe)/mL. For the  $M$ - $H$  curve measurement of suspended sample, 100  $\mu$ L of the original SHP20 magnetic fluid were diluted in 50  $\mu$ L of purified water. The immobilized MNP sample was prepared by diluting 100  $\mu$ L of the original SHP20 magnetic fluid in 180 mg of liquid epoxy resin. Then, the sample was left for 12 h to immobilize via solidification.

### 2.1. Saturation magnetization and core size distribution

The value of  $M_s$  and  $d_c$  distribution were obtained by analyzing the static  $M$ - $H$  curve of suspended MNP samples. In the experiment,  $M$ - $H$  curve was measured up to  $\mu_0 H = 1$  T with measurement time of 30 min. The measurement was performed using equipment constructed in the laboratory based on the conventional sample vibration scheme; the sample vibration frequency was 7 Hz.

Fig. 1(a) shows the measured  $M$ - $H$  curve of the SHP20 sample at low fields. It is well known that the  $M$ - $H$  curve of suspended MNP samples can be described by the Langevin function as follows [7–11]:

$$M = \int_0^\infty n_m(m) m L(\xi) dm \quad (4)$$

with

$$L(\xi) = \coth(\xi) - 1/\xi \quad (5)$$

$$\xi = \frac{\mu_0 m H}{k_B T} \quad (6)$$

where  $M$  is the ensemble magnetization in the direction of the applied field  $H$  and  $L(\xi)$  is the Langevin function. The value  $n_m(m)$  in Eq. (4) represents the number density of MNP with a magnetic moment  $m$  per unit of MNP volume.

The measured  $M$ - $H$  curve of the suspended SHP20 sample at low fields is represented with dots in Fig. 1(a). The value  $M_s = 270$  kA/m was determined by the value of  $M$  at  $\mu_0 H = 1$  T. The distribution of  $m$  in the MNP sample can be obtained from the experimental  $M$ - $H$  curve by solving the inversion problem given in Eq. (4) [9–11]. The inversion problem was solved numerically by using a mathematical technique called nonlinear-non-negative least square method (NNLS) [10].

The obtained  $n_m(m)m^2$  vs.  $m$  curve for the SHP20 sample is shown in Fig. 1(b). As shown, the curve has main peak at  $m = 1.4 \times 10^{-18}$  Am<sup>2</sup>. Another sub peak is also obtained at  $m = 2 \times 10^{-20}$  Am<sup>2</sup>. Using Eq. (4), we can reconstruct the  $M$ - $H$  curve from the obtained  $nm(m)m^2$  vs.  $m$

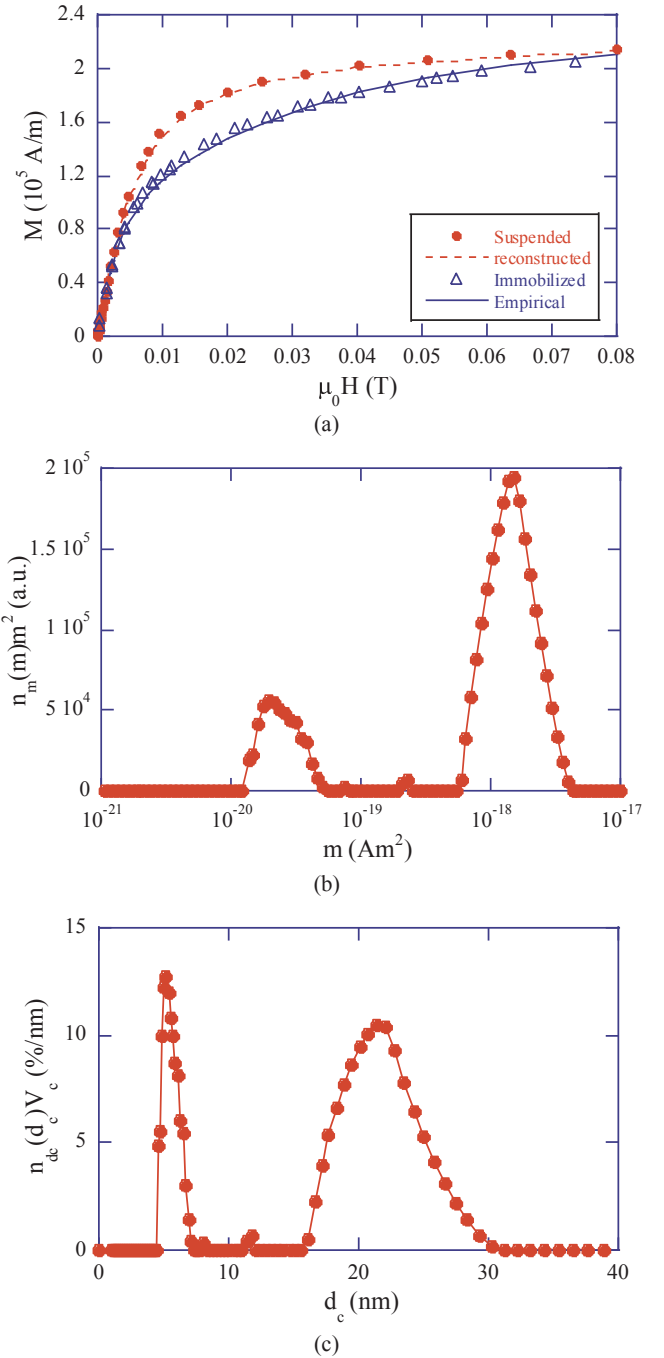


Fig. 1. (a)  $M$ - $H$  curve of suspended and immobilized SHP20 samples and analytical results. (b) Magnetic moment distribution for SHP20 MNP. (c) Normalized core size distribution of SHP20 MNP.

curve. The reconstructed  $M$ - $H$  is illustrated with the dotted line in Fig. 1(a) showing good agreement with the experimental  $M$ - $H$  curve of suspended sample.

The  $n_m(m)m^2$  vs.  $m$  curve was then transferred to the distribution of  $d_c$  using the following relationship between  $n_m(m)$  and number density of MNP with core size  $d_c$  per unit of MNP volume,  $n_{d_c}(d_c)$ :

$$n_{d_c}(d_c) = n_m(m) M_s \frac{\pi}{2} d_c^2 \quad (7)$$

Fig. 1(c) represents the estimated core size distribution obtained with  $M_s = 270$  kA/m. The horizontal axis represents the diameter of the magnetic core  $d_c$ . The vertical axis represents the estimated volume-weighted core size distributions,  $n_{d_c}(d_c)V_c$ , normalized to 100%. As

shown, the  $n_{dc}(d_c)V_c$  vs.  $d_c$  curve has peaks at  $d_c = 5$  and 21 nm, corresponding to the peaks in  $n_m(m)m^2$  vs.  $m$  curve shown in Fig. 1(b). The value of  $d_c = 21$  nm is consistent with the nominal size of 20 nm of the SHP20 sample. The curve also shows another peak at  $d_c = 5$  nm. Such small core size may be explained by the incomplete crystallization of MNP [22]. We note that iron-oxide nanoparticles often suffer from a degraded magnetization which is caused by a magnetic dead layer and incomplete oxygenation of the core.

## 2.2. Magnetic anisotropy

In Fig. 1(a), the experimentally measured  $M$ - $H$  curve of the immobilized SHP20 sample is represented with triangles. The value of  $K$  can be obtained by analyzing the immobilized sample  $M$ - $H$  curve. For this purpose, we previously obtained an empirical expression for the  $M$ - $H$  curve of immobilized MNP based on the numerical simulation results of the  $M$ - $H$  curve using the energy expression including the anisotropy term [17]. The empirical expression for the magnetization,  $M_{Imm}$ , of the immobilized MNP is given by

$$M_{Imm} = gM_0 + (1 - g)M_\infty \quad (8)$$

where  $M_0$  is the magnetization of suspended MNP given by Eq. (4). The value of  $M_\infty$  represent the magnetization of immobilized MNP in the case of infinite  $\sigma$ , and is given by

$$M_\infty = \int_0^\infty n_m(m)m_z(\xi, \sigma = \infty)dm \quad (9)$$

where

$$\frac{m_z(\xi, \sigma = \infty)}{m} = a_1 \tanh(b_1 \xi) + a_2 \tanh(b_2 \xi) + a_3 \tanh(b_3 \xi) \quad (10)$$

with the parameters  $a_1 = 0.3374$ ,  $b_1 = 0.8225$ ,  $a_2 = 0.1467$ ,  $b_2 = 0.3703$ ,  $a_3 = 0.0159$ , and  $b_3 = 0.0948$ .

The expression for  $g$  is

$$g = c_1 \tanh\left(d_1 \frac{H}{H_k}\right) + c_2 \tanh\left(d_2 \frac{H}{H_k}\right) + c_3 \tanh\left(d_3 \frac{H}{H_k}\right), \quad (11)$$

where,

$$\mu_0 H_k = \frac{2K}{M_s} \quad (12)$$

with the parameters  $c_1 = 0.893$ ,  $d_1 = 1.27$ ,  $c_2 = 0.04$ ,  $d_2 = 0.228$ ,  $c_3 = 0.067$ , and  $d_3 = 54.6$ .

The empirical expression given in Eq. (8) can be calculated using the distribution of  $n_m(m)$  given in Fig. 1(b) and using  $H_k$  as an adjustable parameter. In Fig. 1(a), experimentally measured  $M$ - $H$  curve of the immobilized SHP20 sample (triangles) is compared with the empirical expression (solid line). As shown, good agreement was obtained between calculated and experimental results when we choose  $\mu_0 H_k = 50$  mT. Note that the field range from  $\mu_0 H = 20$  to 80 mT corresponds to  $H/H_k = 0.4$  to 1.6.

The value of  $K$  can be obtained using the relation given in Eq. (12). As  $M_s = 270$  kA/m in the present sample,  $\mu_0 H_k = 50$  mT gives  $K = 6.8$  kJ/m<sup>3</sup>.

## 2.3. Characteristic relaxation time

The characteristic time  $\tau_o$ , which determines the Néel relaxation time  $\tau_N$  as given in Eq. (2), was obtained from the ACS of the immobilized MNP sample. In the experiment, weak external field with  $\mu_0 H_{ac} = 0.1$  mT was applied to satisfy the condition of magnetization linearity. The frequency of the excitation field was changed from 10 Hz to 100 kHz. The measurement was performed using equipment constructed in the laboratory.

In Fig. 2, the frequency dependence of ACS for the immobilized SHP20 sample is illustrated with triangles for the real part of the

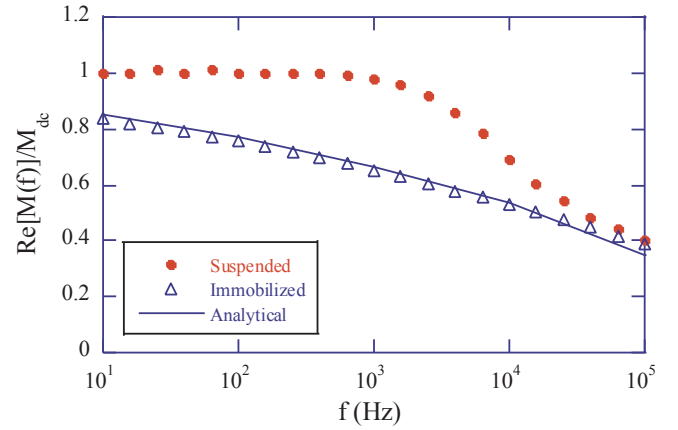


Fig. 2. Real part of the AC susceptibility of SHP20 samples. Symbols represent the experimental results. The solid line was calculated from Eq. (13) for  $\tau_o = 1 \times 10^{-10}$  s.

susceptibility,  $Re[M(f)]$ . The ACS measurement of suspended MNP sample is also plotted to show the difference between the suspended and immobilized case.

The value of  $\tau_o$  was estimated by analyzing the experimental results of immobilized sample by using the analytical relation previously explained in [23]

$$\frac{Re[M(f)]}{M_{dc}} = \frac{\int_0^\infty \frac{n_m(m)m^2}{1 + (2\pi f \tau_N)^2} dm}{\int_0^\infty n_m(m)m^2 dm} \quad (13)$$

The relation given in Eq. (13) can be calculated using the obtained distribution of  $n_m(m)$  and  $K$  value while taking  $\tau_o$  value as an adjustable parameter. The solid line in Fig. 2 was calculated using Eq. (13) with  $\tau_o = 1 \times 10^{-10}$  s. As shown, good agreement between calculated and experimental results was obtained.

Using this estimation procedure, we obtained the SHP20 sample parameters  $M_s$ ,  $\mu_0 H_k$ ,  $K$ , and  $\tau_o$ . These parameters are listed in Table 1. We also show the typical core diameter, denoted by  $d_{c,typ}$ , that gives the peak in the  $n_{dc}(d_c)V_c$  vs.  $d_c$  curve.

As shown in Figs. 1 and 2, magnetic properties reconstructed from the obtained parameters agree well with the experimental results. This agreement indicates the validity of the present procedure for parameters evaluation.

## 3. Resovist MNP parameter evaluation

Resovist samples are known to have admirable performance in both hyperthermia and MPI applications. However, it has been shown that Resovist MNP samples have wide distribution of parameters [24]. Therefore, we fractionated Resovist MNP using magnetic fractionation [25,26]. The Resovist MNP were fractionated into two MNP samples, MS1 and MS3, with narrower core size distribution. The iron concentration of the original sample was 28 mg (Fe)/mL for these three MNP. Magnetic properties and parameters of fractionated MNP were compared to those of the original Resovist MNP.

The measured  $M$ - $H$  curves of the suspended MS1, Resovist, and MS3

Table 1

Summary of magnetic parameters for the different MNP samples.

Sample	$M_s$ (kA/m)	$d_{c,typ}$ (nm)	$\mu_0 H_k$ (mT)	$K$ (kJ/m <sup>3</sup> )	$\tau_o$ (s)
SHP20	270	21	50	6.8	$1 \times 10^{-10}$
MS1	370	23	64.8	12.0	$1 \times 10^{-12}$
MS3	250	7	40	5.0	$1 \times 10^{-12}$
Resovist	300	7 & 26	53.3	8.0	$1 \times 10^{-12}$

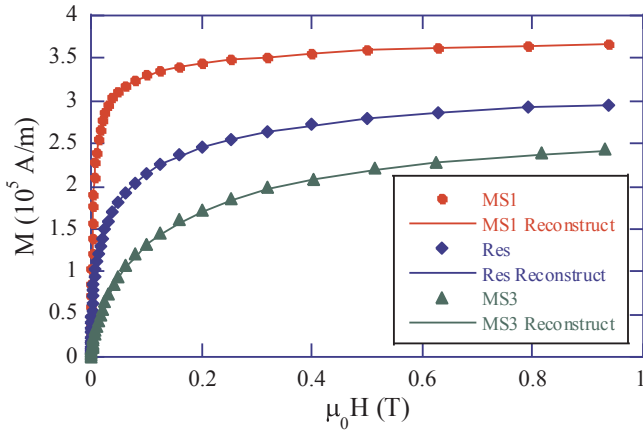


Fig. 3.  $M$ - $H$  curve of suspended MS1, Resovist, and MS3 samples.

samples are represented in Fig. 3 with circle, diamond, and triangle markers, respectively. MS1 had the highest value of  $M_s = 370$  kA/m, the Resovist sample had  $M_s = 300$  kA/m, and MS3 had  $M_s = 250$  kA/m.

Using the procedure described in Section. 2.1, we obtained the core size distribution for each MNP sample. Fig. 4 illustrates the estimated size distributions for each MNP sample. As shown in Fig. 4, the Resovist sample had a wide size distribution with typical core sizes of  $d_{c,typ} = 7$  nm and 26 nm. The MS1 sample had a narrower size distribution with typical core size around 23 nm, while MS3 sample had a smaller core size of 7 nm. The  $M$ - $H$  curves reconstructed using the obtained magnetic moment distributions are illustrated with the solid lines in Fig. 3 showing good agreement with the experimental  $M$ - $H$  curves.

The measured  $M$ - $H$  curves of the immobilized MNP samples were compared to the empirical expression using the procedure given in Section 2.2. The solid lines in Fig. 5 represent the empirical expressions when the values of  $\mu_0 H_k = 64.8$ , 53, and 40 mT were chosen for MS1, Resovist, and MS3, respectively. As shown, good agreement was obtained between the empirical and experimental results. Using the  $M_s$  and  $\mu_0 H_k$  values, we obtained  $K = 12$ , 8, and 5 kJ/m<sup>3</sup> for MS1, Resovist, and MS3, respectively.

Fig. 6 shows the measured real parts of ACS as compared to the analytical expression evaluated from Eq. (13) for MS1, Resovist, and MS3 samples. The best fit between experimental and analytical results was obtained at  $\tau_0 = 1 \times 10^{-12}$  s for the three samples.

We note that the difference in ACS between suspended and immobilized MS3 samples was caused by the large-diameter tail in the size distribution shown in Fig. 4. Particles with  $d_c$  7 nm have very short

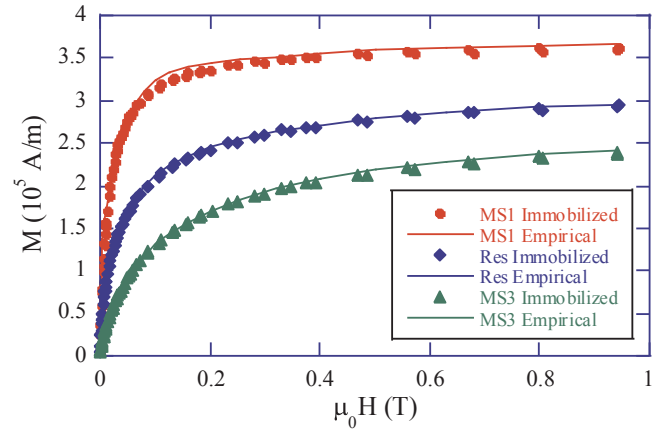


Fig. 5.  $M$ - $H$  curve of immobilized MS1, Resovist, and MS3 samples.

relaxation time, and, therefore, no difference occurs between the suspended and immobilized cases for these particles.

Table 1 shows the summary of parameters evaluated for the Resovist, MS1, and MS3 MNP samples. As shown, the MS1 sample showed the largest values of  $M_s$ ,  $H_k$  and  $K$ , while the MS3 sample showed the smallest values. On the other hand, characteristic time  $\tau_0$  was the same among the three samples.

We note that  $\tau_0$  can be expressed as [20]

$$\tau_0 = \frac{M_s}{2K} \frac{1}{\alpha \gamma} = \frac{1}{\mu_0 H_k} \frac{1}{\alpha \gamma} \quad (14)$$

where,  $\gamma = 1.76 \times 10^{11}(\text{sT})^{-1}$  is gyromagnetic ratio and  $\alpha$  is the dimensionless damping factor. Substituting the estimated  $H_k$  value listed in Table 1, we obtain the  $\tau_0$  value of the SHP20 sample as  $\tau_0 = 1.1 \times 10^{-9}$  s for typical value of  $\alpha = 0.1$ . The  $\tau_0$  value obtained from the ACS experiment ( $\tau_0 = 1 \times 10^{-10}$  s) was not significantly different from that calculated from Eq. (14).

On the other hand, for the case of multi-core MNP sample (Resovist, MS1 and MS3), the estimated  $\tau_0$  values ( $\tau_0 = 1 \times 10^{-12}$  s) were much smaller than the value ( $\tau_0 = 1 \times 10^{-9}$  s) calculated with Eq. (14). This difference may be explained if we take the interactions between the cores into account for the multi-core MNPs samples, as shown in Ref. [21]: It was shown that the magnetic interaction between particles decreases the effective  $\tau_0$  value and increases the effective  $K$  value.

Next, we discuss the relationship between the obtained parameters of the original and fractionated samples. We note that the original Resovist sample is a mixture of MS1 and MS3 samples with certain portion of each sample. We first evaluate the portion of MS1 and MS3 MNPs in the Resovist sample using the  $M_s$  values of the three samples. As was shown previously, the  $M_s$  values were 300, 370, and 250 kA/m for the Resovist, MS1, and MS3 samples, respectively. When the portion of MS1 MNP is given by  $a$ , the portion of MS3 MNP is given by  $1 - a$ . Therefore, the  $M_s$  value of the Resovist sample is given by the volume-weighted average of the MS1 and MS3 samples as  $300 = a \times 370 + (1 - a) \times 250$ . Therefore, we obtain  $a = 0.42$ . This means that the original Resovist sample contains 42% MS1 and 58% MS3 MNP.

Using the estimated value of  $a$ , we can find the value of  $K$  of a mixture of MS1 and MS3 MNP. As the  $K$  values are 12 and 5 kJ/m<sup>3</sup> for MS1 and MS3, respectively, the volume-weighted average of  $K$  is given by  $K = a \times 12 + (1 - a) \times 5 = 7.97$  kJ/m<sup>3</sup>. This value agrees well with  $K$  obtained for the Resovist sample ( $K = 8$  kJ/m<sup>3</sup>). Similarly,  $H_k$  value of the mixture is given by  $\mu_0 H_k = a \times 64.8 + (1 - a) \times 40 = 50.3$  mT. This value agrees with the  $\mu_0 H_k$  value obtained for the Resovist sample ( $\mu_0 H_k = 53.3$  mT).

The above results indicate that the parameters of the Resovist sample are given by the volume-weighted average of the two

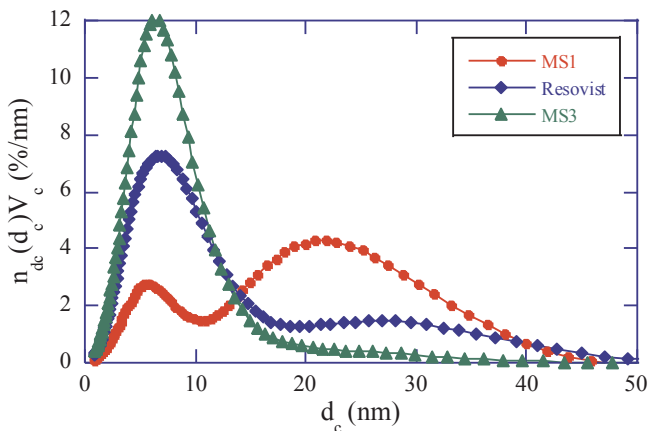
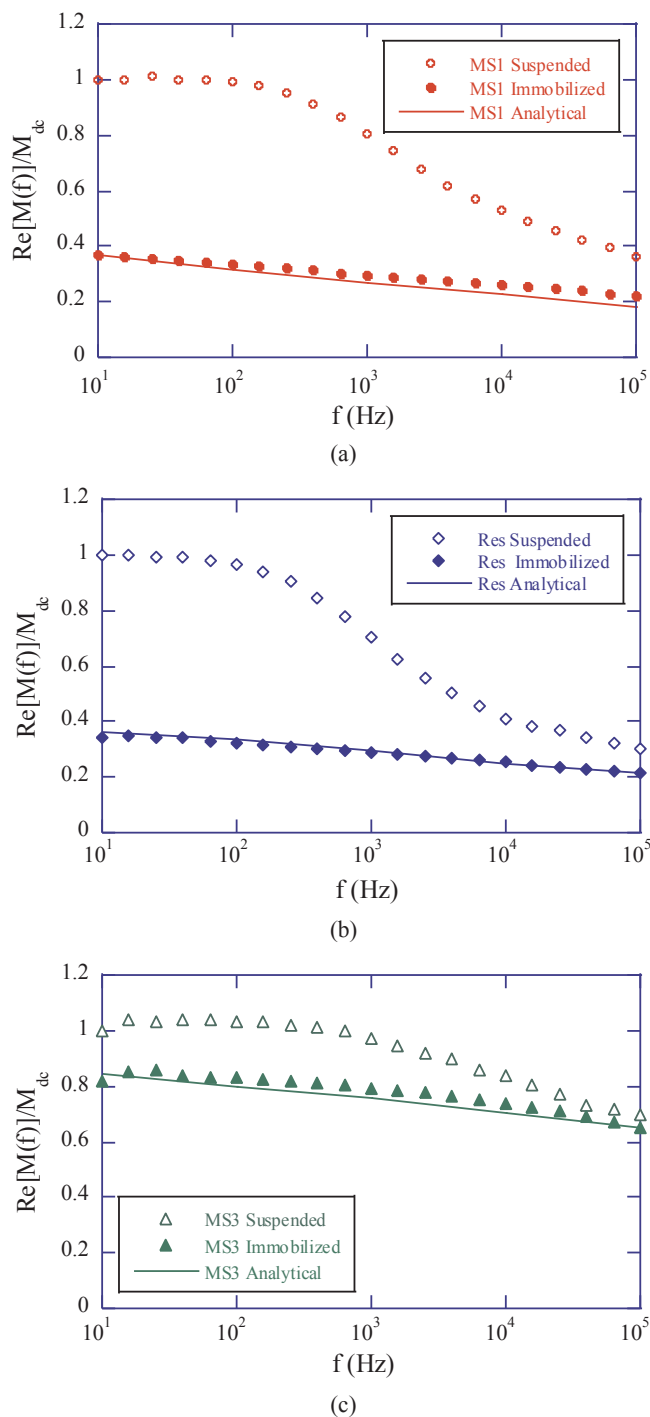


Fig. 4. Normalized core size distributions of MS1, Resovist, and MS3 samples. Distributions are estimated from  $M$ - $H$  curves of suspended MNP samples.

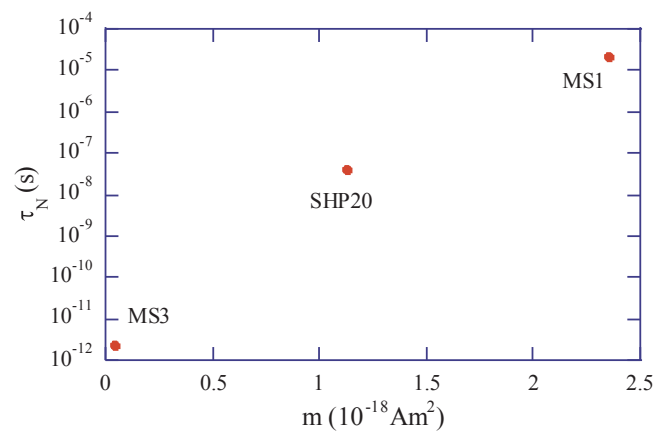


**Fig. 6.** AC susceptibility of immobilized (a) MS1, (b) Resovist, and (c) MS3 samples and the analytical result.

fractionated samples.

We note that the different values of  $M_s$  and  $K$  for the MS1 and MS3 samples indicate that these values are not constant in the MNP sample but change with the core size  $d_c$  of particles. Therefore, strictly speaking, we have to take the dependence of  $K$  and  $M_s$  on  $d_c$  into account. However, for simplicity, we assumed constant values of  $K$  and  $M_s$  in the sample for the evaluation procedure given in Section 2. Therefore, the parameters obtained with the present procedure represent the averaged values in each sample.

Finally, we estimated the  $m$  and  $\tau_N$  values of MNP samples using parameters listed in Table 1. Fig. 7 shows the relationship between



**Fig. 7.** Values of  $m$  and  $\tau_N$  estimated for SHP20, MS1, and MS3 samples for typical core size  $d_{c,typ}$  listed in Table 1.

typical values of  $m$  and  $\tau_N$  calculated using typical core size  $d_{c,typ}$  of SHP20, MS1, and MS3 samples. When we take the distribution of  $d_c$  into account, the  $m$  and  $\tau_N$  values exist around these typical values. The results shown in Fig. 7 are useful for the selection of MNP with appropriate values of  $m$  and  $\tau$  to be used in specific biomedical applications. We note, however, that it is necessary to collect more data, which will be our future work.

#### 4. Conclusions

We demonstrated a procedure for estimating the magnetic parameters of MNP samples ( $M_s$ ,  $d_c$ ,  $K$ , and  $\tau_0$ ) from independent experimental measurements, namely, suspended sample  $M$ - $H$  curve, immobilized sample  $M$ - $H$  curve and ACS measurements. Using these parameters, we can obtain magnetic moment  $m$  and Néel relaxation time  $\tau_N$  of a sample, which determine MNP performance in biomedical applications.

The proposed estimation procedure can be useful for the selection of MNP appropriate for specific applications. For example, among four studied MNP samples, the MS1 sample was the most suitable for the MPI application because it had large  $m$  and appropriate  $\tau_N$  for the AC field with a frequency around 10 kHz.

#### Acknowledgments

This work was supported in part by a Grant-in-Aid for Scientific Research (S) JP15H05764, Japan Society for the Promotion of Science, Japan.

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